Control Number: 45570

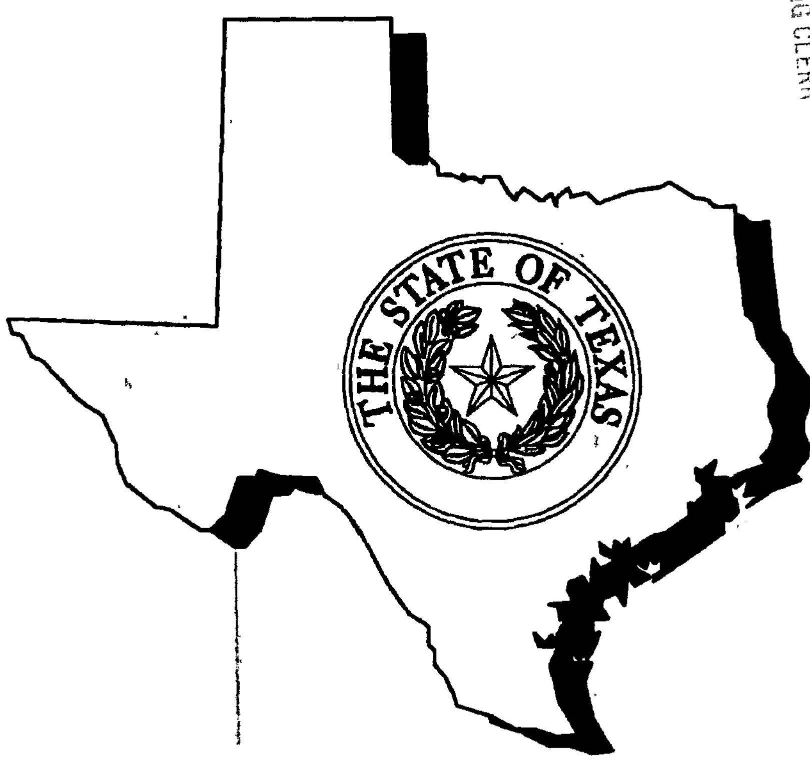
Item Number: 279

Addendum StartPage: 0

SOAH DOCKET NO. 473-16-2873.WS
PUC DOCKET NO. 45570

APPLICATION OF MONARCH	§	BEFORE THE STATE OFFICE
UTILITIES I, LP FOR AUTHORITY	§	OF
TO CHANGE RATES	§	ADMINISTRATIVE
	§	HEARINGS

RECEIVED
2016 AUG 24 AM 10: 55
PUBLIC UTILITY COMMISSION
FILING CLERK



WORKPAPERS OF
EMILY SEARS
WATER UTILITY REGULATION
PUBLIC UTILITY COMMISSION OF TEXAS
AUGUST 24, 2016

THE VALUE LINE® Investment Survey®

Part 1 Summary & Index

File at the front of the *Ratings & Reports* binder. Last week's *Summary & Index* should be removed.

July 15, 2016

TABLE OF SUMMARY & INDEX CONTENTS

SCREENS

The Median of Estimated
PRICE-EARNINGS RATIOS
of all stocks with earnings

18.0

26 Weeks Ago	Market Low 3-9-09	Market High 5-21-15
17.3	10.3	19.3

The Median of Estimated
DIVIDEND YIELDS
(next 12 months) of all dividend paying stocks under review

2.3%

26 Weeks Ago	Market Low 3-9-09	Market High 5-21-15
2.4%	4.0%	2.0%

The Estimated Median Price
APPRECIATION POTENTIAL
of all 1700 stocks in the Value Line universe in the hypothesized economic environment 3 to 5 years hence

45%

26 Weeks Ago	Market Low 3-9-09	Market High 5-21-15
50%	185%	35%

ANALYSES OF INDUSTRIES IN ALPHABETICAL ORDER WITH PAGE NUMBER

Numeral in parenthesis after the industry is rank for probable performance (next 12 months).

*Reviewed in this week's issue.

In three parts: This is Part 1, the Summary & Index. Part 2 is Selection & Opinion. Part 3 is Ratings & Reports. Volume LXXI, No. 48.

Published weekly by VALUE LINE PUBLISHING LLC, 485 Lexington Avenue, New York, N.Y. 10017-2630

0000002

ASIA EDITION

American States Water Co.

U.S. NYSE

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Fe edback on ew quotes? EMAIL US

QUOTE COMPANY & PEOPLE RESEARCH & RATING

MARKET OPEN

$43.12

▼-0.30 (-0.691%)

Jul 18, 2016 1 24 p ET EDT
Real time quote

25.8K	188.8K
Current Vol	65 Day Avg

Previo Clo	$43.42
Ope	$43.46
Day Range	$43.07 - $43.64
52 Wk Range	$35.80 - $47.24
Market Valu	$1.6B
Ytd t et Change	2.8%
1 Yr et Change	10.6%
P/E Ratio(TTM)	27.66
EPS(TTM)	$1.56
Div & Yield	$0.90 (2.08%)
Beta	0.74

1Y COMPARE

Mar 10
U.AWR $41.2900

16 Apr 16

43.441

36.55M

$0.22 (Jun 1, 2016)

May 16, 2016

65.52%

$638,239

932.68K (6/30/2016)

-0.26%

2.59%

$43.4K

1.13%

SEE COMPANY FINANCIALS ›
SEE COMPANY RATINGS ›

NEWS

OTHER DOW JONES PRESS RELEASES

May 8 2015	Research Reports
Sep 17 201	American States Water Set for Upside
Aug 4 201	Macquarie Infrastructure Hoists Its Dividend
Ma 17 2012	Barron's Research Reports
Oct 16, 2006	Liquid Assets
Jul 31 2006	Staying Liquid
Jul 14 2003	Follow-Up
Nc 1999	Follow-Up
Aug 30 999	Follow-Up
Aug 16 1 99	Tsunami
Oct 5 1998	Liquid Investments

American States Water Co. engages in the provision of water supply and electricity distribution services. It operates through.

SEE COMPANY OVERVIEW ›

Robert J Sprowls

Eva G Tang

James C Cotton III

John R Fielder

Janine L Zanelli

MAJOR HOLDERS

INSTITUTIONAL DIRECT HOLDERS

Name	Sha Held	% Outstanding	Change in Sha	% of As ets	As Of Date
iSha Core S&P Small Cap ETF	1.08M	2.94%	1.37K	0.26%	07/6/16
Vangu ard Small Cap Inde Fund	758.25K	2.07%	7.17K	0.06%	05/31/16
Vangu rd Total Stock Market Inde Fund	708.45K	1.94%	4.84K	0.01%	05/31/16
iSha Ru ell 2000 ETF	568.73K	1.56%	-6.27K	0.1%	07/6/16
Vangu ard Small Cap Valu Inde Fund	456.61K	1.25%	18.73K	0.1%	06/30/16
Vangu ard Extended Market Inde Fund	417.2K	1.14%	6.35K	0.04%	05/31/16

0000003

Gc emment Pensio i Fund - Global (The)	403.59K	1.1%	12 83K	0%	12/31/15
DFA US Micro Cap Portfolio	402K	1.1%	0	0.28%	04/30/16
Pictet - Water	384.26K	1.05%	3 03K	0.47%	12/31/15
Baillie Gifford Investment Funds ICVC - Div ersified Growth Fd.	382.32K	1.05%	90K	0.21%	03/31/16

Symbol	% Chg	Market Cap
CPW	-0 224%	$401.6M
AR	1 316%	$295.8M
[illegible]	-0.962%	$571.3M
EX	0.265%	$675.3M
CDZ	0%	$120.6M
[illegible]	1.366%	$104.5M
	-0.757%	$1.6B
WI	0 073%	$6B
AWK	-0.026%	$14.5B
W	-1 195%	$803.6M

More nformatic on AWR
Competitor Data Provided By:

ASIA EDITION

American Water Works Co.

U.S. NYSE

Add to Watchlist

Feedback on · new quotes? EMAIL US

QUOTE COMPANY & PEOPLE RE [illegible] RCH & RATINGS

MARKET OPEN

$81.57

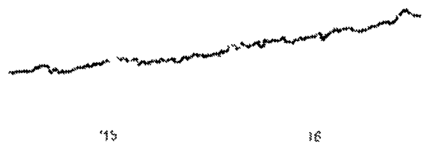
▼-0.02 (-0.025%)

Jul 18 2016 1 30 p.m ET EDT
Real time quote

565.8K	1.3M
Current Vol	65 Day Avg

Pri vious Close	$81.59
Ope	$81.60
Day Range	$81.41 - $81.95
52 Wk Range	$50.16 - $85.24
Market Valu	$14.5B
Ytd i et Change	36.5%
1 Yr et Change	58.8%
P/E Ratio(TTM)	30.75
EPS(TTM)	$2.65
Div & Yield	$1.50 (1.84%)
Beta	0.55

1Y COMPARE



$177.71M

$0.38 (Jun 1, 2016)

May 5, 2016

89.26%

$478,258

5.94M (6/30/2016)

-0.65%

3.35%

$1.89M

1.19%

SEE COMPANY FINANCIALS

SEE COMPANY RATINGS

NEWS

OTHER DOW JONES PRESS RELEASES

Jul 8 2016	11 Utilities Picks After First-Half Surge
Mar 8 2016	4 Stocks with Market-Beating Growth & Yields
Ma 1 2016	American Water Works Will Join S&P 500
Feb 29 2016	American Water Stock at Full Value
i 23, 2016	A Dozen Utilities for Income Investors
A[illegible] 10, 20[illegible]	Utilities: Buy Them for the Dividends, Bet On the Growth
Ju i 9, [illegible]	American Water Works Awash With Upside
Apr 24, [illegible]	4 Picks from Reaves Utility Income Fund
J[illegible] 20[illegible]	Payouts Rise Despite Energy Fears
30, 2014	Northeast Utilities Shares Look Fully Valued
May 5, 20[illegible]	Undervalued Energy Spinoff Could Pay Dividend
[illegible] 3, 20[illegible]	The Many Ways to Tap the Water Boom
May [illegible], 201[illegible]	The Many Ways to Tap the Water Boom
D[illegible] 19, 2013	These Five Stocks Could Be Taper Losers

American Water Works Co., Inc. provides water and wastewater utility services to residential, commercial, industrial, public,.

SEE COMPANY OVERVIEW

Susan N Story

Linda G Sullivan

Mark S Smith

Martin Uczen

Bruce Hauk

MAJOR HOLDERS

INSTITUTIONAL DIRECT HOLDERS

Name	Sha i Held	% Outstanding	Change in Sh	% of As ets	As Of Date
Vanguard Mid Cap Inde (Fund	3.97M	2.23%	11.16K	0.49%	06/30/16
Vanguard Total Stock Market Inde (Fund	3.46M	1.95%	54.62K	0.07%	05/31/16
SPDR Serie · Utilitie i Select Sector SPDR Fund	2.43M	1.37%	15.73K	2.3%	07/6/16

0000005

ASIA EDITION

Aqua America Inc. U.S. NYSE

Add to Watchl st

Feedback on our new quotes? EMAIL US

QUOTE COMPANY - PEOPLE RESEARCH & RATINGS

MARKET OPEN

$34.05

▲ 0.02 (0.059%)

16, 2016 1 30 p ET EDT Real I quo

209.5K	768.8K
Current Vol	65 Day Avg

Previo Clo	$34.03
Open	$34.03
Day Range	$34.01 - $34.20
52 Wk Range	$24.45 - $35.83
Market Valu	$6B
Yld et Change	14.3%
1 Yr et Change	33.8%
P/E Ratio(TTM)	29.61
EPS(TTM)	$1.15
Div & Yield	$0.71 (2.09%)
Beta	0.69

1Y COMPARE

ow :

Sha ut
177.27M

atest Di nd
$0.18 (Jun 1, 2016)

Ex d Date
May 11, 2016

stitut al Owr shi
51.66%

Re Pe Em l
$504,938

ort te st
5.34M (6/30/2016)

-1.37%

3.02%

$-461.68K

0.72%

SEE COMPANY FINANCIALS

SEE COMPANY RATINGS

NEWS

OTHER DOW JONES PRESS RELEASES

Jul 8 2016	11 Utilities Picks After First-Half Surge
Ju 18 2016	Aqua America Is Overvalued
Aug 10 2015	Utilities: Buy Them for the Dividends, Bet On the Growth
Apr 25 2015	Water Asset Management: Hunting Liquid Assets
De 30, 2014	Northeast Utilities Shares Look Fully Valued
Ma 23, 2013	Waiting for the Other Shoe
Jul 18, 2012	Aqua America May Be Fairly Priced
Mr 3, 2012	Research Reports
Aug 27, 2011	Research Reports
Jul 18, 2011	SJW, California Water Seen as Favored
Feb 16, 2010	Consolidation to Drive Water-Sector Growth
Ma 2009	Earnings Upside in Gas and Water
N 2008	Stimulus Plan May Lift Infrastructure Plays
Ja 2, 2008	Preview

Aqua America, Inc. operates as a holding company for regulated water and wastewater utilities serving people in Pennsylvania,

SEE COMPANY OVERVIEW

MAJOR HOLDERS

INSTITUTIONAL DIRECT HOLDERS

Name	Sha Held	% Outstanding	Change In Shares	% of As ets	As Of Date
Pictet - Water	4.08M	2.3%	32.21K	4.09%	12/31/15
SPDR S&P Dividend ETF	3.83M	2.16%	4.59K	0.98%	07/6/16
Vanguard Small Cap Inde Fund	3.64M	2.06%	24.3K	0.23%	05/31/16

Nicholas DeBenedictis

Christopher H Franklin

Richard S Fox

David P Smeltzer

Whitney S Kellett

0000006

ASIA EDITION

California Water Service Group

U.S. NYSE

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EMAIL US

QUOTE COMPANY & PEOPLE RESEARCH RATINGS

MARKET OPEN

$32.74

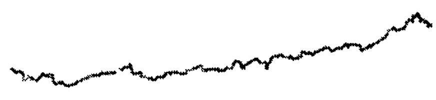
▼-0.27 (-0.818%)

Jul 18 2016 1 30 p.m ET EDT
Real time quote

73.2K	297.9K
Current Vol	65 Day Avg

Previous Close	$33.01
Open	$32.91
Day Range	$32.73 - $33.19
52 Wk Range	$19.55 - $35.62
Market Value	$1.6B
Ytd Pct Change	40.7%
1 Yr Pct Change	38.6%
P/E Ratio(TTM)	36.78
EPS(TTM)	$0.89
Div & Yield	$0.69 (2.11%)
Beta	0.73

1Y COMPARE ▾



Shares Outstanding
47.97M

Last Dividend
$0.17 (May 20, 2016)

Ex-Dividend Date
May 5, 2016

Institutional Ownership
75.5%

$509,186

2.3M (6/30/2016)

+3.83%

4.84%

$-358.93K

0.57%

SEE COMPANY FINANCIALS
SEE COMPANY RATINGS

NEWS

OTHER DOW JONES PRESS RELEASES

May 2 201	California Water Shares Lack Upside
Jul 18, 201	SJW, California Water Seen as Favored
Jun 4 2011	An Emerging IMF Chief?
Feb 16 2010	Consolidation to Drive Water-Sector Growth
Mar 19 2009	Earnings Upside in Gas and Water
Nov 8 2008	Research Reports
11 2007	Research Reports
Dec 2005	A Water Co. That Looks Refreshing
Jul 14 2003	Follow-Up
Nov 1999	Follow-Up

California Water Service Group engages in the production, purchase, storage, treatment, testing, distribution and sale of..

SEE COMPANY OVERVIEW

Peter C Nelson

Martin A Kropelnicki

Timothy D Treloar

Thomas F Smegal III

Robert J Kuta

MAJOR HOLDERS

INSTITUTIONAL DIRECT HOLDERS

Name	Shares Held	% Outstanding	Change in Shares	% of Assets	As Of Date
Pictet - Water	2.31M	4.81%	173.16K	2.27%	12/31/15
iShares Core S&P Small Cap ETF	1.41M	2.94%	1.8K	0.27%	07/6/16
Baillie Gifford Investment Funds ICVC - Diversified Growth Fd.	1.1M	2.29%	300K	0.48%	03/31/16
Vanguard Small Cap Index Fund	987.51K	2.06%	4.7K	0.06%	05/31/16
Vanguard Total Stock Market Index Fund	956.59K	1.99%	5.12K	0.01%	05/31/16
iShares Russell 2000 ETF	748.56K	1.56%	-8.28K	0.1%	07/6/16
Goldman Sachs Small Cap Value Fund	690.99K	1.44%	690.99K	0.42%	03/31/16

0000007

ASIA EDITION

Connecticut Water Service Inc.

U.S. Nasdaq

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EMAIL US

QUOTE · COMPANY & PEOPLE · RESEARCH & RATING

MARKET OPEN

$51.48

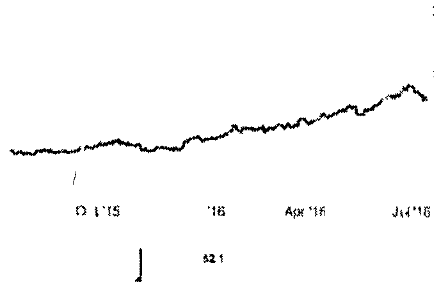
▼-0.50 (-0.962%)

Jul 18, 2016 1:08 p.m. ET EDT
Composite

14K	51.8K
Current Vol	65 Day Avg

Previous Close	$51.98
Open	$51.94
Day Range	$51.39 - $52.19
52 Wk Range	$33.15 - $56.62
Market Value	$571.3M
Ytd Pct Change	35.4%
1 Yr Pct Change	46.3%
P/E Ratio(TTM)	25.15
EPS(TTM)	$2.05
Div & Yield	$1.13 (2.2%)
Beta	0.69

1Y · COMPARE



10.99M

$0.28 (Jun 15, 2016)

May 27, 2016

44.4%

$366,778

425.85K (6/30/2016)

+2.76%

3.98%

$-72.33K

0.67%

SEE COMPANY FINANCIALS
SEE COMPANY RATINGS

NEWS

OTHER DOW JONES · PRESS RELEASES

Mar 14 2016	Nasdaq Dividend Index: Travelers In, ConocoPhillips, Darden Out
Aug 27 2011	Research Reports
Apr 8 2002	Follow-Up
Oct 1 2001	Corrections & Amplifications
Mar 5 2001	Cover Story, Part 2
Aug 21 2000	Shiver Me Timbers!
Nov 8 1999	Follow-Up
Aug 30 1999	Follow-Up

Connecticut Water Service, Inc. manages, operates, and regulates water supply. It operates through the following segments:.

SEE COMPANY OVERVIEW

MAJOR HOLDERS

INSTITUTIONAL · DIRECT HOLDERS

Name	Shares Held	% Outstanding	Change in Shares	% of Assets	As Of Date
Vanguard Total Stock Market Index Fund	217.47K	1.98%	0	0%	05/31/16
iShares Russell 2000 ETF	169.14K	1.54%	-1.86K	0.04%	07/6/16
Vanguard Extended Market Index Fund	120.92K	1.1%	1.29K	0.02%	05/31/16
Lord Abbett Micro Cap Value Fund	105.4K	0.96%	9.7K	3.83%	04/30/16
DWS Water Sustainability Fund	103.49K	0.94%	0	2.36%	05/31/16
DFA US Small Cap Portfolio	101.3K	0.92%	16.17K	0.04%	04/30/16
Government Pension Fund - Global (The)	94.95K	0.86%	81.71K	0%	12/31/15
DFA US Micro Cap Portfolio	85.16K	0.78%	1.74K	0.08%	04/30/16
Calvert Global Water Fund	76.11K	0.69%	3.76K	0.99%	05/31/16
Vanguard Dividend Appreciation Index Fund	73.82K	0.67%	354	0.02%	06/30/16

Eric W Thornburg

David Charles Benoit

Peter J Bancroft

Craig J Patla

Robert J Doffek

0000008

ASIA EDITION

Middlesex Water Co.

U.S. Nasdaq

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QUOTE COMPANY & PEOPLE RESEARCH & RATINGS

MARKET OPEN

$41.69

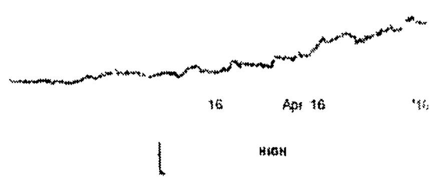
▲ 0.11 (0.265%)

Jul 18, 2016 1:22 p.m. ET EDT
Real time quote

22.1K	98.4K
Current Vol	65 Day Avg

Previous Close	$41.58
Open	$41.43
Day Range	$41.43 - $41.99
52 Wk Range	$22.12 - $44.11
Market Value	$675.3M
Ytd Pct Change	57.1%
1 Yr Pct Change	79.2%
P/E Ratio(TTM)	32.29
EPS(TTM)	$1.29
Div & Yield	$0.80 (1.91%)
Beta	0.70

1Y COMPARE



16.24M

$0.20 (Jun 1, 2016)

May 11, 2016

42.88%

$436,259

451.66K (6/30/2016)

+11.56%

2.89%

$-100.28K

0.7%

SEE COMPANY FINANCIALS

SEE COMPANY RATINGS

NEWS

OTHER DOW JONES PRESS RELEASES

Jul 14 2003	Follow-Up
Apr 8, 2002	Follow-Up
Nov 8 1999	Follow-Up
Aug 30 1999	Follow-Up

MAJOR HOLDERS

INSTITUTIONAL DIRECT HOLDERS

Name	Shares Held	% Outstanding	Change in Shares	% of Assets	As Of Date
Vanguard Total Stock Market Index Fund	366.12K	2.25%	0	0%	05/31/16
iShares Russell 2000 ETF	247.21K	1.52%	-2.74K	0.04%	07/6/16
Vanguard Extended Market Index Fund	204.98K	1.26%	1.48K	0.02%	05/31/16
ASN Beleggingsfondsen NV - Milieu & Waterfonds	195.12K	1.2%	92	1.87%	06/30/16
DFA US Small Cap Portfolio	137.17K	0.85%	19.88K	0.04%	04/30/16
DFA US Micro Cap Portfolio	119.16K	0.73%	294	0.08%	04/30/16
Calvert Global Water Fund	104.9K	0.65%	5.18K	1.05%	05/31/16
Government Pension Fund - Global (The)	103.61K	0.64%	14.91K	0%	12/31/15
iShares Russell 2000 Growth ETF	95.79K	0.6%	-444	0.07%	07/6/16
PowerShares Water Resources Portfolio	86.7K	0.53%	-230	0.53%	07/7/16

Middlesex Water Co. owns and operates regulated water utility and wastewater systems in New Jersey, Delaware and Pennsylvania..

SEE COMPANY OVERVIEW

Dennis W Doll

Richard M Risoldi

A Bruce O'Connor

Kim C Hanemann

Bernadette M Sohler

ASIA EDITION

SJW Corp. U.S.: NYSE

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QUOTE COMPANY & PEOPLE RE: ARCH & RATINGS

MARKET OPEN

$38.81

▼-0.53 (-1.347%)

Jul 18, 2016 1:31 p.m. ET EDT
Real time quote

16.8K	81.1K
Current Vol	65 Day Avg

Pr vio : Clo	$39.34
Ope	$39.37
Day Range	$38.72 - $39.42
52 Wk Range	$27.54 - $39.48
Market Valu	$803.6M
Ytd r al Change	30.9%
1 Yr al Change	25.4%
P/E Ratio(TTM)	21.92
EPS(TTM)	$1.77
Div & Yield	$0.81 (2.09%)
Beta	0.85

1Y COMPARE ▾

20.43M

$0.20 (Jun 1, 2016)

May 5, 2016

44.52%

$762,110

425.48K (6/30/2016)

+8%

2.95%

$-24.67K

0.66%

SEE COMPANY FINANCIALS
SEE COMPANY RATINGS

NEWS

OTHER DOW JONES PRESS RELEASES

Jul 9 2016	Elliott Associates Wants to Unlock Value in Imperva
Sep 23 2011	Jefferies Group CEO Sells Stock to Leucadia
Sep 16 2011	Hyatt Hotels CEO Buys $1.43 Million in Stock
Jul 18 2011	SJW, California Water Seen as Favored
Feb 19 2007	13D Filings
No 13 2006	13D Filings
Ma 27 2006	13D Filings
No 8 1999	Follow-Up

SJW Corp. operates as a holding company, which through its subsidiaries engages in water supply business. Its subsidiaries..

SEE COMPANY OVERVIEW

MAJOR HOLDERS

INSTITUTIONAL DIRECT HOLDERS

Name	Sha : Held	% Outstanding	Change in Sha	% of As ets	As Of Date
Royc Total Return Fund	400 4K	1.98%	0	0.55%	03/31/16
Vanguard Total Stock Market Inde Fund	313.84K	1.54%	0	0%	05/31/16
iShar Ru all 2000 ETF	253.63K	1.24%	-2.79K	0.04%	07/6/16
Gabelli Utilitie Fund (The)	214K	1.05%	-11K	0.39%	03/31/16
Vanguard Extended Market Inde Fund	199.22K	0.98%	2.47K	0.02%	05/31/16
DFA US Micro Cap Portfolio	195.54K	0.96%	0	0.12%	04/30/16
DFA US Small Cap Portfolio	192.94K	0.95%	24.41K	0.05%	04/30/16
EQ/GAMCO Small Company Valu Portfolio	180K	0.88%	-20K	0.27%	03/31/16
Vangu rd Dividend Appreciatio Inde Fund	134.43K	0.66%	649	0.02%	06/30/16
PowerShares Water Resource Portfolio	130.5K	0.64%	-345	0.72%	07/7/16

W Richard Roth

Andrew R Gere

James Patrick Lynch

Andrew F Walters

Curtis A Rayer Jr.

ASIA EDITION

York Water Co.

U.S. Nasdaq

Add to Watchlist

:back ur new qu ote s? EMAIL US

QUOTE

MARKET OPEN

$31 19

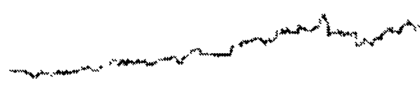
▼-0.07 (-0.224%)

Jul 18, 2016 1:29 p.

23.7K	63.9K
Current Vol	65 Day Avg

Previous Close	$31.26
Open	$31.28
Day Range	$31.15 - $31.89
52 Wk Range	$19.69 - $33.40
Market Value	$401.6M
Ytd Net Change	25.1%
1 Yr Net Change	43.9%
P/E Ratio(TTM)	32.41
EPS(TTM)	$0.97
Div & Yield	$0.62 (1.99%)
Beta	0.71

1Y COMPARE



12.85M

$0.16 (Jul 15, 2016)

Jun 28, 2016

31.11%

$453,442

359.12K (6/30/2016)

+15.87%

2.83%

$91.63K

1.55%

SEE COMPANY FINANCIALS

SEE COMPANY RATINGS

NEWS

OTHER DOW JONES PRESS RELEASES

18 201	Adobe's John E. Warnock Sells 40,000 Shares
Feb 1 2010	Consolidation to Drive Water-Sector Growth
Oct 10 2009	13D Filings
Apr 8 2002	Follow-Up
Ma 2001	Cover Story, Part 2

York Water Co. engages in impounding, purifying and distributing drinking water in Pennsylvania. The company operates within..

SEE COMPANY OVERVIEW

MAJOR HOLDERS

INSTITUTIONAL DIRECT HOLDERS

Name	Shares Held	% Outstanding	Change in Shs	% of Assets	As Of Date
Vanguard Total Stock Market Index Fund	280.68K	2.19%	0	0%	05/31/16
iShares Ru ell 2000 ETF	200.35K	1.56%	2.21K	0.03%	07/6/16
Royce Total Return Fund	166.63K	1.3%	0	0.19%	03/31/16
Vanguard Extended Market Index Fund	141.42K	1.1%	1 14K	0.01%	05/31/16
Gabelli Utilities Fund (The)	88K	0.69%	0	0.13%	03/31/16
DFA US Small Cap Portfoli	86.72K	0.68%	13 67K	0.02%	04/30/16
iSha Ru ell 2000 Growth ETF	82.29K	0.64%	-380	0 05%	07/6/16
DFA US Mic Cap Portfolio	76.38K	0.6%	4.8K	0.04%	04/30/16
Bridgeway Ultra Small Company Market Fund	68.05K	0.53%	-1 8K	0.64%	03/31/16
	61.36K	0.48%	3 88K	1.8%	06/27/16

Jeffrey R Hines

Joseph Thomas Hand

Kathleen M Miller

Vernon L Bracey

Mark S Snyder

0000011

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Indexes PEs and Yields

DJ latest 52-week earnings and dividends adjusted by Dow Divisors at Friday's close. S & P Dec. 4-quarter's GAAP earnings as reported and indicated dividends based on Friday close.S & P 500 P/E ratios based on GAAP earnings as reported. For additional earnings series, please refer to www.spglobal.com. DJ latest available book values for FY 2014 and 2013, and S & P latest for 2014 and 2013. r-Revised data

	Last Week	Prev. Week	Year Ago
DJ Ind Avg	**18516.55**	**18146.74**	**18086.45**
P/E Ratio	19.79	19.40	16.20
Earns Yield %	5.05	5.15	6.17
Earns $	935.48	935.41	1116.60
Divs Yield %	2.44	2.48	2.34
Divs $	450.92	450.92	422.77
Mkt to Book	3.39	3.32	3.13
Book Value $	5465.34	5465.34	5770.32
DJ Trans Avg	**7985.17**	**7683.28**	**8293.61**
P/E Ratio	12.45	11.99	19.22
Earns Yield %	8.03	8.34	5.20
Earns $	641.23	640.56	431.40
Divs Yield %	1.45	1.50	1.34
Divs $	115.46	115.46	110.82
Mkt to Book	3.66	3.52	3.63
Book Value $	2180.11	2180.11	2285.19
DJ Utility Avg	**710.12**	**717.37**	**575.42**
P/E Ratio	23.82	24.06	16.42
Earns Yield %	4.20	4.16	6.09
Earns $	29.81	29.81	35.05
Divs Yield %	3.09	3.06	3.67
Divs $	21.97	21.97	21.09
Mkt to Book	2.16	2.18	1.91
Book Value $	328.93	328.93	301.58
S & P 500 Index	**2161.74**	**2129.90**	**2126.64**
P/E Ratio	25.01	24.62	21.43
Earns Yield %	4.00	4.06	4.67
Earns $	86.43	86.52	99.25
Divs Yield %	2.13	2.15	2.05
Divs $	46.05	45.79	43.60
Mkt to Book	2.97	2.93	2.97
Book Value $	726.96	726.96	715.84
S & P Ind Index	**2920.79**	**2883.04**	**2835.98**
P/E Ratio	29.59	29.54	22.98
Earns Yield %	3.38	3.38	4.35
Earns $	98.71	97.59	123.40
Divs Yield %	2.05	2.07	2.02
Divs $	59.88	59.68	57.29
Mkt to Book	3.93	3.88	3.78
Book Value $	743.97	743.97	751.00

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Earnings History	6/29/2015	9/29/2015	12/30/2015	3/30/2016
EPS Est.	0.41	0.56	0.3	0.32
EPS Actual	0.41	0.56	0.31	0.28
Difference	N/A	N/A	0.01	-0.04
Surprise %	N/A	N/A	3.30%	-12.50°

EPS Trend	Current Qtr	Next Qtr.	Cu nt Year	Next Ye
Current Estimate	0.44	0.6	1.66	1.73
7 Days Ago	0.44	0.6	1.67	1.72
30 Days Ago	0.44	0.6	1.66	1.72
60 Days Ago	0.44	0.6	1.66	1.72
90 Days Ago	0.47	0.58	1.68	1.75

EPS Revisions	Current Qtr.	Next Qtr.	Cu nt Ye	Next Year
Up Last 7 Days	N/A	N/A	N/A	1
Up Last 30 Days	N/A	1	1	1
Down Last 30 Days	N/A	N/A	N/A	N/A
Down Last 90 Days	N/A	N/A	N/A	N/A

Growth Estimates	AWR	Industry	Sector	S&P 500
Current Qtr.	7.30%	0.17		
Next Qtr.	7.10%	0.31		
Current Year	3.60%	0.00		
Next Year	4.20%	0.05		
Next 5 Years (per annum)	3.85%	0.09		
Past 5 Years (per num)	7.00%	N/A		

Low 35.00 High 44.00
Current 43.12

Upgrades & Downgrades >

↑ Upgrade	Ladenburg Thalmann: Sell to Neutral	5/11/2016
↓ Downgrade	Ladenburg Thalmann: Neutral to Sell	2/26/2016
↓ Downgrade	Brean Capital: Buy to Hold	10/31/2014
↑ Upgrade	Brean Capital: Hold to Buy	2/28/2014
	Ladenburg Thalmann: Buy	2/24/2014
↓ Downgrade	Brea Capital: Buy to Hold	10/22/2013

Mc Upgrade & Downgrade

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Ago Sales	M	590.21M	5B	5B
Sales Growth (year/est)	6.40%	6.00%	6.10%	4.60%

Earnings History	6/29/2015	9/29/2015	12/30/2015	3/30/2016
EPS Est.	0.67	0.94	0.55	0.46
EPS Actual	0.68	0.96	0.55	0.46
Difference	0.01	0.02	N/A	N/A
Surprise %	1.50%	2.10%	N/A	N/A

EPS Trend	Current Qtr	Next Qtr.	Current Year	Next Year
Current Estimate	0.73	1.02	2.83	3.04
7 Days Ago	0.73	1.02	2.83	3.04
30 Days Ago	0.73	1.02	2.82	3.04
60 Days Ago	0.73	1.02	2.82	3.04
90 Days Ago	0.74	1 02	2.82	3.04

EPS Revisions	Current Qtr.	Next Qtr	Current Year	Next Year
Up Last 7 Days	1	1	1	N/A
Up Last 30 Days	1	1	2	N/A
Down Last 30 Days	N/A	N/A	N/A	N/A
Down Last 90 Days	N/A	N/A	N/A	N/A

Growth Estimates	AWK	Industry	Sector	S&P 500
Current Qtr.	7.40%	0.17		
Next Qtr.	6.30%	0.31		
Current Year	7.20%	0.00		
Next Year	7.40%	0.05		
Next 5 Years (per annum)	7.27%	0.09		
Past 5 Years (per annum)	9.23%	N/A		

Average 75.15

Low 62.00 | Current 81 56 | High 90.00

Upgrades & Downgrades >

↓ Downgrade	BofA/Merrill: Buy to Neutral	7/6/2016
↓ Downgrade	Ladenburg Thalmann: Buy to Neutral	10/15/2015
	Goldman. Neutral	6/29/2015
↑ Upgrade	Ladenburg Thalmann: Neutral to Buy	6/8/2015
	Guggenheim: Buy	4/22/2015
↓ Downgrade	Robert W. Baird: Outperform to Neutral	12/1/2014

More Upgrades & Downgrades

Avg. Estimate	210.11M	228.26M	838.19M	880.81M
Low Estimate	208M	224.4M	818.9M	846M
High Estimate	213.37M	232M	858M	938M
Year Ago Sales	205.76M	221.05M	814.2M	838.19M
Sales Growth (year/est)	2.10%	3.30%	2.90%	5.10%

Earnings History	6/29/2015	9/29/2015	12/30/2015	3/30/2016
EPS Est.	0.32	0.38	0.29	0.28

1 Strong Buy 2 Buy 3 Hold 4 Under-perform 5 Sell

Analyst Price Targets (7) >

Average 32.86

Low 27.00 Current 34 05 High 38.00

Upgrades & Downgrades >

Ladenburg Thalma Bi

EPS Trend	Cu nt Qtr.	Next Qtr.	Cu nt Year	Next Year
Current Estimate	0.34	0.41	1.33	1.41
7 Days Ago	0.34	0.41	1.33	1.41
30 Days Ago	0.34	0.41	1.33	1.41
60 Days Ago	0.34	0.41	1.34	1.41
90 Days Ago	0.34	0.41	1.34	1.41

↑ Upgrade	Hilliard Lyons: Neutral to Long-term Buy	11/6/2012
↓ Downgrade	Hilliard Lyons: Long-term Buy to Neutral	7/18/2012
↓ Downgrade	Robert W. Baird: Outperform to Neutral	3/2/2012

More Upgrades & Downgrades

EPS Revisions	Current Qtr	Next Qtr.	Current Yea	Next Ye
Up Last 7 Days	N/A	N/A	N/A	N/A
Up Last 30 Days	N/A	N/A	N/A	N/A
Down Last 30 Days	N/A	N/A	N/A	N/A
Down Last 90 Days	N/A	N/A	N/A	N/A

Growth Estimates	WTR	Industry	Sector	S&P 500
Current Qtr.	6.30%	0.17		
Next Qtr.	7.90%	0.31		
Current Year	5.60%	0.00		
Next Year	6.00%	0.05		
Next 5 Years (per annum)	6.05%	0.09		
Past 5 Years (per annum)	11.23%	N/A		

Low Estimate	97.1M	128.2M	595M	630M
High Estimate	146M	187M	617M	721.2M
Year Ago Sales	144.41M	183.54M	588.37M	607.33M

1 Strong Buy	2 Buy	3 Hold	4 Under-perform	5 Sell

Analyst Price Targets (4) >

EPS Actual	0.21	0.52	0.18	-0.02
Difference	-0.1[illegible]	-0.1[illegible]	0.02	-0.05
Surprise %	-38.20[illegible]	[illegible]2.40[illegible]	-10.00%	-166.70%

	Barclays: Equal Weight	4/4/2016
Downgrade	Gabelli & Co: Buy to Hold	3/7/2016
Downgrade	Robert W. Baird: Outperform to Neutral	2/26/2016
Upgrade	Hilliard Lyons: Neutral to Buy	7/31/2015
Upgrade	Robert W. Baird: Neutral to Outperform	11/1/2013
Downgrade	Brean Capital: Buy to Hold	5/2/2013

More Upgrades & Downgrades

EPS Trend	Current Qtr.	Next Qtr.	Current Year	Next Year
Current Estimate	0.25	0.58	1.03	1.37
7 Days Ago	0.25	0.58	1.04	1.37
30 Days Ago	0.25	0.58	1.04	1.37
60 Days Ago	0.25	0.58	1.04	1.37
90 Days Ago	0.22	0.59	1.03	1.34

EPS Revisions	Current Qtr.	Next Qtr.	Current Year	Next Year
Up Last 7 Days	N/A	N/A	N/A	N/A
Up Last 30 Days	N/A	N/A	N/A	N/A
Down Last 30 Days	N/A	N/A	N/A	N/A
Down Last 90 Days	N/A	N/A	N/A	N/A

Growth Estimates	CWT	Industry	Sector	S&P 500
Current Qtr.	19.00%	0.17		
Next Qtr.	11.50%	0.31		
Current Year	9.60%	0.00		
Next Year	33.00%	0.05		
Next 5 Years (per annum)	9.05%	0.09		
Past 5 Years (per annum)	19.85%	N/A		

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Year Ago Sales	2M	1.44M	96.04M	100.1M
Sales Growth (year/est)	2.10%	2.20%	4.20%	7.70%

Low 47.00 High 47.00

Earnings History	6/29/2015	9/29/2015	12/30/2015	3/30/2016
EPS Est.	0.69	0.8	0.21	0.32
EPS Actual	0.77	0.79	0.2	0.28
Differenc	0.08	-0.01	-0.01	-0.04
Surprise %	11.60%	-1.30	-4.80	12.50

EPS Trend	Current Qtr.	Next Qtr.	Current Year	Next Year
Current Estimate	0.72	0.84	2.03	2.29
7 Days Ago	0.72	0.84	2.03	2.29
30 Days Ago	0.72	0.84	2.03	2.29
60 Days Ago	0.72	0.84	2.03	2.29
90 Days Ago	0.72	0.77	2.07	2.25

EPS Revisions	Current Qtr.	Next Qtr.	Current Year	Next Year
Up Last 7 Days	N/A	N/A	N/A	N/A
Up Last 30 Days	N/A	N/A	N/A	N/A
Down Last 30 Days	N/A	N/A	N/A	N/A
Down Last 90 Days	N/A	N/A	N/A	N/A

Growth Estimates	CTWS	Industry	Secto	S&P 500
Current Qtr.	-6.50%	0.17		
Next Qtr.	6.30%	0.31		
Current Year	-0.50%	0.00		
Next Year	12.80%	0.05		
Next 5 Years (per annum)	6.00%	0.09		
Past 5 Years (per annum)	6.05%	N/A		

Upgrades & Downgrades >

↓ Downgrade	Wells Fargo: Outperform to Market Perform	2/1/2016
↑ Upgrade	Wells Fargo: Market Perform to Outperform	5/15/2015
↑ Upgrade	Robert W. Baird: Neutral to Outperform	8/13/2013
↑ Upgrade	Boenning & Scattergood: Neutral to Outperform	8/13/2013
↑ Upgrade	Ladenburg Thalmann: Neutral to Buy	11/13/2012
↓ Downgrade	Janney Mntgmy Scott: Buy to Neutral	11/10/2008

More Upgrades & Downgrades

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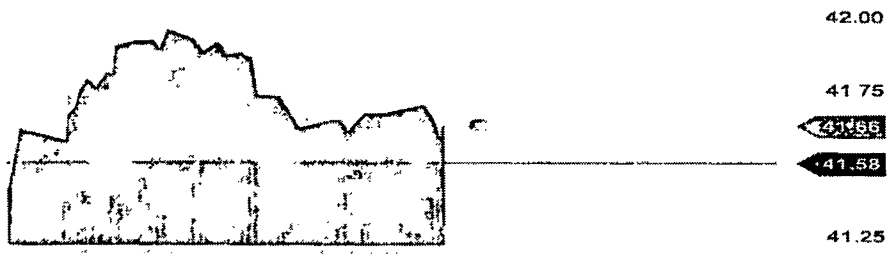
S&P 500	Dow 30	Nasdaq
2,165.14	18,520.96	5,053.34
3.40 (0.16%)	4.41 (0.02%)	23.75 (0.47%)

MSEX Middlesex Water Co. NasdaqGS ☆ Add to watchlist

People also watch: CTWS SJW ARTNA YORW CWT

41.69 0.11 (0.26%)

1D 5D 1M 6M YTD 1Y Interactive chart



Prev Close	41.58	52wk Range	22.12 - 44.11
Open	41.43	Day's Range	41.43 - 41.99
Bid	41.58 x 200	Volume	22,122
Ask	41.67 x 100	Avg Vol (3m)	94,561

As of 1:22 PM EDT. NasdaqGS Real Time Price. Market open

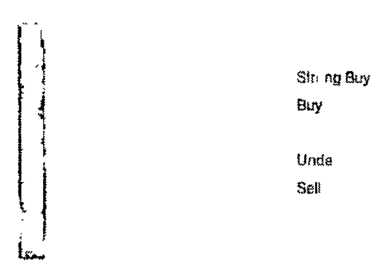
Summary | Conversations | Statistics | Profile | Financials | Options | Holders

Historical Data | Analysts | Curre cy in USD.

Key Statistics >

Market Cap	677.11M
P/E Ratio (ttm)	32.27
Diluted EPS	1.29
Beta	0.53
Earnings Date	Aug 1, 2016 - Aug 5, 2016
Dividend & Yield	0.80 (1.91%)
Ex-Dividend Date	May 11, 2016

Recommendation Trends >



Recommendation Rating >

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Low 31.00 High 31.00

Upgrades & Downgrades >

↑ Upgrade	Janney Mntgmy Scott: Neutral to Buy	5/7/2008
↑ Upgrade	Boenning & Scattergood: Market Perform to Market Outperform	11/8/2007
↓ Downgrade	Janney Mntgmy Scott: Buy to Neutral	8/8/2007
	Boenning & Scattergood: Market Perform	11/7/2006
	Janney Mntgmy Scott: Buy	8/25/1999

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Year Ago Sales	4M	.95M	,06M	304M
Sales Growth (year/est)	3.60%	4.90%	0 40[illegible]	1.50%

Low 35.00 High 35.00

Earnings History	6/29/2015	9/29/2015	12/30/2015	3/30/2016
EPS Est.	0.42	0.57	0.29	0.21
EPS Actual	0.36	0.46	0.79	0.16
Difference	-0.06	-0 1[illegible]	0.5	0.0[illegible]
Surprise %	-14.30%	-19 30[illegible]	172.40%	[illegible]3.80[illegible]

EPS Trend	Current Qtr.	Next Qtr.	Current Year	Next Ye
Current Estimate	0.41	0.58	1.57	1.74
7 Days Ago	0.41	0.58	1.57	1.74
30 Days Ago	0.41	0.58	1.57	1.74
60 Days Ago	0.41	0.58	1.57	1.74
90 Days Ago	0.41	0.58	1.74	1.85

EPS Revisions	Current Qtr	Next Qtr.	Current Year	Next Year
Up Last 7 Days	N/A	N/A	N/A	N/A
Up Last 30 Days	N/A	N/A	N/A	N/A
Down Last 30 Days	N/A	N/A	N/A	N/A
Down Last 90 Days	N/A	N/A	N/A	N/A

Growth Estimates	SJW	Industry	Secto	S&P 500
Current Qtr.	13.90%	0.17		
Next Qtr.	26.10%	0.31		
Current Year	-15.10%	0.00		
Next Year	10.80%	0.05		
Next 5 Years (per annum)	14.00%	0.09		
Past 5 Years (per annum)	25.42%	N/A		

Upgrades & Downgrades >

↑ Upgrade	Robert W. Baird: Neutral to Outperform	2/22/2016
↑ Upgrade	Robert W. Baird: Neutral to Outperform	7/16/2014
↓ Downgrade	Brean Capital: Buy to Hold	8/2/2013
↑ Upgrade	Brean Murray: Hold to Buy	2/23/2012
	Ladenburg Thalmann: Buy	6/9/2011
↑ Upgrade	Brean Murray: Sell to Hold	2/24/2011

More Upgrades & Downgrades

Ago Sales		M	.09M	47.55M
Sales Growth (year/est)	1.60%	0.80%	1.60%	5.10%

Low 25.50 High 25.50

Earnings History	6/29/2015	9/29/2015	12/30/2015	3/30/2016
EPS Est.	0.25	0.26	0.23	0.2
EPS Actual	0.22	0.28	0.27	0.19
Difference	-0.03	0.02	0.04	-0.01
Surprise %	-12.00%	7.70%	17.40%	-5.00%

EPS Trend	Current Qtr.	Next Qtr.	Current Yea	Next Year
Current Estimate	0.23	0.29	0.97	1.05
7 Days Ago	0.23	0.29	0.97	1.05
30 Days Ago	0.23	0.29	0.97	1.05
60 Days Ago	0.23	0.29	0.97	1.05
90 Days Ago	0.23	0.29	1.01	1.08

EPS Revisions	Current Qtr.	Next Qtr.	Cu nt Year	Next Year
Up Last 7 Days	N/A	N/A	N/A	N/A
Up Last 30 Days	N/A	N/A	N/A	N/A
Down Last 30 Days	N/A	N/A	N/A	N/A
Down Last 90 Days	N/A	N/A	N/A	N/A

Growth Estimates	YORW	Industry	Secto	S&P 500
Current Qtr.	4.50%	0.17		
Next Qtr.	3.60%	0.31		
Current Year	N/A	0.00		
Next Year	8.20%	0.05		
Next 5 Years (per annum)	4.90%	0.09		
Past 5 Years (per annum)	7.90%	N/A		

Upgrades & Downgrades >

↑ Upgrade	Boenning & Scattergood: Neutral to Outperform	2/3/2015
	Boenning & Scattergood: Neutral	10/13/2011
↑ Upgrade	Brean Murray: Hold to Buy	3/9/2011
↓ Downgrade	Brean Murray: Buy to Hold	12/10/2010
	Brean Murray: Buy	4/27/2009
↑ Upgrade	Janney Mntgmy Scott: Neutral to Buy	7/25/2008

More Upgrades & Downgrades

DJIA 18514.49 8.08(0.04%) Gold 1335.00 8.50(0.64%) Light Crude 45.03 -0.92(-2.00%)

American States Water Co AWR

Annual Earnings Estimates AWR

	12/2016		12/2017	
	USD	Growth %	USD	Growth %
High	1.70	6.3	1.80	5.9
Low	1.70	6.3	1.80	5.9
Mean	1.70	6.3	1.80	5.9
Median	1.70	6.3	1.80	5.9
30 Days Ago	1.70	6.3	1.80	5.9
60 Days Ago	1.70	6.3	1.80	5.9
90 Days Ago	—	—	—	—
Number of Estimates		1		1

Analyst Ratings AWR

Five-Year Growth Forecast	Industry Avg
—	—

Average Rating	Last Month	Industry Avg	S&P 500 Avg
3.0	—	—	—

Total Number of Analysts:

Buy	0
Outperform	0
Hold	1
Underperform	0
Sell	0

Forward Comparisons AWR

	5Y Growth Forecast %	Forward P/E	PEG Ratio
AWR	—	25.5	—
Industry	—	—	—
S&P 500	8.8	18.4	—

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DJIA 18514.49 8.08(0.04%) Gold 1335.00 8.50(0.64%) Light Crude 45.03 -0.92(-2 00%)

American Water Works Co Inc AWK

Quote Chart Stock Analysis Performar Key Ratio Financials **Valuation** Insiders Ownership Filings Bonds

Valuation Wall Street Estimates

Annual Earnings Estimates AWK

	12/2016		12/2017	
	USD	Growth %	USD	Growth %
High	2.86	8.3	3.23	12.9
Low	2.75	4.2	2.95	7.3
Mean	2.83	7.2	3.08	8.8
Media	2.84	7.6	3.10	9.2
30 Days Agc	2.80	6.1	3.02	7.9
60 Days Agc	2.80	6.1	2.95	5.4
90 Days Agc	—	—	—	—
Numbe of Estimate		3		1

Analyst Ratings AWK

Five-Year Growth Forecast		Industry Avg	
6.5%		—	
Average Rating	**Last Month**	**Industry Avg**	**S&P 500 Avg**
3.8	—	—	—

Total Numbe of Analysts:

Buy	3
Outperform	0
Hold	1
Underperform	0
Sell	1

Forward Comparisons AWK

	5Y Growth Fcst %	Forward P/E	PEG Ratio
AWK	6.5	28.7	4.4
Industry	—	—	—
S&P 500	8.8	18.4	—

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Membership Home Portfolio Stocks Bonds Funds ETFs CEF Markets Tools Real Life Finance Discuss

18514.49 8.68(0.04%) DJIA | 1335.00 8.50(0.64%) Gold | 45.03 -0.92(-2 00%) Light Crude

Aqua America Inc WTR

Print

Quote Chart Stock Analysis Performance Key Ratios Financials **Valuation** Insiders Ownership Filings Bonds

Wall Str at Estimate

Annual Earnings Estimates WTR

	12/2016		12/2017	
	USD	Growth %	USD	Growth %
High	1.35	18.4	1.45	7.4
Low	1.34	17.5	1.38	3.0
Mean	1.35	18.4	1.42	5.2
Median	1.35	18.4	1.42	5.2
30 Days Ago	1.35	18.4	1.42	5.2
60 Days Ago	1.35	18.4	1.42	5.2
90 Days Ago	—	—	—	—
Number of Estimates		3		3

Analyst Ratings WTR

Five-Year Growth Forecast	Industry Avg
—	—

Average Rating	Last Month	Industry Avg	S&P 500 Avg
4.3	—	—	—

Total Number of Analysts

Buy	2
Outperform	0
Hold	1
Underperform	0
Sell	0

Forward Comparisons WTR

	5Y Growth Forecast %	Forward P/E	PEG Ratio
WTR	—	25.2	—
Industry	—	—	—
S&P 500	8.8	18.4	—

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Welcome! Log In Premium Company Site Company News

Membership Home Portfolio Stocks Bonds Funds ETFs CEF Markets Tools Real Life Fin nce Discuss

DJIA 18514.49 8.08(0.04%) Gold 1335.00 8.50(0.64%) Light Crude 45.03 -0.92(-2.00%)

California Water Service Group CWT

Quote Chart Stock Analysis Performance Key Ratios Financials **Valuation** Insiders Ownership Filings Bonds

V luati **Wall Str et Estimates**

Annual Earnings Estimates CWT

	12/2016		12/2017	
	USD	Growth %	USD	Growth %
High	1.15	22.3	1.35	17.4
Low	1.15	22.3	1.35	17.4
Me	1.15	22.3	1.35	17.4
Median	1.15	22.3	1.35	17.4
30 Days Ago	1.15	22.3	1.35	17.4
60 Days Ago	1.15	22.3	1.35	17.4
90 Days Ago	—	—	—	—
Numbe of Estimates		1		1

Analyst Ratings WT

Five-Ye Growth Forecast		Industry Avg	
—		—	
Average Rating	**Last Month**	**Industry Avg**	**S&P 500 Avg**
3.0	—	—	—

Total Numbe of Analysts:

Buy	0
Outperform	0
Hold	1
Underperform	0
Sell	0

Forward Comparisons CWT

	5Y Growth Fc st %	Forward P/E	PEG Ratio
CWT	—	28.7	—
Industry	—	—	—
S&P 500	8.8	18.4	—

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Membership Home Portfolio Stocks Bonds Funds ETFs CEF Markets Tools Real Life Finance Discuss

DJIA	Gold	Light Crude
18514.49 8.08(0.04%)	1335.00 8.50(0.64%)	45.03 -0.92(00%)

Connecticut Water Service Inc CTWS

Quote Chart Stock Analysis Performance Key Ratios Financials **Valuation** Insiders Ownership Filings Bonds

Wall Str at Estimates

Annual Earnings Estimates CTWS

		Growth %		Growth %
High				
Low				
Mear				
Median				
30 Days Agc				
60 Days Ago				
90 Days Ago				
Numbe of Estimates				

Analyst Ratings CTWS

Five-Ye Growth Fc ast		Industry Avg	
—		—	
Average Rating	**Last Month**	**Industry Avg**	**S&P 500 Avg**
—	—	—	—

Total Numbe of Analysts	
Buy	—
Outperform	—
Hold	
Underperform	
Sell	—

Forward Comparisons CTWS

	5Y Growth Fo st %	Forward P/E	PEG Ratio
CTWS	—	—	—
Industry	—	—	
S&P 500	8.8	18.4	—

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Membership Home Portfolio Stocks Bonds Funds ETFs CEF Markets Tools Real Life Finance Discuss

DJIA 18514.49 8.08(0.04%) Gold 1335.00 8.50(0.64%) Light Crude 45.03 0.92(- 00%)

Middlesex Water Co MSEX

Quote Chart Stock Analysis Performance Key Ratic Fir cials **Valuation** Insiders Ownership Filings Bonds

Valuati **Wall Street Estimates**

Annual Earnings Estimates MSEX

	Growth %	Growth %
High		
Low		
Mear		
Median		
30 Days Agc		
60 Days Ago		
90 Days Ago		
Numbe of Estimates		

Analyst Ratings MSEX

Five-Ye · Growth Forecast		Industry Avg	
—		—	
Average Rating	**Last Month**	**Industry Avg**	**S&P 500 Avg**
—	—	—	—

Total Numbe of Analysts:

Buy	—
Outperform	—
Hold	
Underperform	—
Sell	—

Forward Comparisons MSE

	5Y Growth Fc st %	Forward P/E	PEG Ratio
MSEX	—	—	—
Industry	—	—	—
S&P 500	8.8	18.4	—

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Welcome!

Membership Home Portfolio Stocks Bonds Funds ETFs CEF Markets Tools Real Life Finance Discuss

DJIA	Gold	Light Crude
18514.49 8.08(0.04%)	1335.00 8.50(0.64%)	45.03 -0 92(-2 00%)

21,078% ... Amazon ...What's

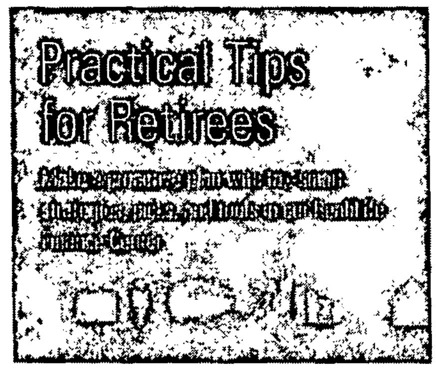
SJW Corp SJW

Quote Chart Stock Analysis Performance Key Ratios Financials **Valuation** Insiders Ownership Filings Bonds

Valuation **Wall Street Estimates**

Annual Earnings Estimates SJW

	Growth %	Growth %
High		
Low		
Me		
Media		
30 Days Ago		
60 Days Ago		
90 Days Ago		
Number of Estimates		



AD Read This Before the Retirement Crisis

Analyst Ratings SJW

Five-Year Growth Forecast		Industry Avg	
—		—	
Average Rating	**Last Month**	**Industry Avg**	**S&P 500 Avg**
—	—	—	—

Total Number of Analysts:

Buy	—
Outperform	—
Hold	—
Underperform	—
Sell	—

Forward Comparisons SJW

	5Y Growth Forecast %	Forward P/E	PEG Ratio
SJW	—	—	—
Industry		—	—
S&P 500	8.8	18.4	—

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Membership Home Portfolio Stocks Bonds Funds ETFs CEF Markets Tools Real Life Finance Discuss

DJIA 18514.49 8.08(0.04%) Gold 1335.00 8.50(0.64%) Light Crude 45.03 -0.92(- .00%)

York Water Co YORW

Quote Chart Stock Analysis Performance Key Ratio Financials **Valuation** Insiders Ownership Filings Bonds

Wall Street Estimates

Annual Earnings Estimates YORW

	Growth	Growth %
High		
Low		
Me		
Median		
30 Days Ago		
60 Days Ago		
90 Days Ago		
Number of Estimates		

Analyst Ratings ORW

Five-Ye Growth Fo ast		Industry Avg	
—		—	
Average Rating	**Last Month**	**Industry Avg**	**S&P 500 Avg**
—	—	—	—

Total Number of Analysts:

Buy	
Outperform	—
Hold	—
Underperform	—
Sell	

Forward Comparisons YORW

	5Y Growth Forecast %	Forward P/E	PEG Ratio
YORW	—	—	—
Industry	—	—	—
S&P 500	8.8	18.4	—

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Quote or Search

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Amer States Wtr: (AWR)

(Real Time Quote From BATS)

$43.15 USD

-0.27 (-0.62%)

Updated Jul 18, 2016 01:16 PM ET

Volume:	24,087	Zacks Rank [?]:	3-Hold
Open:	$43.46	Style Scores [?]:	Value: D | Growth: D | Momentum: D | VGM:
Prior Close:	$43.42		

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DETAILED ESTIMATES

Amer States Wtr (AWR) Quote Overview » Estimates » Amer States Wtr (AWR) Detailed Estimates

Detailed Estimates

Enter Symbol

Estimates

Next Report Date	8/2/16	Current Year	1.66
Current Quarter	0.47	Next Year	1.72
Earnings ESP [?]	0.00%	EPS(TTM)	1.57
EPS Last Quarter	0.47	P/E (F1)	26.09
Last EPS Surprise	-17.65%	ABR	3.67

Growth Estimates	AWR	IND	S&P
Current Qtr (06/2016)	14.63	NA	NA
Next Qtr (09/2016)	-2.63	NA	NA
Current Year (12/2016)	3.40	6.70	18.00
Next Year (12/2017)	3.60	18.90	8.50
Past 5 Years	10.30	3.30	4.90
Next 5 Years	3.80	11.60	NA
PE	26.09	29.30	18.20
PEG Ratio	6.78	2.53	NA

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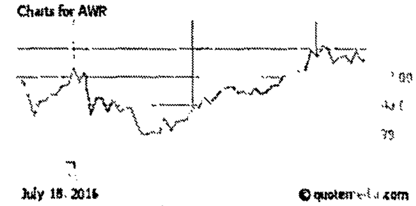
Research Reports for AWR [?]:

Chart for AWR



Interactive Chart | Fundamental Charts

Premium Research for AWR

Zacks Rank [?]	Hold
Zacks Industry Rank [?]	64 / 265 (Top 24%)
Style Scores [?]	

Value: D | Growth: D | Momentum: D | VGM:

Research Reports for AWR [?]: Analyst | Snapshot

(Change in last 30 days)

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	Tuesday	In 1 Week	In 1 Month	In 3 Months
AWR Amer States				

Sales Estimates

Current Qtr	Next Qtr	Current Year	Next Year

0000030

Quote or Search

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Amer Water Work: (AWK)

(Real Time Quote From BATS)

$81.49 USD	Volume:	534,383	Zacks Rank [?]:	2-Buy	
-0.10 (-0.12%)	Open:	$81.60	Style Scores [?]:	Value: D | Growth: B | Momentum: A | VGM:	
Updated Jul 18, 2016 01:16 PM ET	Prior Close:	$81.59		View All Zacks Rank #1 Strong Buys	

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DETAILED ESTIMATES

Amer Water Work (AWK) Quote Overview › Estimates › Amer Water Work (AWK) Detailed Estimates

Detailed Estimates

Enter Symbol

Estimates

Next Report Date	8/3/16	Current Year	2.83
Current Quarter	0.72	Next Year	3.03
Earnings ESP [?]	5.56%	EPS(TTM)	2.65
EPS Last Quarter	0.72	P/E (F1)	28.86
Last EPS Surprise	0.00%	ABR	2.25

Growth Estimates	AWK	IND	S&P
Current Qtr (06/2016)	6.13	NA	NA
Next Qtr (09/2016)	6.46	NA	NA
Current Year (12/2016)	7.10	6.70	18.00
Next Year (12/2017)	7.30	16.90	8.50
Past 5 Years	11.70	3.30	4.90
Next 5 Years	7.20	11.60	NA
PE	28.86	29.30	18.20
PEG Ratio	4.01	2.53	NA

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Research Reports for AWK [?]:

Chart for AWK

Charts for AWK

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Premium Research for AWK

Zacks Rank [?]	▲ Buy
Zacks Industry Rank [?]	64 / 265 (Top 24%)
Style Scores [?]	
Value: D | Growth: B | Momentum: A | VGM:	
Research Reports for AWK [?]:	Analyst | Snapshot

(Change in last 30 days)

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	Tuesday	In 1 Week	In 1 Month	In 3 Months
AWK America Water				

Sales Estimates

	Current Qtr	Next Qtr	Current Year	Next Year

Quote or Search

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Aqua Amer Inc: (WTR)

(Real Time Quote From BATS)

$34.04 USD

+0.01 (0.03%)

Updated Jul 18, 2016 01:16 PM ET

Add to portfolio

Volume:	197,690	Zacks Rank [?]:	4-Sell
Open:	$34.03	Style Scores [?]:	Value: F | Growth: B | Momentum: A | VGM:
Prior Close:	$34.03		View All Zacks Rank #1 Strong Buys

DETAILED ESTIMATES

Aqua Amer Inc (WTR) Quote Overview » Estimates » Aqua Amer Inc (WTR) Detailed Estimates

Detailed Estimates

Enter Symbol

Estimates

Next Report Date	*AMC8/2/16	Current Year	1.33
Current Quarter	0.33	Next Year	1.41
Earnings ESP [?]	0.00%	EPS(TTM)	1.27
EPS Last Quarter	0.33	P/E (F1)	25.50
Last EPS Surprise	3.57%	ABR	2.56

*BMO = Before Market Open *AMC = After Market Close

Growth Estimates	WTR	IND	S&P
Current Qtr (06/2016)	3.13	NA	NA
Next Qtr (09/2016)	9.21	NA	NA
Current Year (12/2016)	5.90	6.70	18.00
Next Year (12/2017)	5.80	18.90	8.50
Past 5 Years	12.50	3.30	4.90
Next 5 Years	6.30	11.60	NA
PE	25.50	29.30	18.20
PEG Ratio	4.03	2.53	NA

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Research Reports for WTR [?]:

Chart for WTR

Charts for WTR

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Premium Research for WTR

Zacks Rank [?]	▼ Sell
Zacks Industry Rank [?]	64 / 265 (Top 24%)
Style Scores [?]	
	Value: F | Growth: B | Momentum: A | VGM:
Research Reports for WTR [?]:	Analyst | Snapshot

(: Change in last 30 days)

View All Zacks Rank #1 Strong Buys

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	Today	In 1 Week	In 1 Month	In 3 Months
WTR Aqua America, I				

Sales Estimates

0000032

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Calif Water Svc: (CWT)

(Real Time Quote From BATS)

$32.76 USD

-0.25 (-0.76%)

Updated Jul 18, 2016 01:16 PM ET

Volume:	66,588	Zacks Rank [?]:	2-Buy
Open:	$32.91	Style Scores [?]:	Value: D | Growth: C | Momentum: B | VGM:
Prior Close:	$33.01		View All Zacks Rank #1 Strong Buys

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DETAILED ESTIMATES

Calif Water Svc (CWT) Quote Overview » Estimates » Calif Water Svc (CWT) Detailed Estimates

Detailed Estimates

Enter Symbol

Research Report for CWT [?]:

Estimates

Next Report Date	*BMO 7/28/16	Current Year	1.04
Current Quarter	0.27	Next Year	1.37
Earnings ESP [?]	0.00%	EPS(TTM)	0.89
EPS Last Quarter	0.27	P/E (F1)	31.80
Last EPS Surprise	-166.67%	ABR	3.00

*BMO = Before Market Open *AMC = After Market Close

Growth Estimates	CWT	IND	S&P
Current Qtr (06/2016)	28.57	NA	NA
Next Qtr (09/2016)	10.58	NA	NA
Current Year (12/2016)	10.40	6.70	18.00
Next Year (12/2017)	32.40	18.90	8.50
Past 5 Years	0.90	3.30	4.90
Next 5 Years	9.10	11.60	NA
PE	31.80	29.30	18.20
PEG Ratio	3.51	2.53	NA

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See Earnings Report Transcript

Chart for CWT

Charts for CWT

July 18, 2016 © quotemedia.com

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	Tuesday	In 1 Week	In 1 Month	In 3 Months
CWT California Wate				

Premium Research for CWT

Zacks Rank [?]	▲ Buy
Zacks Industry Rank [?]	64 / 265 (Top 24%)
Style Scores [?]	
	Value: D | Growth: C | Momentum: B | VGM:
Research Report for CWT [?]:	Snapshot

(= Change in last 30 days)

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Sales Estimates

0000033

Quote or Search

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Conn Water Svc: (CTWS)

(Real Time Quote From BATS)

$51.72 USD

-0.26 (-0.50%)

Updated Jul 18, 2016 01:16 PM ET

Volume:	13,549	Zacks Rank [?]:	2-Buy
Open:	$51.94	Style Scores [?]:	Value: D | Growth: F | Momentum: D | VGM:
Pri Clo	$51.98		View All Zacks Rank #1 Strong Buys

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DETAILED ESTIMATES

Conn Water Svc (CTWS) Quote Overview » Estimates » Conn Water Svc (CTWS) Detailed Estimates

Detailed Estimates

Enter Symbol

Estimates

Next Report Date	8/5/16	Current Year	2.03
Current Quarter	0.70	Next Year	2.29
Earnings ESP [?]	0.00%	EPS(TTM)	2.04
EPS Last Quarter	0.70	P/E (F1)	25.61
Last EPS Surprise	-6.67%	ABR	3.00

Growth Estimates	CTWS	IND	S&P
Current Qtr (06/2016)	-9.09	NA	NA
Next Qtr (09/2016)	7.59	NA	NA
Current Year (12/2016)	-0.50	6.70	18.00
Next Year (12/2017)	12.80	18.90	8.50
Past 5 Years	11.10	3.30	4.90
Next 5 Years	6.00	11.60	NA
PE	25.61	29.30	18.20
PEG Ratio	4.27	2.53	NA

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Research Reports for CTWS [?]:

Chart for CTWS

Charts for CTWS

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Interactive Chart | Fundamental Charts

Premium Research for CTWS

Zacks Rank [?]	▲ Buy
Zacks Industry Rank [?]	64 / 265 (Top 24%)
Style Scores [?]	
	Value: D | Growth: F | Momentum: D | VGM:
Research Reports for CTWS [?]:	Analyst | Snapshot

(= Change in last 30 days)

View All Zacks Rank #1 Strong Buys

Learn to Profit from the Zacks Rank

More Premium Research »

	Tuesday	In 1 Week	In 1 Month	In 3 Months
CTWS Connecticut Wat..				

Sales Estimates

	Current Qtr (ND)	Next Qtr (ND)	Current Year (12/2016)	Next Year (12/2017)

0000034

Quote or Search

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Middlesex Water: (MSEX)

(Real Time Quote From BATS)

Add to portfolio

$41.66 USD

+0.08 (0.19%)

Updated Jul 18, 2016 01:16 PM ET

Volume	19,879	Zacks Rank [?]:	
Open:	$41.43	Style Scores [?]:	Value: NA | Growth: NA | Momentum: NA | VGM: NA
Prior Close	$41.58		View All Zacks Rank #1 Strong Buys

DETAILED ESTIMATES

Middlesex Water (MSEX) Quote Overview » Estimates » Middlesex Water (MSEX) Detailed Estimates

Detailed Estimates

Enter Symbol

Estimates

Next Report Date	8/1/16	Current Year	NA
Current Quarter	NA	Next Year	NA
Earnings ESP [?]	0.00%	EPS(TTM)	1.29
EPS Last Quarter	NA	P/E (F1)	NA
Last EPS Surprise	NA	ABR	NA

Growth Estimates	MSEX	IND	S&P
Current Qtr (06/2016)	NA	NA	NA
Next Qtr (09/2016)	NA	NA	NA
Current Year (12/2016)	NA	6.70	18.00
Next Year (12/2017)	NA	18.90	8.50
Past 5 Years	NA	3.30	4.90
Next 5 Years	NA	11.60	NA
PE	NA	29.30	18.20
PEG Ratio	NA	2.53	NA

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Chart for MSEX

Charts for MSEX

July 18, 2016 © quotemedia.com

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Premium Research for MSEX

Zacks Rank [?]	NA
Zacks Industry Rank [?]	64 / 265 (Top 24%)
Style Scores [?]	

Value: NA | Growth: NA | Momentum: NA | VGM: NA

Research Report for MSEX [?]: Snapshot

(= Change in last 30 days)

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Learn to Profit from the Zacks Rank

More Premium Research »

	Today	In 1 Week	In 1 Month	In 3 Months
MSEX Middlesex Water				

Sales Estimates

Current Qtr (ND)	Next Qtr (ND)	Current Year (ND)	Next Year (ND)

0000035

Quote or Search

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Sjw Corp: (SJW)

(Real Time Quote From BATS)

$38.80 USD

-0.54 (-1.37%)

Updated Jul 18, 2016 01:18 PM ET

Volume	13,302	Zacks Rank [?]:	3-Hold
Open:	$39.37	Style Scores [?]:	Value B | Growth: B | Momentum: F | VGM:
Prior Close:	$39.34		View All Zacks Rank #1 Strong Buys

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DETAILED ESTIMATES

Sjw Corp (SJW) Quote Overview » Estimates » Sjw Corp (SJW) Detailed Estimates

Detailed Estimates

Enter Symbol

Research Report for SJW [?]:

Estimates

Next Report Date	*AMC7/27/16	Current Year	1.57
Current Quarter	0.41	Next Year	1.74
Earnings ESP [?]	0.00%	EPS(TTM)	1.77
EPS Last Quarter	0.41	P/E (F1)	25.06
Last EPS Surprise	-23.81%	ABR	3.00

*BMO = Before Market Open *AMC = After Market Close

Growth Estimates	SJW	IND	S&P
Current Qtr (06/2016)	13.89	NA	NA
Next Qtr (09/2016)	26.09	NA	NA
Current Year (12/2016)	-15.10	6.70	18.00
Next Year (12/2017)	10.80	18.90	8.50
Past 5 Years	16.50	3.30	4.90
Next 5 Years	NA	11.60	NA
PE	25.06	29.30	18.20
PEG Ratio	NA	2.53	NA

Learn More About Estimate Research

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See Earnings Report Transcript

Chart for SJW

Interactive Chart | Fundamental Charts

SJW Sjw Corporation	Tuesday	In 1 Week	In 1 Month	In 3 Months

Premium Research for SJW

Zacks Rank [?]	▲ Hold
Zacks Industry Rank [?]	64 / 265 (Top 24%)
Style Scores [?]	

Value: B | Growth: B | Momentum: F | VGM:

Research Report for SJW [?]: Snapshot

(Change in last 30 days)

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Sales Estimates

York Water Co: (YORW)

(Real Time Quote From BATS)

$31.26 USD

0.00 (0.00%)

Updated Jul 18, 2016 01:18 PM ET

Volume	21,605	Zacks Rank [?]:	3-Hold
Open:	$31.28	Style Scores [?]:	Value: F | Growth: C | Momentum: D | VGM:
Prior Close:	$31.26		

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DETAILED ESTIMATES

York Water Co (YORW) Quote Overview : Estimates : York Water Co (YORW) Detailed Estimates

Detailed Estimates

Enter Symbol

Estimates

Next Report Date	8/4/16	Current Year	0.97
Current Quarter	NA	Next Year	1.05
Earnings ESP [?]	0.00%	EPS(TTM)	0.96
EPS Last Quarter	0.26	P/E (F1)	32.23
Last EPS Surprise	3.85%	ABR	5.00

Growth Estimates	YORW	IND	S&P
Current Qtr (06/2016)	NA	NA	NA
Next Qtr (09/2016)	NA	NA	NA
Current Year (12/2016)	0.00	6.70	18.00
Next Year (12/2017)	8.20	18.90	8.50
Past 5 Years	7.10	3.30	4.90
Next 5 Years	NA	11.60	NA
PE	32.23	29.30	18.20
PEG Ratio	NA	2.53	NA

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Research Report for YORW [?]:

Chart for YORW

Charts for YORW

July 18 2016 © quote om

Interactive Chart | Fundamental Charts

Premium Research for YORW

Zacks Rank [?]	Hold
Zacks Industry Rank [?]	64 / 265 (Top 24%)
Style Scores [?]	

Value: F | Growth: C | Momentum: D | VGM:

Research Report for YORW [?]: Snapshot

(= Change in last 30 days)

View All Zacks Rank #1 Strong Buys

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More Premium Research :

Tuesday In 1 Week In 1 Month In 3 Months

YORW
The York Wate

Sales Estimates

Current Qtr (ND)	Next Qtr (ND)	Current Year (ND)	Next Year (ND)

0000037

A Note on the Relationship between Firm Size and Return in the Electric Utility Industry

Wallace Davidson III, Kenneth Ferris III and William Reichenstein III
Journal of Accounting, Auditing & Finance 1993 8: 193
DOI: 10.1177/0148558X9300800301

A Note on the Relationship Between Firm Size and Return in the Electric Utility Industry

WALLACE DAVIDSON, III*
KENNETH FERRIS**
WILLIAM REICHENSTEIN***

Prior research has argued that given the well-documented inverse relationship between firm size and market returns, smaller utilities should be allowed to earn higher accounting rates of return than larger utilities. To test the validity of this argument, this study investigated the relationship between firm size and market returns in the electric utility industry for the period 1962 through 1985 and found no evidence of either a positive or negative size effect. Moreover, although market returns on utility stocks were found to be higher in January than in non-January months, this January effect was found to be unrelated to firm size. In short, this study found no evidence that allowable accounting rates of return should be adjusted by regulatory authorities to reflect a firm's size.

1. Introduction

The accounting rate of return (ARR) earned by firms operating in a regulated environment is generally established by regulatory authorities on the basis of measures produced under regulatory accounting principles. In some cases, the allowable ARR is based on the level of invested assets (e.g. ROA or ROE), whereas in others it is set as a percentage of costs incurred (e.g. cost plus X percent). In all cases, however, the allowable ARR is relatively unaffected by the size of the regulated firm in that standardized indices are used.[1]

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This paper has benefited from the constructive comments of an anonymous reviewer. All errors remain the responsibility of the authors.

1. Size arguments are frequently made in the context of rate determination hearings; hence, although size may be implicitly considered by regulatory authorities in establishing the allowable rate base, it is normally not an explicit consideration in the rate determination process.

Bolton and Besley [6] argue, however, that given the consistent higher market returns earned by small firms' stocks, a utility's cost of capital and therefore its allowable ARR should reflect its size. That is, smaller utilities should be allowed to earn a higher ARR than larger utilities.

Although there is substantial empirical support for the existence of a size effect [1,2,3,8,9,11,14,16,20,21,25, among others],[2] the presence of this stock market anomaly is not well documented in the utility industry, and what evidence there is suggests that there may be a *large* firm utility effect. Moreover, Schwert [24] questions the appropriateness of adjusting a firm's cost of capital, and by extension the allowable ARR, for the size effect.

Thus, this paper investigates the long-run relationship between firm size and market return for electric utility stocks. If regulatory authorities are to consider the adjustment of allowable ARR by firm size, then the existence of a size effect in the utility industry must first be clearly demonstrated.

2. Investigation

For purposes of this study, we assume the capital markets to be informationally efficient in a semistrong form. Thus, in spite of the presence of artificially controlled ARRs, risk and market return differentials may emerge in response to perceived variability in earnings and cash flows associated with firm size [7,11,12,22,23].

Prior research involving utilities has observed a *positive* relation between a utility's size and market return. For the period 1967–1972, Melicher [18] found a positive relationship between ex post beta and the log of total assets. Similarly, Reichenstein and Davidson [19] observed a significant positive relation between the market value of utilities' common stock and ex ante measures of stock price premiums for the period 1986–1987. Thus, contrary to the findings of the industrial-based size literature, available evidence involving utilities suggests the presence of a positive size effect.

2.1 Sample

The sample for the current study consists of all electric utilities listed on the Center for Research in Security Prices (daily) tapes for pairs of consecutive years, with not more than 10 days of missing data in either year. The only firms eliminated by this restriction are those whose stock was delisted during a two-year period. The study period is 1962 through

2. Recent evidence [12,13] suggests that the size effect may be smaller than previously thought.

1985; however, because one additional year is needed to generate market model parameters, results are reported for only 1963–1985. The sample varies by year from 90 to 103 firms.

2.2 Analysis

At the end of each year ($t - 1$), the market value of equity for each firm was computed and then used to assign the firm to one of four portfolios based on a ranking of relative market value. Firms assigned to MV_1 represent the lowest quartile of relative market value for a given year, whereas those assigned to MV_4 represent the highest quartile of relative market value. Using parameter estimates obtained for year $t - 1$, daily abnormal returns were computed for year t. These returns were then summed for each company to yield a cumulative abnormal return (CAR_t), and grouped by firm size to produce a portfolio CAR. Cumulative abnormal returns for each of the four equally weighted portfolios were calculated using two separate return-generating models. The first model was the market model, with parameter estimates for year $t - 1$ obtained by regressing daily returns against the returns on the value-weighted market index. The second model was the aggregate beta model proposed by Dimson [13] to minimize measurement problems associated with infrequently traded stocks. The results for the aggregate beta model are not specifically discussed here in that it yielded qualitatively similar results and supported similar conclusions to those of the market model.[3]

3. Empirical Results

3.1 Annual Results

Table 1 summarizes the average annual abnormal returns for the four portfolios generated by the market model. The average CARs do not differ significantly over the investigated period 1963 to 1985 ($F_{3,15} = 0.0394$). The range of values is small (i.e. -0.0474 [MV_3] to -0.0290 [MV_4]), and they neither increase nor decrease monotonically with size. In short, the data provide no evidence of *either* a negative or a positive annual size effect.

Moreover, Table 2 shows the distributions of average raw returns and average betas across the four portfolios. Neither raw returns nor betas

3. The Dimson model [13] is appropriate when stocks trade infrequently, which is primarily a small firm phenomenon. We reach the same conclusions with the market model and the Dimson aggregate beta model. The results for the aggregate beta model are presented in Table 1, but are not discussed.

TABLE 1

Tests for an Annual Firm Size Effect

Average Annual Abnormal Returns	MV_1	MV_2	MV_3	MV_4
Market Model F_3 = 0.0394	−0.0313	−0.0343	−0.0474	−0.0290
Aggregate Beta Model $F_{3,15}$ = 0.0700	0.0458	0.0449	0.0383	0.0301

vary systematically with firm size, which implies that there are no risk differences between small and large utilities.

3.2 January Effect

A January effect is closely associated with the size effect [4,26]. It appears in two distinct ways. First, average returns for all size categories are larger in January than in non-January months (referred to as the 'seasonal returns effect"). And second, the difference between annual returns on smaller and larger firms is concentrated in January (referred to as the 'January small firm effect").

The seasonal returns effect is a stock market anomaly, possibly indicating that stocks in general represent a riskier investment in January than in other months. The existence of such an effect among utility stocks neither suggests nor justifies an adjustment to a firm's cost of capital or allowable ARR. A January small firm effect, on the other hand, would suggest that the riskiness of stocks varies systematically with firm size, and thus if present, might imply that allowable ARRs should be adjusted to reflect firm size.

Table 3 summarizes the tests for a seasonal returns effect. The tests are based on abnormal returns cumulated monthly for each of the four portfolios and for the aggregate portfolio of all utility stocks. The monthly returns permit tests of significant difference between the abnormal returns in January

TABLE 2

Average Beta and Raw Returns by Portfolio

	MV_1	MV_2	MV_3	MV_4
Average Beta F_3 = 1.171	.481	.532	.522	.539
Average Raw Return F_3 = 0.890	.078	.079	.065	.084

TABLE 3

Summary of Tests for a Seasonal Returns Effect: Differences Between Abnormal Returns in January and Other Months

Market Model	MV_1		MV_2		MV_3		MV_4		All Firms	
Month	*Mean*	*Other Tests*	*Mean*	*Other Tests*	*Mean*	*Other Tests*	*Mean*	*Other Tests*	*Mean*	*Other Tests*
February	−.0084 (5.33*)	T,D,S	−.0165 (8.51**)	T,D,S	−.0190 (6.53*)	T,D,S	−.0112 (4.92*)	T,D,S	−.0138 (25.65**)	T,D,S
March	−.0162 (10.05**)	T,D,S	−.0097 (6.81*)	T,D,S	−.0139 (5.66*)	T,D,S	−.0111 (6.66*)	T,D,S	−.0127 (29.67**)	T,D,S
April	−.0050 (3.01)		−.0108 (4.71*)	T,D,S	−.0174 (4.43*)	T,D,S	−.0135 (4.16*)	T,D,S	−.0117 (16.60**)	T,D,S
May	−.0151 (5.65)	T,D,S	−.0057 (4.62*)	T,D,S	−.0043 (1.99)		−.0013 (1.67)		−.0066 (15.09**)	T,D,S
June	.0023 (1.85)		.0001 (2.17)		.0009 (0.66)		.0005 (1.50)		.0009 (6.17*)	T,D,S
July	−.0018 (3.59)		−.0049 (4.77*)	T,D,S	.0053 (0.31)		.0002 (2.23)		−.0003 (9.86**)	T,D,S
August	−.0069 (4.95*)	T,D,S	−.0092 (5.54*)	T,D,S	−.0093 (3.03)		−.0057 (3.65)		−.0078 (17.53**)	T,D,S
September	−.0054 (4.68*)		−.0031 (3.95)		−.0048 (2.01)		−.0001 (2.16)		−.0033 (12.82**)	T,D,S

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TABLE 3 (*cont.*)

Market Model	MV_1		MV_2		MV_3		MV_4		*All Firms*	
Month	*Mean*	*Other Tests*	*Mean*	*Other Tests*	*Mean*	*Other Tests*	*Mean*	*Other Tests*	*Mean*	*Other Tests*
October	.0066		.0048		.0037		.0078		.0057	
	(1.21)		(1.47)		(0.38)		(0.50)		(3.45)	
November	.0037		.0027		−.0014		.0027		.0019	T,D,S
	(1.47)		(1.85)		(0.99)		(1.14)		(5.56*)	
December	−.0015		−.0052	T,D,S	−.0058		.0074		−.0013	T,D,S
	(2.89*)		(4.32**)		(2.11)		(0.66)		(9.56**)	
Eleven Months	.0043	T,D,S	.0052	T,D,S	.0059	T,D,S	.0022	T,D,S	.0044	T,D,S
	(9.25**)		(11.07**)		(4.65*)		(5.15*)		(29.18**)	

Note: In the mean column, the F statistic from a general linear model appears in parentheses below the mean. In the column labeled 'Other Tests, significance is indicated by T, D, and/or S if the month's abnormal return is significantly different from January's according to Tukey's, Dunn's, and/or Scheffe's tests, respectively. Significance for the F test is noted with a [illegible] or [illegible] for significance at the 0.01 and 0.05 levels, respectively.

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TABLE 4

Summary of Tests for a January Firm Size Effect

Market Model	MV_1	MV_2	MV_3	MV_4
Average January Abnormal Return	0.0164	0.0232	0.0186	0.0109
F_3 = 0.349				

and in the other individual months (rows 1 through 11), and between the abnormal returns in January and the other months in aggregate (row 12). The statistical significance of the differences was evaluated using an F statistic from a general linear model and with the Tukey, Dunn, and Scheffe tests; significant differences at the .05 level for these tests are labeled T, D, or S, respectively.

The results in Table 3 indicate that (1) the abnormal returns in January were significantly higher than the average of the non-January months for all four size portfolios and for the aggregate sample; (2) the abnormal returns in January were significantly higher than the returns for the other months in 8 of the 11 tests for the aggregate sample; and (3) for the four portfolios, the abnormal returns in January were significantly greater than the returns in individual months in 17 of the 44 comparisons. Thus, the data provide some evidence of a seasonal returns effect.[4]

Table 4 compares the January returns for MV_1 through MV_4 to investigate for the presence of a January small firm effect for the sample of utilities. The F statistic comparing the mean returns was 0.349 and is statistically insignificant. Even the nominal size of the returns indicates the absence of a relationship with firm size.

3.3 Analysis of Results

One explanation for the positive association between beta and firm size observed by Melicher [18] and between ex ante risk premium and size observed by Reichenstein and Davidson [19] may involve the time periods investigated.[5] Both studies examined periods when large firms generally

4. One possible explanation for the seasonal returns effect is that more information becomes available in January than in other months because of the number of companies with December 31 year-end dates. The release (or leak) of year-end information may produce a significant reduction in uncertainty, lowering of risk, and raising of stock prices across the range of firm size [1]. If the seasonal returns effect represents a predictable pattern, presumably the natural workings of self-interested investors should have eliminated it.

5. Melicher [18] used data for the period 1967 to 1971. For this same time period, the average CAR for MV_1 through MV_4 for the current sample of utilities was −.0569, −.0824, −.0783, and −.0682, respectively. The F-statistic for these values is insignificant, suggesting that an explanation based on time period differences can be rejected.

outperformed small firms. Brown, Kleidon, and Marsh [8] report that the size effect is unstable over time; thus, it is possible that the direction and strength of the size effect may vary as a function of the time period investigated. Nonetheless, over the 23-year period investigated in this study, no evidence of a material size effect was observed.

Research since Melicher also suggests that his results may have been influenced by error-in-variables or estimation problems. The error-in-variables problems include questions involving the reliability of individual betas (see [5], and [23], among others), and the use of the log of total assets as a measure of size. Brown, Kleidon, and Marsh, for instance, indicate that the size effect is best measured by the log of market value of common equity. Moreover, the presence of heteroskedasticity in the cross-sectional sample—a possibility apparently not considered in earlier research—may produce biased *t* statistics.

Further, the size difference between the companies in our sample may not be as large as the size difference in other studies. The equity value of the largest firms in 1985 (valued as of 31 December 1984) was $6.5 billion and in 1963 was $72.5 million. Comparable figures for the smallest firms are $40.2 million in 1985 and $5.7 million in 1963.[6] Even this range, however, should permit detection of a significant size effect if it exists, and our results do not reveal even a nominal size effect (ignoring tests of significance).

Finally, recent research [10,11,16] suggests that the small firm effect is related to the losing firm effect: smaller firms on organized exchanges consist largely of firms that have recently lost market value, and because of the leverage effect or increased financial distress, they become risky firms. The relative stability of utility stocks, and the regulatory charge to avoid possible financial distress, suggest that utility companies may be relatively exempt from the losing firm effect.[7]

4. Summary and Implications

Substantial empirical evidence indicates that small firm stocks consistently produce higher risk-adjusted returns than large firm stocks. On the

6. Basu [3] reports the median for his small firm portfolio to be $30.3 million over the period 1963 to 1979. Our small firm portfolio of utilities had a median of $49.8 million over this same time period. Hence, the utilities in our sample are not as small as the firms in Basu's small firm portfolio, but they are smaller than his second-ranked group, which had a median of $81.6 million. We believe there are sufficiently large size differences among the utilities in our sample to permit a valid test of the size effect.

7. We define a 'losing firm' as one whose stock experienced negative returns in a given year. For most utilities, the largest component of return is dividend yield, so stock price decreases generally do not cause annual negative returns. For our sample, drawn from 1963 through 1985, the proportion of losing stocks in MV_1 through MV_4 was 22, 17, 22, and 24 percent, respectively. We conclude that small utility stocks are not dominated by losing stocks.

basis of this evidence, some researchers have argued that a utility's cost of capital and therefore its allowable ARR should be adjusted to reflect a firm's size.

Although the extant literature provides evidence of two within-industry studies indicating that the relation between utility size and returns is positive, we arrive at a different conclusion. On the basis of historical returns on electric utility stocks for the period 1963 through 1985, we are unable to reject the null hypothesis that annual and January-only abnormal returns are equal among utility portfolios of varying size. Further, raw returns and betas were not found to vary systematically with portfolio size.

The evidence obtained in this study indicates that abnormal returns in January exceed the average abnormal returns in the other eleven months. However, this seasonal returns effect was found to exist across *all* size portfolios, and hence we conclude that it is unrelated to firm size. Thus, our results suggest that neither large nor small utilities merit a premium because of their size.

The implications of our findings for regulatory officials and for regulatory accounting standard-setters are straightforward: we find no evidence among the electric utility industry during the period 1963 to 1985 to suggest that a utility's cost of capital or its allowable ARR should be adjusted to reflect firm size.

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UTILITY STOCKS AND THE SIZE EFFECT: AN EMPIRICAL ANALYSIS

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I. Introduction

The objective of this study is to examine whether the firm size effect exists in the public utility industry. Public utilities are regulated by federal, municipal, and state authorities. Every state has a public service commission with board and varying powers. Often their task is to estimate a fair rate of return to a utility's stockholders in order to determine the rates charged by the utility. The legal principles underlying rate regulation are that "the return to the equity owner should be commensurate with returns on investments in other enterprises having corresponding risks," and that the return to a utility should be sufficient to "attract capital and maintain credit worthiness."[1] However, difficulties arise from the ambiguous interpretation of the legal definition of *fair and reasonable rate of return* to an equity owner.

Some finance researchers have suggested that the Capital Asset Pricing Model (CAPM) should be used in rate regulation because the CAPM beta can serve as a risk measure, thus making risk comparisons possible. This approach is consistent with the spirit of a Supreme Court ruling that equity owners sharing similar level of risk should be compensated by similar rate of return.

The empirical studies of Banz (1981) and Reinganum (1981) showed that small firms tend to earn higher returns than large firms after adjusting for beta. This phenomenon leads to the proposition that firm size is a proxy for omitted risk factors in determining stock returns. Barry and Brown (1984) and Brauer (1986) suggested that the omitted risk factor could be the differential information environment between small and large firms. Their argument is based on the fact that investors often have less publicly available information to assess the future cash flows of small firms than that of large firms. Therefore, an additional risk premium should be included to determine the appropriate rate of return to *shareholders* of small firms.

The samples used in prior studies are dominated by industrial firms, no one has examined the size effect in public utilities. The objective of this study is to extend the empirical findings of the existing studies by investigating whether the size effect is also present in the utility industry. The findings of this study have important implications for investors, public utility firms, and state regulatory agencies. If the size effect does exist in the utility industry, this would suggest that the size factor should be considered when the CAPM is being used to determine the fair rate of return for public utilities in regulatory proceedings.

II. Information Environment of Public Utilities

In general, utilities differ from industriales in that utilities are heavily regulated and they follow similar accounting procedures. A public utility's financial reporting is mainly regulated by the Securities and Exchange Commission (SEC) and the Federal Energy Regulatory Commission (FERC). Under the Public Utility Holding Company Act of 1935, the SEC is empowered to regulate the holding company systems of electric and gas utilities. The Act requires registration of public utility holding companies with the SEC. Only under strict conditions would the purchase, sale or issuance of securities by these holding companies be permitted. The purpose of the Act is to keep the SEC and investors informed of the financial conditions of these firms. Moreover, the FERC is in charge of the interstate operations of electric and gas companies. It requires utilities to follow the accounting procedures set forth in its Uniform Systems of Accounts. In particular, electric and gas utilities must request their Certified Public Accountants to certify that certain schedules in the financial reports are in conformity with the Commission's accounting requirements. These detailed reports are submitted annually and are open to the public.

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The FERC requires public utilities to keep accurate records of revenues, operating costs, depreciation expenses, and investment in plant and equipment. Specific financial accounting standards for these purposes are also issued by the Financial Accounting Standards Board (FASB). Uniformity is required so that utilities are not subject to different accounting regulations in each of the states in which they operate. The ultimate objective is to achieve comparability in financial reporting so that factual matters are not hidden from the public view by accounting flexibility.

Other regulatory reports tend to provide additional financial information about utilities. For example, utilities are required to file the FERC Form No. 1 with the state commission. This form is designed for state commissions to collect financial and operational information about utilities, and serves as a source for statistical reports published by state commissions.

Unlike industriales, a utility's earnings are predetermined to a certain extent. Before allowed earnings requests are approved, a utility's performance is analyzed in depth by the state commission, interest groups, and other witnesses. This process leads to the disclosure of substantial amount of information.

III. Hypothesis and Objective

Due to the Act of 1935, the Uniform Systems of Accounts, the uniform disclosure requirements, and the predetermined earnings, all utilities are reasonably homogeneous with respect to the information available to the public. Barry and Brown (1984) and Brauer (1986) suggested that the difference of risk-adjusted returns between small and large firms is due to their differential information environment. Assuming that the differential information hypothesis is true, then uniformity of information availability among utility firms would suggest that the size effect should not be observed in the public utility industry. The objective of this paper is to provide a test of the size effect in public utilities.

IV. Methodology

1. Sample and Data

To test for the size effect, a sample of public utilities and a sample of industriales matched by equity value are formed so that their results can be compared. Companies in both samples are listed on the Center for Research in Security Prices (CRSP) Daily and Monthly Returns files. The utility sample includes 152 electric and gas companies. For each utility in the sample, two industrial firms with similar firm size (one is slightly larger and the other is slightly smaller than the utility) are selected. Thus, the industrial sample includes 304 non-regulated firms.

The size variable is defined as the natural logarithm of market value of equity at the beginning of each year. Both the equally-weighted and value-weighted CRSP indices are employed as proxies for the market returns. Daily, weekly and monthly returns are used. The Fama-MacBeth (1973) procedure is utilized to examine the relation between risk-adjusted returns and firm size.

2. Research Design

All utilities in the sample are ranked according to the equity size at the beginning of the year, and the distribution is broken down into deciles. Decile one contains the stocks with the lowest market values while decile ten contains those with the highest market values. These portfolios are denoted by MV_1, MV_2, ... and MV_{10}, respectively.

The combinations of the ten portfolios are updated annually. In the year after a portfolio is formed, equally-weighted portfolio returns are computed by combining the returns of the component stocks within the portfolio. The betas for each portfolio at year t, β_{pt}'s, are estimated by regressing the previous five years of portfolio returns on market returns:

$$\tilde{R}_{pt} = \alpha_p + \beta_{pt}\tilde{R}_{mt} + \tilde{U}_{pt} \qquad (1)$$

where

R_{pt} = periodic return in year t on portfolio p

R_{mt} = periodic market return in year t

U_{pt} = disturbance term.

Banz (1981) applied both the ordinary and generalized least squares regressions to estimate β; and concluded that the results are essentially identical (p.8). Since adjusting for heteroscedasticity does not necessarily lead to more efficient estimators, the ordinary least squares procedures are used in this study to estimate β in equation (1).

The following cross-sectional regression is then run for the portfolios to estimate γ_{it}, i = 0, 1, and 2:

$$R_{pt} = \gamma_0 + \gamma_1\hat{\beta}_{pt} + \gamma_2\hat{S}_{pt} + U_{pt} \qquad (2)$$

where

$\hat{\beta}_{pt}$ = estimated beta for portfolio p at year t, t=1968, ., 1987

$\hat{S}_{pt}$ = mean of the logarithm of firm size in portfolio p at the beginning of year t

U_{pt} = disturbance term.

Depending on whether daily, weekly or monthly returns are used, a portfolio's average return changes periodically while its beta and size only change once a year. The γ_1 and γ_2 coefficients are estimated over the following four subperiods: 1968-72, 1973-77, 1978-82 and 1983-1987. If portfolio betas can fully account for the differences in returns, one would expect the average coefficient for the beta variable to be positive and for the size variable to be zero. A t-statistic will be used to test the hypothesis. The coefficients of a matched sample are also examined so that the results between industrial and utility firms can be compared.

V. Analysis of Results

1. Equity Value of the Utility Portfolios

The mean equity values of the ten size-based utility portfolios are reported in Table 1. Panels A and B present the average firm size of these portfolios at the beginning and end of the test period, 1968-1987. The first interesting observation from Table 1 is that the difference in magnitude between the smallest and the largest market value utility portfolios is tremendous. In Panel A, the average size of MV_1 is about $31 million while that of MV_{10} is over $1.4 billion. In Panel B, that is twenty years later, they are $62 million and $5.2 billion, respectively. Another interesting finding is that there is a substantial increase in average firm size from MV_9 to MV_{10}. Since these two findings are consistent over the entire test period, the average portfolio market values for interim years are not reported. These results are similar to the empirical evidence provided by Reinganum (1981).

The utility sample in this study contains 152 firms whereas Reinganum's sample contains 535 firms that are mainly industrial companies. Two conclusions may be drawn from the results of the Reinganum study and this one. First, utilities and industriales are similar in the sense that their market values vary over a wide spectrum. Second, the fact that there is a huge jump in firm size from MV_9 to MV_{10} indicates that the distribution of firm size is positively skewed. To correct for the skewness problem, the natural logarithm of the mean equity value of each portfolio is calculated. This variable is then used in later regressions instead of the actual mean equity value.

2. Betas of the Utility and Industrial Samples

The betas based on monthly, weekly and daily returns are reported for the utility and industrial samples. For simplicity, they will be referred to as monthly, weekly, and daily betas. In all cases, five years of returns are used to estimate the systematic risk. The betas estimated over the 1963-67 time period are used to proxy for the betas in 1968, which is the beginning of the test period. By the same token, the betas obtained from the time period 1982-86 are used as proxies for the betas in 1987, which is the end of the test period.

The betas from using the equally-weighted and value-weighted indices are calculated in order to check whether the results are affected by the choice of market index. Since the results are similar, only those obtained from the equally-weighted index are reported and analyzed.

Table 2 reports the monthly, weekly and daily betas of the two samples at the beginning and end of the test period. Panel A shows the various betas of the industrial portfolios. Two conclusions may be drawn. First, in the 1960's, smaller market value portfolios tend to have relatively larger betas. This is consistent with the empirical findings by Banz (1981) and Reinganum (1981). Second, this trend seems to vanish in the 1980's, especially when weekly and daily returns are used.

The betas of the utility portfolios are presented in Panel B. The table shows that none of the utility betas are greater than 0.71. A comparison between Panels A and B reveals that utility portfolios are relatively less risky than industrial portfolios after controlling for firm size. The comparison also reveals that, unlike industrial stocks, betas of the utility portfolios are not related to the market values of equity.

The negative correlation between firm size and beta in the industrial sample may introduce a multicollinearity problem in estimating equation (2). Banz (p.11) had addressed this issue and concluded that the test results are not sensitive to the multicollinearity problem. For the utility sample, this problem does not exist.

3. Tests on the Coefficients of Beta and Size

The beta and firm size are used to estimate γ_1 and γ_2 in equation (2). A t-statistic is used to test if the mean values of the gammas are significantly different from zero. The tests were performed for four 5-year periods which are reported in Table 3. The mean of the gammas and their t-statistic are presented in Panel A for the utilities and in Panel B for the industrial firms.

The empirical results for the utility sample are reported in Panel A of Table 3. When monthly returns are used, 60 regressions were run to obtain 60 pairs of gammas for each of the 5-year periods. When daily returns are used, over 1200 regressions were run for each period to obtain the gammas. The results are similar: in all of the time periods tested, none of the average coefficients for beta and size are significantly different from zero. When weekly returns are used, 260 pairs of gammas were obtained. The average coefficients for beta are not significant in any test period, and the average coefficients for size are not significant in three of the test periods. For the test period of 1978-82, the average coefficient for size is significantly negative at a 5% level.

The test results for the industrial sample are reported in Panel B of Table 3. When monthly returns are used, the average coefficient estimates for size and beta are significant and have the expected sign only in the 1983-87 test period. When weekly returns are used, only the size variable is significantly negative in the 1978-82 period. When daily returns are used, the coefficient estimates for betas and size are not significant at any conventional level.

According to the CAPM, beta is the sole determinant of stock returns. It is expected that the coefficient for beta is significantly positive. However, the empirical findings reported in this study and in Fama and French (1992) only provide weak support for beta in explaining stock returns. The empirical findings in this study also suggest that the size effect varies over time. It is not unusual to document the firm size effect at certain time periods but not at others. Banz (1981) found that the size effect is not stable over time with substantial differences in the magnitude of the coefficient of the size factor (p.9, Table 1). Brown, Kleidon and Marsh (1983) not only have shown that size effect is not constant over time but also have reported a reversal of the size anomaly for certain years.

The research design of this study allows us to keep the sample, test period, and methodology the same with the holding-period being the only variable. The size effect is documented for the industrial sample in one of the four test periods when monthly returns are used and in another when weekly returns are used. When daily returns are used, no size effect is observed. For the utility sample, the size effect is significant in only one test period when weekly returns are used. When monthly and daily returns are used, no size effect is found. Therefore, this study concludes that the size effect is not only time-period specific but also holding-period specific.

VI. Concluding Remarks

The fact that the two samples show different, though weak, results indicates that utility and industrial stocks do not share the same characteristics. First, given firm size, utility stocks are consistently less risky than industrial stocks. Second, industrial betas tend to decrease with firm size but utility betas do not. These findings may be attributed to the fact that all public utilities operate in an environment with regional monopolistic power and regulated financial structure. As a result, the business and financial risks are very similar among the utilities regardless of their sizes. Therefore, utility betas would not necessarily be expected to be related to firm size.

The objective of this study is to examine if the size effect exists in the utility industry. After controlling for equity values, there is some weak evidence that firm size is a missing factor from the CAPM for the industrial but not for the utility stocks. This implies that although the size phenomenon has been strongly documented for the industriales, the findings suggest that there is no need to adjust for the firm size in utility rate regulations.

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Table 1

Average Equity Size of the Utility Portfolios at the Beginning and End of the Test Period
(Dollar figures in millions)

	A: Beginning (1968)	B: End (1987)
MV_1	$31	$62
MV_2	$77	$177
MV_3	$113	$334
MV_4	$161	$475
MV_5	$220	$715
MV_6	$334	$957
MV_7	$437	$1,279
MV_8	$505	$1,805
MV_9	$791	$2,665
MV_{10}	$1,447	$5,399

Table 2

Betas of the Two Samples at the Beginning and End of the Test Period

	Monthly Betas		Weekly Betas		Daily Betas	
	1963-67	1982-86	1963-67	1982-86	1963-67	1982-86
Panel A: Industrial Firms						
MV_1	0.89	1.00	1.15	0.95	1.11	0.92
MV_2	0.94	0.87	1.07	1.01	1.14	1.01
MV_3	0.88	0.82	1.12	0.86	1.14	1.04
MV_4	0.69	0.74	1.00	0.83	1.03	0.86
MV_5	0.73	0.80	1.05	0.96	1.13	1.01
MV_6	0.66	0.82	1.03	1.01	1.05	1.04
MV_7	0.64	0.81	0.97	1.04	0.98	1.09
MV_8	0.62	0.75	0.97	1.11	1.00	1.20
MV_9	0.52	0.78	0.84	1.06	0.94	1.16
MV_{10}	0.43	0.65	0.78	1.01	0.86	1.22
Panel B: Public Utilities						
MV_1	0.30	0.37	0.31	0.43	0.30	0.40
MV_2	0.28	0.38	0.37	0.47	0.36	0.44
MV_3	0.22	0.42	0.33	0.42	0.31	0.49
MV_4	0.27	0.35	0.36	0.52	0.34	0.54
MV_5	0.25	0.45	0.37	0.61	0.35	0.62
MV_6	0.25	0.41	0.39	0.54	0.40	0.65
MV_7	0.20	0.35	0.34	0.54	0.37	0.63
MV_8	0.17	0.38	0.34	0.65	0.33	0.68
MV_9	0.19	0.34	0.35	0.60	0.34	0.71
MV_{10}	0.18	0.29	0.38	0.59	0.39	0.71

Table 3

Tests on the Mean Coefficients of Beta (γ_1) and Size (γ_2)

$$R_{jt} = \gamma_{ot} + \gamma_{1t}\hat{\beta}_{jt} + \gamma_{2t}\hat{S}_{jt} + U_{jt}$$

Returns Used:		Monthly (t-value)	Weekly (t-value)	Daily (t-value)
Panel A: Utility Sample				
1968-72	γ_1	-0.46% (-0.26)	-0.32% (-0.42)	-0.02% (-0.18)
	γ_2	-0.07% (-0.78)	-0.01% (-0.51)	-0.00% (-0.46)
1973-77	γ_1	-0.28% (-0.13)	0.14% (0.14)	-0.03% (-0.21)
	γ_2	-0.11% (-0.70)	-0.03% (-0.67)	-0.00% (-0.53)
1978-82	γ_1	0.55% (0.36)	0.54% (1.00)	0.05% (0.43)
	γ_2	-0.10% (-0.75)	-0.05% (-1.71)*	-0.01% (-1.60)
1983-87	γ_1	1.74% (1.28)	-0.24% (-0.51)	-0.02% (-0.18)
	γ_2	-0.16% (-1.54)	-0.03% (-0.86)	-0.01% (-0.63)
Panel B: Industrial Sample				
1968-72	γ_1	-0.36% (-0.27)	-0.28% (-0.55)	-0.02% (-0.32)
	γ_2	0.07% (0.43)	-0.01% (-0.19)	0.00% (0.51)
1973-77	γ_1	1.34% (0.64)	-0.23% (-0.31)	0.14% (1.45)
	γ_2	-0.01% (-0.06)	-0.04% (-0.85)	-0.00% (-0.64)
1978-82	γ_1	-0.84% (-0.28)	-0.56% (-0.91)	-0.09% (-0.81)
	γ_2	-0.29% (-0.75)	-0.01% (-1.72)*	-0.00% (-1.33)
1983-87	γ_1	2.51% (1.83)*	0.34% (0.64)	0.11% (1.40)
	γ_2	-0.25% (-1.90)*	-0.01% (-0.43)	0.00% (0.14)

* Significant at the 5% level based on a one-tailed test.

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THE COST OF CAPITAL, CORPORATION FINANCE AND THE THEORY OF INVESTMENT

By FRANCO MODIGLIANI AND MERTON H. MILLER*

What is the "cost of capital" to a firm in a world in which funds are used to acquire assets whose yields are uncertain; and in which capital can be obtained by many different media, ranging from pure debt instruments, representing money-fixed claims, to pure equity issues, giving holders only the right to a pro-rata share in the uncertain venture? This question has vexed at least three classes of economists: (1) the corporation finance specialist concerned with the techniques of financing firms so as to ensure their survival and growth; (2) the managerial economist concerned with capital budgeting; and (3) the economic theorist concerned with explaining investment behavior at both the micro and macro levels.[1]

In much of his formal analysis, the economic theorist at least has tended to side-step the essence of this cost-of-capital problem by proceeding as though physical assets—like bonds—could be regarded as yielding known, sure streams. Given this assumption, the theorist has concluded that the cost of capital to the owners of a firm is simply the rate of interest on bonds; and has derived the familiar proposition that the firm, acting rationally, will tend to push investment to the point

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[1] The literature bearing on the cost-of-capital problem is far too extensive for listing here. Numerous references to it will be found throughout the paper though we make no claim to completeness. One phase of the problem which we do not consider explicitly, but which has a considerable literature of its own is the relation between the cost of capital and public utility rates. For a recent summary of the "cost-of-capital theory" of rate regulation and a brief discussion of some of its implications, the reader may refer to H. M. Somers [20].

where the marginal yield on physical assets is equal to the market rate of interest.[2] This proposition can be shown to follow from either of two criteria of rational decision-making which are equivalent under certainty, namely (1) the maximization of profits and (2) the maximization of market value.

According to the first criterion, a physical asset is worth acquiring if it will increase the net profit of the owners of the firm. But net profit will increase only if the expected rate of return, or yield, of the asset exceeds the rate of interest. According to the second criterion, an asset is worth acquiring if it increases the value of the owners' equity, *i.e.*, if it adds more to the market value of the firm than the costs of acquisition. But what the asset adds is given by capitalizing the stream it generates at the market rate of interest, and this capitalized value will exceed its cost if and only if the yield of the asset exceeds the rate of interest. Note that, under either formulation, the cost of capital is equal to the rate of interest on bonds, regardless of whether the funds are acquired through debt instruments or through new issues of common stock. Indeed, in a world of sure returns, the distinction between debt and equity funds reduces largely to one of terminology.

It must be acknowledged that some attempt is usually made in this type of analysis to allow for the existence of uncertainty. This attempt typically takes the form of superimposing on the results of the certainty analysis the notion of a "risk discount" to be subtracted from the expected yield (or a "risk premium" to be added to the market rate of interest). Investment decisions are then supposed to be based on a comparison of this "risk adjusted" or "certainty equivalent" yield with the market rate of interest.[3] No satisfactory explanation has yet been provided, however, as to what determines the size of the risk discount and how it varies in response to changes in other variables.

Considered as a convenient approximation, the model of the firm constructed via this certainty—or certainty-equivalent—approach has admittedly been useful in dealing with some of the grosser aspects of the processes of capital accumulation and economic fluctuations. Such a model underlies, for example, the familiar Keynesian aggregate investment function in which aggregate investment is written as a function of the rate of interest—the same riskless rate of interest which appears later in the system in the liquidity-preference equation. Yet few would maintain that this approximation is adequate. At the macroeconomic level there are ample grounds for doubting that the rate of interest has

[2] Or, more accurately, to the marginal cost of borrowed funds since it is customary, at least in advanced analysis, to draw the supply curve of borrowed funds to the firm as a rising one. For an advanced treatment of the certainty case, see F. and V. Lutz [13].

[3] The classic examples of the certainty-equivalent approach are found in J. R. Hicks [8] and O. Lange [11].

as large and as direct an influence on the rate of investment as this analysis would lead us to believe. At the microeconomic level the certainty model has little descriptive value and provides no real guidance to the finance specialist or managerial economist whose main problems cannot be treated in a framework which deals so cavalierly with uncertainty and ignores all forms of financing other than debt issues.[4]

Only recently have economists begun to face up seriously to the problem of the cost of capital *cum* risk. In the process they have found their interests and endeavors merging with those of the finance specialist and the managerial economist who have lived with the problem longer and more intimately. In this joint search to establish the principles which govern rational investment and financial policy in a world of uncertainty two main lines of attack can be discerned. These lines represent, in effect, attempts to extrapolate to the world of uncertainty each of the two criteria—profit maximization and market value maximization—which were seen to have equivalent implications in the special case of certainty. With the recognition of uncertainty this equivalence vanishes. In fact, the profit maximization criterion is no longer even well defined. Under uncertainty there corresponds to each decision of the firm not a unique profit outcome, but a plurality of mutually exclusive outcomes which can at best be described by a subjective probability distribution. The profit outcome, in short, has become a random variable and as such its maximization no longer has an operational meaning. Nor can this difficulty generally be disposed of by using the mathematical expectation of profits as the variable to be maximized. For decisions which affect the expected value will also tend to affect the dispersion and other characteristics of the distribution of outcomes. In particular, the use of debt rather than equity funds to finance a given venture may well increase the expected return to the owners, but only at the cost of increased dispersion of the outcomes.

Under these conditions the profit outcomes of alternative investment and financing decisions can be compared and ranked only in terms of a *subjective* "utility function" of the owners which weighs the expected yield against other characteristics of the distribution. Accordingly, the extrapolation of the profit maximization criterion of the certainty model has tended to evolve into utility maximization, sometimes explicitly, more frequently in a qualitative and heuristic form.[5]

The utility approach undoubtedly represents an advance over the certainty or certainty-equivalent approach. It does at least permit us

[4] Those who have taken a "case-method" course in finance in recent years will recall in this connection the famous Liquigas case of Hunt and Williams, [9, pp. 193–96] a case which is often used to introduce the student to the cost-of-capital problem and to poke a bit of fun at the economist's certainty-model.

[5] For an attempt at a rigorous explicit development of this line of attack, see F. Modigliani and M. Zeman [14].

to explore (within limits) some of the implications of different financing arrangements, and it does give some meaning to the "cost" of different types of funds. However, because the cost of capital has become an essentially subjective concept, the utility approach has serious drawbacks for normative as well as analytical purposes. How, for example, is management to ascertain the risk preferences of its stockholders and to compromise among their tastes? And how can the economist build a meaningful investment function in the face of the fact that any given investment opportunity might or might not be worth exploiting depending on precisely who happen to be the owners of the firm at the moment?

Fortunately, these questions do not have to be answered; for the alternative approach, based on market value maximization, can provide the basis for an operational definition of the cost of capital and a workable theory of investment. Under this approach any investment project and its concomitant financing plan must pass only the following test: Will the project, as financed, raise the market value of the firm's shares? If so, it is worth undertaking; if not, its return is less than the marginal cost of capital to the firm. Note that such a test is entirely independent of the tastes of the current owners, since market prices will reflect not only their preferences but those of all potential owners as well. If any current stockholder disagrees with management and the market over the valuation of the project, he is free to sell out and reinvest elsewhere, but will still benefit from the capital appreciation resulting from management's decision.

The potential advantages of the market-value approach have long been appreciated; yet analytical results have been meager. What appears to be keeping this line of development from achieving its promise is largely the lack of an adequate theory of the effect of financial structure on market valuations, and of how these effects can be inferred from objective market data. It is with the development of such a theory and of its implications for the cost-of-capital problem that we shall be concerned in this paper.

Our procedure will be to develop in Section I the basic theory itself and to give some brief account of its empirical relevance. In Section II, we show how the theory can be used to answer the cost-of-capital question and how it permits us to develop a theory of investment of the firm under conditions of uncertainty. Throughout these sections the approach is essentially a partial-equilibrium one focusing on the firm and "industry." Accordingly, the "prices" of certain income streams will be treated as constant and given from outside the model, just as in the standard Marshallian analysis of the firm and industry the prices of all inputs and of all other products are taken as given. We have chosen to focus at this level rather than on the economy as a whole because it is at the level of the firm and the industry that the interests of the various specialists concerned with the cost-of-capital problem come most closely together. Although the emphasis has thus been placed on partial-equilibrium analysis, the results obtained also provide the essential building blocks for a general equilibrium model which shows how those prices which are here taken as given, are themselves determined. For reasons of space, however, and because the material is of interest in its own right, the presentation of the general equilibrium model which rounds out the analysis must be deferred to a subsequent paper.

I. *The Valuation of Securities, Leverage, and the Cost of Capital*

A. *The Capitalization Rate for Uncertain Streams*

As a starting point, consider an economy in which all physical assets are owned by corporations. For the moment, assume that these corporations can finance their assets by issuing common stock only; the introduction of bond issues, or their equivalent, as a source of corporate funds is postponed until the next part of this section.

The physical assets held by each firm will yield to the owners of the firm—its stockholders—a stream of "profits" over time; but the elements of this series need not be constant and in any event are uncertain. This stream of income, and hence the stream accruing to any share of common stock, will be regarded as extending indefinitely into the future. We assume, however, that the mean value of the stream over time, or average profit per unit of time, is finite and represents a random variable subject to a (subjective) probability distribution. We shall refer to the average value over time of the stream accruing to a given share as the return of that share; and to the mathematical expectation of this average as the expected return of the share.[6] Although individual investors may have different views as to the shape of the probability distri-

[6] These propositions can be restated analytically as follows: The assets of the *i*th firm generate a stream:

$$X_i(1),\ X_i(2) \qquad X_i(T)$$

whose elements are random variables subject to the joint probability distribution:

$$\chi_i[X_i(1),\ X_i(2) \qquad X_i(t)].$$

The return to the *i*th firm is defined as:

$$X_i = \lim_{T\to\infty} \frac{1}{T} \sum_{t=1}^{T} X_i(t).$$

X_i is itself a random variable with a probability distribution $\Phi_i(X_i)$ whose form is determined uniquely by χ_i. The expected return $\bar{X}_i$ is defined as $\bar{X}_i = E(X_i) = \int_{X_i} X_i \Phi_i(X_i) dX_i$. If N_i is the number of shares outstanding, the return of the *i*th share is $x_i = (1/N)X_i$ with probability distribution $\phi_i(x_i)dx_i = \Phi_i(Nx_i)d(Nx_i)$ and expected value $\bar{x}_i = (1/N)\bar{X}_i$.

bution of the return of any share, we shall assume for simplicity that they are at least in agreement as to the expected return.[7]

This way of characterizing uncertain streams merits brief comment. Notice first that the stream is a stream of profits, not dividends. As will become clear later, as long as management is presumed to be acting in the best interests of the stockholders, retained earnings can be regarded as equivalent to a fully subscribed, pre-emptive issue of common stock. Hence, for present purposes, the division of the stream between cash dividends and retained earnings in any period is a mere detail. Notice also that the uncertainty attaches to the mean value over time of the stream of profits and should not be confused with variability over time of the successive elements of the stream. That variability and uncertainty are two totally different concepts should be clear from the fact that the elements of a stream can be variable even though known with certainty. It can be shown, furthermore, that whether the elements of a stream are sure or uncertain, the effect of variability per se on the valuation of the stream is at best a second-order one which can safely be neglected for our purposes (and indeed most others too).[8]

The next assumption plays a strategic role in the rest of the analysis. We shall assume that firms can be divided into "equivalent return" classes such that the return on the shares issued by any firm in any given class is proportional to (and hence perfectly correlated with) the return on the shares issued by any other firm in the same class. This assumption implies that the various shares within the same class differ, at most, by a "scale factor." Accordingly, if we adjust for the difference in scale, by taking the *ratio* of the return to the expected return, the probability distribution of that ratio is identical for all shares in the class. It follows that all relevant properties of a share are uniquely characterized by specifying (1) the class to which it belongs and (2) its expected return.

The significance of this assumption is that it permits us to classify firms into groups within which the shares of different firms are "homogeneous," that is, perfect substitutes for one another. We have, thus, an analogue to the familiar concept of the industry in which it is the commodity produced by the firms that is taken as homogeneous. To complete this analogy with Marshallian price theory, we shall assume in the

[7] To deal adequately with refinements such as differences among investors in estimates of expected returns would require extensive discussion of the theory of portfolio selection. Brief references to these and related topics will be made in the succeeding article on the general equilibrium model.

[8] The reader may convince himself of this by asking how much he would be willing to rebate to his employer for the privilege of receiving his annual salary in equal monthly installments rather than in irregular amounts over the year. See also J. M. Keynes [10, esp. pp. 53–54].

analysis to follow that the shares concerned are traded in perfect markets under conditions of atomistic competition.[9]

From our definition of homogeneous classes of stock it follows that in equilibrium in a perfect capital market the price per dollar's worth of expected return must be the same for all shares of any given class. Or, equivalently, in any given class the price of every share must be proportional to its expected return. Let us denote this factor of proportionality for any class, say the kth class, by $1/\rho_k$. Then if p_j denotes the price and $\bar{x}_j$ is the expected return per share of the jth firm in class k, we must have:

$$p_j = \frac{1}{\rho_k} \bar{x}_j; \tag{1}$$

or, equivalently,

$$\frac{\bar{x}_j}{p_j} = \rho_k \text{ a constant for all firms } j \text{ in class } k. \tag{2}$$

The constants ρ_k (one for each of the k classes) can be given several economic interpretations: (a) From (2) we see that each ρ_k is the expected rate of return of any share in class k. (b) From (1) $1/\rho_k$ is the price which an investor has to pay for a dollar's worth of expected return in the class k. (c) Again from (1), by analogy with the terminology for perpetual bonds, ρ_k can be regarded as the market rate of capitalization for the expected value of the uncertain streams of the kind generated by the kth class of firms.[10]

B. *Debt Financing and Its Effects on Security Prices*

Having developed an apparatus for dealing with uncertain streams we can now approach the heart of the cost-of-capital problem by dropping the assumption that firms cannot issue bonds. The introduction of debt-financing changes the market for shares in a very fundamental way. Because firms may have different proportions of debt in their capi-

[9] Just what our classes of stocks contain and how the different classes can be identified by outside observers are empirical questions to which we shall return later. For the present, it is sufficient to observe: (1) Our concept of a class, while not identical to that of the industry is at least closely related to it. Certainly the basic characteristics of the probability distributions of the returns on assets will depend to a significant extent on the product sold and the technology used. (2) What are the appropriate class boundaries will depend on the particular problem being studied. An economist concerned with general tendencies in the market, for example, might well be prepared to work with far wider classes than would be appropriate for an investor planning his portfolio, or a firm planning its financial strategy.

[10] We cannot, on the basis of the assumptions so far, make any statements about the relationship or spread between the various ρ's or capitalization rates. Before we could do so we would have to make further specific assumptions about the way investors believe the probability distributions vary from class to class, as well as assumptions about investors' preferences as between the characteristics of different distributions.

tal structure, shares of different companies, even in the same class, can give rise to different probability distributions of returns. In the language of finance, the shares will be subject to different degrees of financial risk or "leverage" and hence they will no longer be perfect substitutes for one another.

To exhibit the mechanism determining the relative prices of shares under these conditions, we make the following two assumptions about the nature of bonds and the bond market, though they are actually stronger than is necessary and will be relaxed later: (1) All bonds (including any debts issued by households for the purpose of carrying shares) are assumed to yield a constant income per unit of time, and this income is regarded as certain by all traders regardless of the issuer. (2) Bonds, like stocks, are traded in a perfect market, where the term perfect is to be taken in its usual sense as implying that any two commodities which are perfect substitutes for each other must sell, in equilibrium, at the same price. It follows from assumption (1) that all bonds are in fact perfect substitutes up to a scale factor. It follows from assumption (2) that they must all sell at the same price per dollar's worth of return, or what amounts to the same thing must yield the same rate of return. This rate of return will be denoted by r and referred to as the rate of interest or, equivalently, as the capitalization rate for sure streams. We now can derive the following two basic propositions with respect to the valuation of securities in companies with different capital structures:

Proposition I. Consider any company j and let $\bar{X}_j$ stand as before for the expected return on the assets owned by the company (that is, its expected profit before deduction of interest). Denote by D_j the market value of the debts of the company; by S_j the market value of its common shares; and by $V_j \equiv S_j + D_j$ the market value of all its securities or, as we shall say, the market value of the firm. Then, our Proposition I asserts that we must have in equilibrium:

$$(3) \qquad V_j \equiv (S_j + D_j) = \bar{X}_j/\rho_k, \text{ for any firm } j \text{ in class } k.$$

That is, the *market value of any firm is independent of its capital structure and is given by capitalizing its expected return at the rate ρ_k appropriate to its class.*

This proposition can be stated in an equivalent way in terms of the firm's "average cost of capital," $\bar{X}_j/V_j$, which is the ratio of its expected return to the market value of all its securities. Our proposition then is:

$$(4) \qquad \frac{\bar{X}_j}{(S_j + D_j)} \equiv \frac{\bar{X}_j}{V_j} = \rho_k, \text{ for any firm } j, \text{ in class } k.$$

That is, *the average cost of capital to any firm is completely independent of* *its capital structure and is equal to the capitalization rate of a pure equity stream of its class.*

To establish Proposition I we will show that as long as the relations (3) or (4) do not hold between any pair of firms in a class, arbitrage will take place and restore the stated equalities. We use the term arbitrage advisedly. For if Proposition I did not hold, an investor could buy and sell stocks and bonds in such a way as to exchange one income stream for another stream, identical in all relevant respects but selling at a lower price. The exchange would therefore be advantageous to the investor quite independently of his attitudes toward risk.[11] As investors exploit these arbitrage opportunities, the value of the overpriced shares will fall and that of the underpriced shares will rise, thereby tending to eliminate the discrepancy between the market values of the firms.

By way of proof, consider two firms in the same class and assume for simplicity only, that the expected return, $\bar{X}$, is the same for both firms. Let company 1 be financed entirely with common stock while company 2 has some debt in its capital structure. Suppose first the value of the levered firm, V_2, to be larger than that of the unlevered one, V_1. Consider an investor holding s_2 dollars' worth of the shares of company 2, representing a fraction α of the total outstanding stock, S_2. The return from this portfolio, denoted by Y_2, will be a fraction α of the income available for the stockholders of company 2, which is equal to the total return X_2 less the interest charge, rD_2. Since under our assumption of homogeneity, the anticipated total return of company 2, X_2, is, under all circumstances, the same as the anticipated total return to company 1, X_1, we can hereafter replace X_2 and X_1 by a common symbol X. Hence, the return from the initial portfolio can be written as:

$$Y_2 = \alpha(X - rD_2). \tag{5}$$

Now suppose the investor sold his αS_2 worth of company 2 shares and acquired instead an amount $s_1 = \alpha(S_2 + D_2)$ of the shares of company 1. He could do so by utilizing the amount αS_2 realized from the sale of his initial holding and borrowing an additional amount αD_2 on his own credit, pledging his new holdings in company 1 as a collateral. He would thus secure for himself a fraction $s_1/S_1 = \alpha(S_2 + D_2)/S_1$ of the shares and earnings of company 1. Making proper allowance for the interest payments on his personal debt αD_2, the return from the new portfolio, Y_1, is given by:

[11] In the language of the theory of choice, the exchanges are movements from inefficient points in the interior to efficient points on the boundary of the investor's opportunity set; and not movements between efficient points along the boundary. Hence for this part of the analysis nothing is involved in the way of specific assumptions about investor attitudes or behavior other than that investors behave consistently and prefer more income to less income, *ceteris paribus*.

$$Y_1 = \frac{\alpha(S_2 + D_2)}{S_1} X - r\alpha D_2 = \alpha \frac{V_2}{V_1} X - r\alpha D_2. \tag{6}$$

Comparing (5) with (6) we see that as long as $V_2 > V_1$ we must have $Y_1 > Y_2$, so that it pays owners of company 2's shares to sell their holdings, thereby depressing S_2 and hence V_2; and to acquire shares of company 1, thereby raising S_1 and thus V_1. We conclude therefore that levered companies cannot command a premium over unlevered companies because investors have the opportunity of putting the equivalent leverage into their portfolio directly by borrowing on personal account.

Consider now the other possibility, namely that the market value of the levered company V_2 is less than V_1. Suppose an investor holds initially an amount s_1 of shares of company 1, representing a fraction α of the total outstanding stock, S_1. His return from this holding is:

$$Y_1 = \frac{s_1}{S_1} X = \alpha X.$$

Suppose he were to exchange this initial holding for another portfolio, also worth s_1, but consisting of s_2 dollars of stock of company 2 and of d dollars of bonds, where s_2 and d are given by:

$$s_2 = \frac{S_2}{V_2} s_1, \qquad d = \frac{D_2}{V_2} s_1. \tag{7}$$

In other words the new portfolio is to consist of stock of company 2 and of bonds in the proportions S_2/V_2 and D_2/V_2, respectively. The return from the stock in the new portfolio will be a fraction s_2/S_2 of the total return to stockholders of company 2, which is $(X - rD_2)$, and the return from the bonds will be rd. Making use of (7), the total return from the portfolio, Y_2, can be expressed as follows:

$$Y_2 = \frac{s_2}{S_2}(X - rD_2) + rd = \frac{s_1}{V_2}(X - rD_2) + r\frac{D_2}{V_2} s_1 = \frac{s_1}{V_2} X = \alpha \frac{S_1}{V_2} X$$

(since $s_1 = \alpha S_1$). Comparing Y_2 with Y_1 we see that, if $V_2 < S_1 \equiv V_1$, then Y_2 will exceed Y_1. Hence it pays the holders of company 1's shares to sell these holdings and replace them with a mixed portfolio containing an appropriate fraction of the shares of company 2.

The acquisition of a mixed portfolio of stock of a levered company j and of bonds in the proportion S_j/V_j and D_j/V_j respectively, may be regarded as an operation which "undoes" the leverage, giving access to an appropriate fraction of the unlevered return X_j. It is this possibility of undoing leverage which prevents the value of levered firms from being consistently less than those of unlevered firms, or more generally prevents the average cost of capital $\bar{X}_j/V_j$ from being systematically higher for levered than for nonlevered companies in the same class.

Since we have already shown that arbitrage will also prevent V_2 from being larger than V_1, we can conclude that in equilibrium we must have $V_2 = V_1$, as stated in Proposition I.

Proposition II. From Proposition I we can derive the following proposition concerning the rate of return on common stock in companies whose capital structure includes some debt: the expected rate of return or yield, i, on the stock of any company j belonging to the kth class is a linear function of leverage as follows:

$$i_j = \rho_k + (\rho_k - r)D_j/S_j. \tag{8}$$

That is, *the expected yield of a share of stock is equal to the appropriate capitalization rate ρ_k for a pure equity stream in the class, plus a premium related to financial risk equal to the debt-to-equity ratio times the spread between ρ_k and r.* Or equivalently, the market price of any share of stock is given by capitalizing its expected return at the continuously variable rate i_j of (8).[12]

A number of writers have stated close equivalents of our Proposition I although by appealing to intuition rather than by attempting a proof and only to insist immediately that the results were not applicable to the actual capital markets.[13] Proposition II, however, so far as we have been able to discover is new.[14] To establish it we first note that, by definition, the expected rate of return, i, is given by:

$$i_j \equiv \frac{\bar{X}_j - rD_j}{S_j} \tag{9}$$

From Proposition I, equation (3), we know that:

$$\bar{X}_j = \rho_k(S_j + D_j).$$

Substituting in (9) and simplifying, we obtain equation (8).

[12] To illustrate, suppose $\bar{X} = 1000$, $D = 4000$, $r = 5$ per cent and $\rho_k = 10$ per cent. These values imply that $V = 10{,}000$ and $S = 6000$ by virtue of Proposition I. The expected yield or rate of return per share is then:

$$i = \frac{1000 - 200}{6000} = .1 + (.1 - .05)\frac{4000}{6000} = 13\tfrac{1}{3} \text{ per cent.}$$

[13] See, for example, J. B. Williams [21, esp. pp. 72–73]; David Durand [3]; and W. A. Morton [15]. None of these writers describe in any detail the mechanism which is supposed to keep the average cost of capital constant under changes in capital structure. They seem, however, to be visualizing the equilibrating mechanism in terms of switches by investors between stocks and bonds as the yields of each get out of line with their "riskiness." This is an argument quite different from the pure arbitrage mechanism underlying our proof, and the difference is crucial. Regarding Proposition I as resting on investors' attitudes toward risk leads inevitably to a misunderstanding of many factors influencing relative yields such as, for example, limitations on the portfolio composition of financial institutions. See below, esp. Section I.D.

[14] Morton does make reference to a linear yield function but only " . . . for the sake of simplicity and because the particular function used makes no essential difference in my conclusions" [15, p. 443, note 2].

C. *Some Qualifications and Extensions of the Basic Propositions*

The methods and results developed so far can be extended in a number of useful directions, of which we shall consider here only three: (1) allowing for a corporate profits tax under which interest payments are deductible; (2) recognizing the existence of a multiplicity of bonds and interest rates; and (3) acknowledging the presence of market imperfections which might interfere with the process of arbitrage. The first two will be examined briefly in this section with some further attention given to the tax problem in Section II. Market imperfections will be discussed in Part D of this section in the course of a comparison of our results with those of received doctrines in the field of finance.

Effects of the Present Method of Taxing Corporations. The deduction of interest in computing taxable corporate profits will prevent the arbitrage process from making the value of all firms in a given class proportional to the expected returns generated by their physical assets. Instead, it can be shown (by the same type of proof used for the original version of Proposition I) that the market values of firms in each class must be proportional in equilibrium to their expected return net of taxes (that is, to the sum of the interest paid and expected net stockholder income). This means we must replace each $\bar{X}_j$ in the original versions of Propositions I and II with a new variable $\bar{X}_j^\tau$ representing the total income net of taxes generated by the firm:

$$\bar{X}_j^\tau \equiv (\bar{X}_j - rD_j)(1 - \tau) + rD_j \equiv \bar{\pi}_j^\tau + rD_j, \tag{10}$$

where $\bar{\pi}_j^\tau$ represents the expected net income accruing to the common stockholders and τ stands for the average rate of corporate income tax.[15]

After making these substitutions, the propositions, when adjusted for taxes, continue to have the same form as their originals. That is, Proposition I becomes:

$$\frac{\bar{X}_j^\tau}{V_j} = \rho_k^\tau, \text{ for any firm in class } k, \tag{11}$$

and Proposition II becomes

$$i_j \equiv \frac{\bar{\pi}_j^\tau}{S_j} = \rho_k^\tau + (\rho_k^\tau - r)D_j/S_j \tag{12}$$

where ρ_k^τ is the capitalization rate for income net of taxes in class k.

Although the form of the propositions is unaffected, certain interpretations must be changed. In particular, the after-tax capitalization rate

[15] For simplicity, we shall ignore throughout the tiny element of progression in our present corporate tax and treat τ as a constant independent of $(\bar{X}_j - rD_j)$.

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ρ_k' can no longer be identified with the "average cost of capital" which is $\rho_k = \bar{X}_j / V_j$. The difference between ρ_k^{τ} and the "true" average cost of capital, as we shall see, is a matter of some relevance in connection with investment planning within the firm (Section II). For the description of market behavior, however, which is our immediate concern here, the distinction is not essential. To simplify presentation, therefore, and to preserve continuity with the terminology in the standard literature we shall continue in this section to refer to ρ_k' as the average cost of capital, though strictly speaking this identification is correct only in the absence of taxes.

Effects of a Plurality of Bonds and Interest Rates. In existing capital markets we find not one, but a whole family of interest rates varying with maturity, with the technical provisions of the loan and, what is most relevant for present purposes, with the financial condition of the borrower.[16] Economic theory and market experience both suggest that the yields demanded by lenders tend to increase with the debt-equity ratio of the borrowing firm (or individual). If so, and if we can assume as a first approximation that this yield curve, $r = r\ (D/S)$, whatever its precise form, is the same for all borrowers, then we can readily extend our propositions to the case of a rising supply curve for borrowed funds.[17]

Proposition I is actually unaffected in form and interpretation by the fact that the rate of interest may rise with leverage; while the average cost of *borrowed* funds will tend to increase as debt rises, the average cost of funds from *all* sources will still be independent of leverage (apart from the tax effect). This conclusion follows directly from the ability of those who engage in arbitrage to undo the leverage in any financial structure by acquiring an appropriately mixed portfolio of bonds and stocks. Because of this ability, the ratio of earnings (*before* interest charges) to market value—*i.e.*, the average cost of capital from all

[16] We shall not consider here the extension of the analysis to encompass the time structure of interest rates. Although some of the problems posed by the time structure can be handled within our comparative statics framework, an adequate discussion would require a separate paper.

[17] We can also develop a theory of bond valuation along lines essentially parallel to those followed for the case of shares. We conjecture that the curve of bond yields as a function of leverage will turn out to be a nonlinear one in contrast to the linear function of leverage developed for common shares. However, we would also expect that the rate of increase in the yield on new issues would not be substantial in practice. This relatively slow rise would reflect the fact that interest rate increases by themselves can never be completely satisfactory to creditors as compensation for their increased risk. Such increases may simply serve to raise r so high relative to ρ that they become self-defeating by giving rise to a situation in which even normal fluctuations in earnings may force the company into bankruptcy. The difficulty of borrowing more, therefore, tends to show up in the usual case not so much in higher rates as in the form of increasingly stringent restrictions imposed on the company's management and finances by the creditors; and ultimately in a complete inability to obtain new borrowed funds, at least from the institutional investors who normally set the standards in the market for bonds.

sources—must be the same for all firms in a given class.[18] In other words, the increased cost of borrowed funds as leverage increases will tend to be offset by a corresponding reduction in the yield of common stock. This seemingly paradoxical result will be examined more closely below in connection with Proposition II.

A significant modification of Proposition I would be required only if the yield curve $r=r(D/S)$ were different for different borrowers, as might happen if creditors had marked preferences for the securities of a particular class of debtors. If, for example, corporations as a class were able to borrow at lower rates than individuals having equivalent personal leverage, then the average cost of capital to corporations might fall slightly, as leverage increased over some range, in reflection of this differential. In evaluating this possibility, however, remember that the relevant interest rate for our arbitrage operators is the rate on brokers' loans and, historically, that rate has not been noticeably higher than representative corporate rates.[19] The operations of holding companies and investment trusts which can borrow on terms comparable to operating companies represent still another force which could be expected to wipe out any marked or prolonged advantages from holding levered stocks.[20]

Although Proposition I remains unaffected as long as the yield curve is the same for all borrowers, the relation between common stock yields and leverage will no longer be the strictly linear one given by the original Proposition II. If r increases with leverage, the yield i will still tend to

[18] One normally minor qualification might be noted. Once we relax the assumption that all bonds have certain yields, our arbitrage operator faces the danger of something comparable to "gambler's ruin." That is, there is always the possibility that an otherwise sound concern—one whose long-run expected income is greater than its interest liability—might be forced into liquidation as a result of a run of temporary losses. Since reorganization generally involves costs, and because the operation of the firm may be hampered during the period of reorganization with lasting unfavorable effects on earnings prospects, we might perhaps expect heavily levered companies to sell at a slight discount relative to less heavily indebted companies of the same class.

[19] Under normal conditions, moreover, a substantial part of the arbitrage process could be expected to take the form, not of having the arbitrage operators go into debt on personal account to put the required leverage into their portfolios, but simply of having them reduce the amount of corporate bonds they already hold when they acquire underpriced unlevered stock. Margin requirements are also somewhat less of an obstacle to maintaining any desired degree of leverage in a portfolio than might be thought at first glance. Leverage could be largely restored in the face of higher margin requirements by switching to stocks having more leverage at the corporate level.

[20] An extreme form of inequality between borrowing and lending rates occurs, of course, in the case of preferred stocks, which can not be directly issued by individuals on personal account. Here again, however, we would expect that the operations of investment corporations plus the ability of arbitrage operators to sell off their holdings of preferred stocks would act to prevent the emergence of any substantial premiums (for this reason) on capital structures containing preferred stocks. Nor are preferred stocks so far removed from bonds as to make it impossible for arbitrage operators to approximate closely the risk and leverage of a corporate preferred stock by incurring a somewhat smaller debt on personal account.

rise as D/S increases, but at a decreasing rather than a constant rate. Beyond some high level of leverage, depending on the exact form of the interest function, the yield may even start to fall.[21] The relation between i and D/S could conceivably take the form indicated by the curve MD

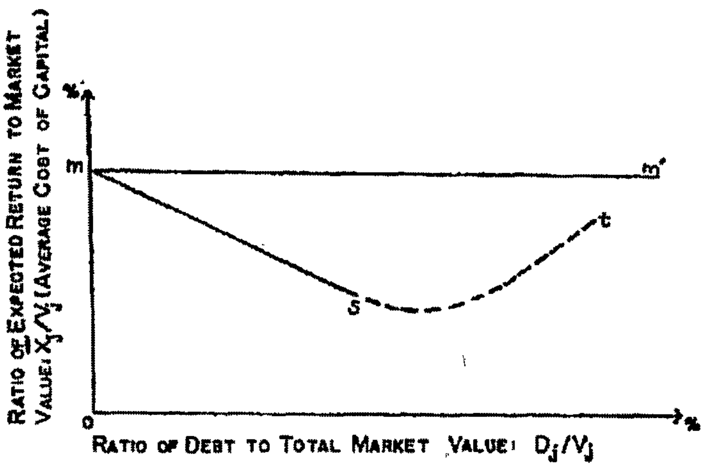

FIGURE 1

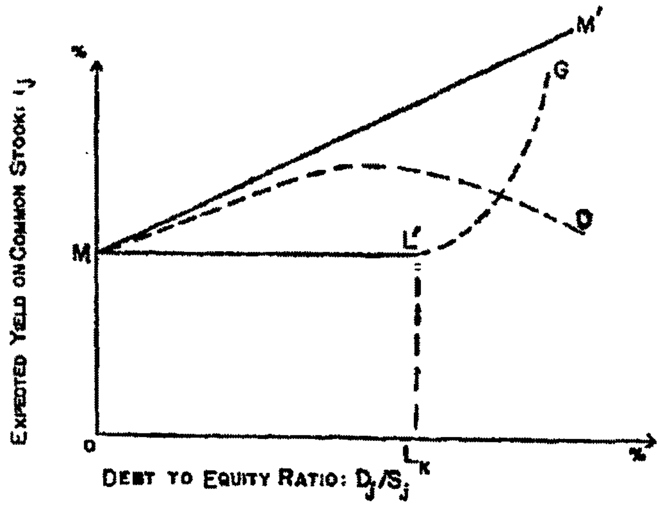

FIGURE 2

in Figure 2, although in practice the curvature would be much less pronounced. By contrast, with a constant rate of interest, the relation would be linear throughout as shown by line MM', Figure 2.

The downward sloping part of the curve MD perhaps requires some

[21] Since new lenders are unlikely to permit this much leverage (*cf.* note 17), this range of the curve is likely to be occupied by companies whose earnings prospects have fallen substantially since the time when their debts were issued.

comment since it may be hard to imagine why investors, other than those who like lotteries, would purchase stocks in this range. Remember, however, that the yield curve of Proposition II is a consequence of the more fundamental Proposition I. Should the demand by the risk-lovers prove insufficient to keep the market to the peculiar yield-curve MD, this demand would be reinforced by the action of arbitrage operators. The latter would find it profitable to own a pro-rata share of the firm as a whole by holding its stock *and* bonds, the lower yield of the shares being thus offset by the higher return on bonds.

D. *The Relation of Propositions I and II to Current Doctrines*

The propositions we have developed with respect to the valuation of firms and shares appear to be substantially at variance with current doctrines in the field of finance. The main differences between our view and the current view are summarized graphically in Figures 1 and 2. Our Proposition I [equation (4)] asserts that the average cost of capital, $\bar{X}_j^\tau/V_j$, is a constant for all firms j in class k, independently of their financial structure. This implies that, if we were to take a sample of firms in a given class, and if for each firm we were to plot the ratio of expected return to market value against some measure of leverage or financial structure, the points would tend to fall on a horizontal straight line with intercept ρ_k^τ, like the solid line mm' in Figure 1.[22] From Proposition I we derived Proposition II [equation (8)] which, taking the simplest version with r constant, asserts that, for all firms in a class, the relation between the yield on common stock and financial structure, measured by D_j/S_j, will approximate a straight line with slope $(\rho_k^\tau - r)$ and intercept ρ_k^τ This relationship is shown as the solid line MM' in Figure 2, to which reference has been made earlier.[23]

By contrast, the conventional view among finance specialists appears to start from the proposition that, other things equal, the earnings-price ratio (or its reciprocal, the times-earnings multiplier) of a firm's common stock will normally be only slightly affected by "moderate' amounts of debt in the firm's capital structure.[24] Translated into our no-

[22] In Figure 1 the measure of leverage used is D_j/V_j (the ratio of debt to market value) rather than D_j/S_j (the ratio of debt to equity), the concept used in the analytical development. The D_j/V_j measure is introduced at this point because it simplifies comparison and contrast of our view with the traditional position.

[23] The line MM' in Figure 2 has been drawn with a positive slope on the assumption that $\rho_k^\tau > r$, a condition which will normally obtain. Our Proposition II as given in equation (8) would continue to be valid, of course, even in the unlikely event that $\rho_k^\tau < r$, but the slope of MM' would be negative.

[24] See, *e.g.*, Graham and Dodd [6, pp. 464–66]. Without doing violence to this position, we can bring out its implications more sharply by ignoring the qualification and treating the yield as a virtual constant over the relevant range. See in this connection the discussion in Durand [3, esp. pp. 225–37] of what he calls the 'net income method' of valuation.

tation, it asserts that for any firm j in the class k,

$$\frac{\bar{X}_j{}^{\tau} - rD_j}{S_j} \equiv \frac{\bar{\pi}_j{}^{\tau}}{S_j} = i_k{}^*, \text{ a constant for } \frac{D_j}{S_j} \leq L_k \tag{13}$$

or, equivalently,

$$S_j = \bar{\pi}_j{}^{\tau}/i_k{}^* \tag{14}$$

Here $i_k{}^*$ represents the capitalization rate or earnings-price ratio on the common stock and L_k denotes some amount of leverage regarded as the maximum "reasonable" amount for firms of the class k. This assumed relationship between yield and leverage is the horizontal solid line ML' of Figure 2. Beyond L', the yield will presumably rise sharply as the market discounts "excessive" trading on the equity. This possibility of a rising range for high leverages is indicated by the broken-line segment $L'G$ in the figure.[25]

If the value of shares were really given by (14) then the over-all market value of the firm must be:

$$V_j \equiv S_j + D_j = \frac{\bar{X}_j{}^{\tau} - rD_j}{i_k{}^*} + D_j = \frac{\bar{X}_j{}^{\tau}}{i_k{}^*} + \frac{(i_k{}^* - r)D_j}{i_k{}^*} \tag{16}$$

That is, for any given level of expected total returns after taxes ($\bar{X}_j{}^{\tau}$) and assuming, as seems natural, that $i_k{}^* > r$, the value of the firm must tend to *rise* with debt;[26] whereas our Proposition I asserts that the value of the firm is completely independent of the capital structure. Another way of contrasting our position with the traditional one is in terms of the cost of capital. Solving (16) for $\bar{X}_j{}^{\tau}/V_j$ yields:

$$\bar{X}_j{}^{\tau}/V_j = i_k{}^* - (i_k{}^* - r)D_j/V_j. \tag{17}$$

According to this equation, the average cost of capital is not independent of capital structure as we have argued, but should tend to *fall* with increasing leverage, at least within the relevant range of moderate debt ratios, as shown by the line ms in Figure 1. Or to put it in more familiar terms, debt-financing should be "cheaper" than equity-financing if not carried too far.

When we also allow for the possibility of a rising range of stock yields for large values of leverage, we obtain a U-shaped curve like mst in

[25] To make it easier to see some of the implications of this hypothesis as well as to prepare the ground for later statistical testing, it will be helpful to assume that the notion of a critical limit on leverage beyond which yields rise rapidly, can be epitomized by a quadratic relation of the form:

$$\bar{\pi}_j{}^{\tau}/S_j = i_k{}^* + \beta(D_j/S_j) + \alpha(D_j/S_j)^2, \qquad \alpha > 0. \tag{15}$$

[26] For a typical discussion of how a promoter can, supposedly, increase the market value of a firm by recourse to debt issues, see W. J. Eiteman [4, esp. pp. 11–13].

Figure 1.[27] That a yield-curve for stocks of the form $ML'G$ in Figure 2 implies a U-shaped cost-of-capital curve has, of course, been recognized by many writers. A natural further step has been to suggest that the capital structure corresponding to the trough of the U is an "optimal capital structure" towards which management ought to strive in the best interests of the stockholders.[28] According to our model, by contrast, no such optimal structure exists—all structures being equivalent from the point of view of the cost of capital.

Although the falling, or at least U-shaped, cost-of-capital function is in one form or another the dominant view in the literature, the ultimate rationale of that view is by no means clear. The crucial element in the position—that the expected earnings-price ratio of the stock is largely unaffected by leverage up to some conventional limit—is rarely even regarded as something which requires explanation. It is usually simply taken for granted or it is merely asserted that this is the way the market behaves.[29] To the extent that the constant earnings-price ratio has a rationale at all we suspect that it reflects in most cases the feeling that moderate amounts of debt in "sound" corporations do not really add very much to the "riskiness" of the stock. Since the extra risk is slight, it seems natural to suppose that firms will not have to pay noticeably higher yields in order to induce investors to hold the stock.[30]

A more sophisticated line of argument has been advanced by David Durand [3, pp. 231–33]. He suggests that because insurance companies and certain other important institutional investors are restricted to debt securities, nonfinancial corporations are able to borrow from them at interest rates which are lower than would be required to compensate

[27] The U-shaped nature of the cost-of-capital curve can be exhibited explicitly if the yield curve for shares as a function of leverage can be approximated by equation (15) of footnote 25. From that equation, multiplying both sides by S_j we obtain: $\bar{\pi}_j^\tau = \bar{X}_j^\tau - rD_j = i_k^* S_j + \beta D_j + \alpha D_j^2 / S_j$ or, adding and subtracting $i_k^* D_k$ from the right-hand side and collecting terms,

$$\bar{X}_j^\tau = i_k^*(S_j + D_j) + (\beta + r - i_k^*)D_j + \alpha D^2_j/S_j. \tag{18}$$

Dividing (18) by V_j gives an expression for the cost of capital:

$$\begin{aligned}\bar{X}_j^\tau/V_j = i_k^* - (i_k^* - r - \beta)D_j/V_j + \alpha D_j^2/S_jV_j = i_k^* - (i_k^* - r - \beta)D_j/V_j \\ + \alpha(D_j/V_j)^2/(1 - D_j/V_j)\end{aligned} \tag{19}$$

which is clearly U-shaped since α is supposed to be positive.

[28] For a typical statement see S. M. Robbins [16, p. 307]. See also Graham and Dodd [6, pp. 468–74].

[29] See *e.g.*, Graham and Dodd [6, p. 466].

[30] A typical statement is the following by Guthmann and Dougall [7, p. 245]: "Theoretically it might be argued that the increased hazard from using bonds and preferred stocks would counterbalance this additional income and so prevent the common stock from being more attractive than when it had a lower return but fewer prior obligations. In practice, the extra earnings from 'trading on the equity' are often regarded by investors as more than sufficient to serve as a 'premium for risk' when the proportions of the several securities are judiciously mixed."

creditors in a free market. Thus, while he would presumably agree with our conclusions that stockholders could not gain from leverage in an unconstrained market, he concludes that they can gain under present institutional arrangements. This gain would arise by virtue of the "safety superpremium" which lenders are willing to pay corporations for the privilege of lending.[31]

The defective link in both the traditional and the Durand version of the argument lies in the confusion between investors' subjective risk preferences and their objective market opportunities. Our Propositions I and II, as noted earlier, do not depend for their validity on any assumption about individual risk preferences. Nor do they involve any assertion as to what is an adequate compensation to investors for assuming a given degree of risk. They rely merely on the fact that a given commodity cannot consistently sell at more than one price in the market; or more precisely that the price of a commodity representing a "bundle" of two other commodities cannot be consistently different from the weighted average of the prices of the two components (the weights being equal to the proportion of the two commodities in the bundle).

An analogy may be helpful at this point. The relations between $1/\rho_k$, the price per dollar of an unlevered stream in class k; $1/r$, the price per dollar of a sure stream, and $1/i_j$, the price per dollar of a levered stream j, in the kth class, are essentially the same as those between, respectively, the price of whole milk, the price of butter fat, and the price of milk which has been thinned out by skimming off some of the butter fat. Our Proposition I states that a firm cannot reduce the cost of capital—*i.e.*, increase the market value of the stream it generates—by securing part of its capital through the sale of bonds, even though debt money appears to be cheaper. This assertion is equivalent to the proposition that, under perfect markets, a dairy farmer cannot in general earn more for the milk he produces by skimming some of the butter fat and selling it separately, even though butter fat per unit weight, sells for more than whole milk. The advantage from skimming the milk rather than selling whole milk would be purely illusory; for what would be gained from selling the high-priced butter fat would be lost in selling the low-priced residue of thinned milk. Similarly our Proposition II—that the price per dollar of a levered stream falls as leverage increases—is an ex-

[31] Like Durand, Morton [15] contends "that the actual market deviates from [Proposition I] by giving a changing over-all cost of money at different points of the [leverage] scale" (p. 443, note 2, inserts ours), but the basis for this contention is nowhere clearly stated. Judging by the great emphasis given to the lack of mobility of investment funds between stocks and bonds and to the psychological and institutional pressures toward debt portfolios (see pp. 444–51 and especially his discussion of the optimal capital structure on p. 453) he would seem to be taking a position very similar to that of Durand above.

act analogue of the statement that the price per gallon of thinned milk falls continuously as more butter fat is skimmed off.[32]

It is clear that this last assertion is true as long as butter fat is worth more per unit weight than whole milk, and it holds even if, for many consumers, taking a little cream out of the milk (adding a little leverage to the stock) does not detract noticeably from the taste (does not add noticeably to the risk). Furthermore the argument remains valid even in the face of instituional limitations of the type envisaged by Durand. For suppose that a large fraction of the population habitually dines in restaurants which are required by law to serve only cream in lieu of milk (entrust their savings to institutional investors who can only buy bonds). To be sure the price of butter fat will then tend to be higher in relation to that of skimmed milk than in the absence such restrictions (the rate of interest will tend to be lower), and this will benefit people who eat at home and who like skim milk (who manage their own portfolio and are able and willing to take risk). But it will still be the case that a farmer cannot gain by skimming some of the butter fat and selling it separately (firm cannot reduce the cost of capital by recourse to borrowed funds).[33]

Our propositions can be regarded as the extension of the classical theory of markets to the particular case of the capital markets. Those who hold the current view—whether they realize it or not—must as-

[32] Let M denote the quantity of whole milk, B/M the proportion of butter fat in the whole milk, and let p_M, p_B and p_α denote, respectively, the price per unit weight of whole milk, butter fat and thinned milk from which a fraction α of the butter fat has been skimmed off. We then have the fundamental perfect market relation:

$$\text{(a)} \qquad p_\alpha(M - \alpha B) + p_B \alpha B = p_M M, \qquad 0 \leq \alpha \leq 1,$$

stating that total receipts will be the same amount $p_M M$, independently of the amount αB of butter fat that may have been sold separately. Since p_M corresponds to $1/\rho$, p_B to $1/r$, p_α to $1/i$, M to $\bar{X}$ and αB to rD, (a) is equivalent to Proposition I, $S+D=\bar{X}/\rho$. From (a) we derive:

$$\text{(b)} \qquad p_\alpha = p_M \frac{M}{M - \alpha B} - p_B \frac{\alpha B}{M - \alpha B}$$

which gives the price of thinned milk as an explicit function of the proportion of butter fat skimmed off; the function decreasing as long as $p_B > p_M$. From (a) also follows:

$$\text{(c)} \qquad 1/p_\alpha = 1/p_M + (1/p_M - 1/p_B) \frac{p_B \alpha B}{p_\alpha(M - \alpha B)}$$

which is the exact analogue of Proposition II, as given by (8).

[33] The reader who likes parables will find that the analogy with interrelated commodity markets can be pushed a good deal farther than we have done in the text. For instance, the effect of changes in the market rate of interest on the over-all cost of capital is the same as the effect of a change in the price of butter on the price of whole milk. Similarly, just as the relation between the prices of skim milk and butter fat influences the kind of cows that will be reared, so the relation between i and r influences the kind of ventures that will be undertaken. If people like butter we shall have Guernseys; if they are willing to pay a high price for safety, this will encourage ventures which promise smaller but less uncertain streams per dollar of physical assets.

sume not merely that there are lags and frictions in the equilibrating process—a feeling we certainly share,[34] claiming for our propositions only that they describe the central tendency around which observations will scatter—but also that there are large and *systematic* imperfections in the market which permanently bias the outcome. This is an assumption that economists, at any rate, will instinctively eye with some skepticism.

In any event, whether such prolonged, systematic departures from equilibrium really exist or whether our propositions are better descriptions of long-run market behavior can be settled only by empirical research. Before going on to the theory of investment it may be helpful, therefore, to look at the evidence.

E. *Some Preliminary Evidence on the Basic Propositions*

Unfortunately the evidence which has been assembled so far is amazingly skimpy. Indeed, we have been able to locate only two recent studies—and these of rather limited scope—which were designed to throw light on the issue. Pending the results of more comprehensive tests which we hope will soon be available, we shall review briefly such evidence as is provided by the two studies in question. (1) an analysis of the relation between security yields and financial structure for some 43 large electric utilities by F B. Allen [1], and (2) a parallel (unpublished) study by Robert Smith [19], for 42 oil companies designed to test whether Allen's rather striking results would be found in an industry with very different characteristics.[35] The Allen study is based on average figures for the years 1947 and 1948, while the Smith study relates to the single year 1953.

The Effect of Leverage on the Cost of Capital. According to the received view, as shown in equation (17) the average cost of capital, $\bar{X}^\tau/V$ should decline linearly with leverage as measured by the ratio D/V, at least through most of the relevant range.[36] According to Proposition I, the average cost of capital within a given class k should tend to have the same value ρ_k^τ independently of the degree of leverage. A simple test

[34] Several specific examples of the failure of the arbitrage mechanism can be found in Graham and Dodd [6, *e.g.*, pp. 646–48]. The price discrepancy described on pp. 646–47 is particularly curious since it persists even today despite the fact that a whole generation of security analysts has been brought up on this book!

[35] We wish to express our thanks to both writers for making available to us some of their original worksheets. In addition to these recent studies there is a frequently cited (but apparently seldom read) study by the Federal Communications Commission in 1938 [22] which purports to show the existence of an optimal capital structure or range of structures (in the sense defined above) for public utilities in the 1930's. By current standards for statistical investigations, however, this study cannot be regarded as having any real evidential value for the problem at hand.

[36] We shall simplify our notation in this section by dropping the subscript j used to denote a particular firm wherever this will not lead to confusion.

of the merits of the two alternative hypotheses can thus be carried out by correlating $\bar{X}^{\tau}/V$ with D/V If the traditional view is correct, the correlation should be significantly negative; if our view represents a better approximation to reality, then the correlation should not be significantly different from zero.

Both studies provide information about the average value of D—the market value of bonds and preferred stock—and of V—the market value of all securities.[37] From these data we can readily compute the ratio D/V and this ratio (expressed as a percentage) is represented by the symbol d in the regression equations below. The measurement of the variable $\bar{X}^{\tau}/V$, however, presents serious difficulties. Strictly speaking, the numerator should measure the expected returns net of taxes, but this is a variable on which no direct information is available. As an approximation, we have followed both authors and used (1) the average value of actual net returns in 1947 and 1948 for Allen's utilities; and (2) actual net returns in 1953 for Smith's oil companies. Net return is defined in both cases as the sum of interest, preferred dividends and stockholders' income net of corporate income taxes. Although this approximation to expected returns is undoubtedly very crude, there is no reason to believe that it will systematically bias the test in so far as the sign of the regression coefficient is concerned. The roughness of the approximation, however, will tend to make for a wide scatter. Also contributing to the scatter is the crudeness of the industrial classification, since especially within the sample of oil companies, the assumption that all the firms belong to the same class in our sense, is at best only approximately valid.

Denoting by x our approximation to $\bar{X}^{\tau}/V$ (expressed, like d, as a percentage), the results of the tests are as follows:

$$\text{Electric Utilities} \quad x = 5.3 + .006d \underset{(\pm .008)}{} \qquad r = .12$$

$$\text{Oil Companies} \quad x = 8.5 + .006d \underset{(\pm .024)}{} \qquad r = .04.$$

The data underlying these equations are also shown in scatter diagram form in Figures 3 and 4.

The results of these tests are clearly favorable to our hypothesis.

[37] Note that for purposes of this test preferred stocks, since they represent an *expected* fixed obligation, are properly classified with bonds even though the tax status of preferred dividends is different from that of interest payments and even though preferred dividends are really fixed only as to their maximum in any year. Some difficulty of classification does arise in the case of convertible preferred stocks (and convertible bonds) selling at a substantial premium, but fortunately very few such issues were involved for the companies included in the two studies. Smith included bank loans and certain other short-term obligations (at book values) in his data on oil company debts and this treatment is perhaps open to some question. However, the amounts involved were relatively small and check computations showed that their elimination would lead to only minor differences in the test results.

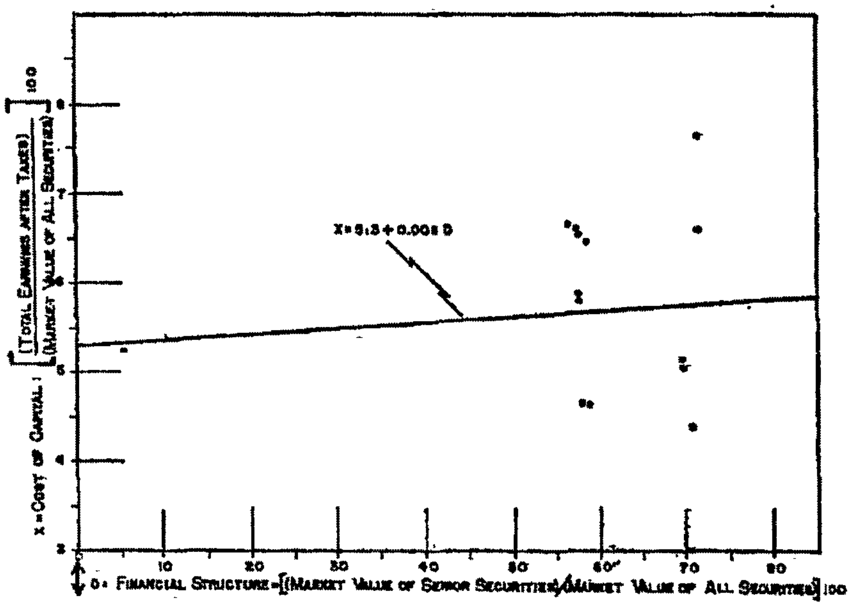

FIGURE 3. COST OF CAPITAL IN RELATION TO FINANCIAL STRUCTURE FOR 43 ELECTRIC UTILITIES, 1947–48

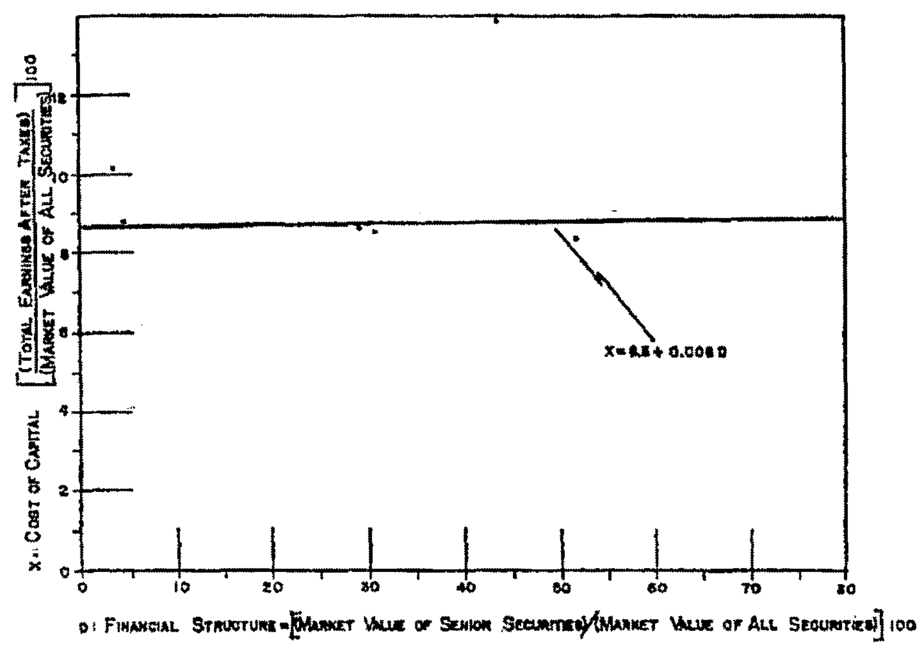

FIGURE 4. COST OF CAPITAL IN RELATION TO FINANCIAL STRUCTURE FOR 42 OIL COMPANIES, 1953

Both correlation coefficients are very close to zero and not statistically significant. Furthermore, the implications of the traditional view fail to be supported even with respect to the sign of the correlation. The data in short provide no evidence of any tendency for the cost of capital to fall as the debt ratio increases.[38]

It should also be apparent from the scatter diagrams that there is no hint of a curvilinear, U-shaped, relation of the kind which is widely believed to hold between the cost of capital and leverage. This graphical impression was confirmed by statistical tests which showed that for both industries the curvature was not significantly different from zero, its sign actually being opposite to that hypothesized.[39]

Note also that according to our model, the constant terms of the regression equations are measures of $\rho_k{}'$, the capitalization rates for unlevered streams and hence the average cost of capital in the classes in question. The estimates of 8.5 per cent for the oil companies as against 5.3 per cent for electric utilities appear to accord well with a priori expectations, both in absolute value and relative spread.

The Effect of Leverage on Common Stock Yields. According to our Proposition II—see equation 12 and Figure 2—the expected yield on common stock, $\bar{\pi}^\tau/S$, in any given class, should tend to increase with leverage as measured by the ratio D/S. The relation should tend to be linear and with positive slope through most of the relevant range (as in the curve MM' of Figure 2), though it might tend to flatten out if we move

[38] It may be argued that a test of the kind used is biased against the traditional view. The fact that both sides of the regression equation are divided by the variable V which may be subject to random variation might tend to impart a positive bias to the correlation. As a check on the results presented in the text, we have, therefore, carried out a supplementary test based on equation (16). This equation shows that, if the traditional view is correct, the market value of a company should, for given $\bar{X}^\tau$, increase with debt through most of the relevant range; according to our model the market value should be uncorrelated with D, given $\bar{X}^\tau$. Because of wide variations in the size of the firms included in our samples, all variables must be divided by a suitable scale factor in order to avoid spurious results in carrying out a test of equation (16). The factor we have used is the book value of the firm denoted by A. The hypothesis tested thus takes the specific form:

$$V/A = a + b(\bar{X}^\tau/A) + c(D/A)$$

and the numerator of the ratio X^τ/A is again approximated by actual net returns. The partial correlation between V/A and D/A should now be positive according to the traditional view and zero according to our model. Although division by A should, if anything, bias the results in favor of the traditional hypothesis, the partial correlation turns out to be only .03 for the oil companies and $-.28$ for the electric utilities. Neither of these coefficients is significantly different from zero and the larger one even has the wrong sign.

[39] The tests consisted of fitting to the data the equation (19) of footnote 27. As shown there, it follows from the U-shaped hypothesis that the coefficient α of the variable $(D/V)^2/(1-D/V)$, denoted hereafter by d^*, should be significant and positive. The following regression equations and partials were obtained:

$$\text{Electric Utilities} \quad x = 5.0 + .017d - .003d^*: r_{xd^*.d} = -.15$$

$$\text{Oil Companies} \quad x = 8.0 + .05d - .03d^*: r_{xd^*.d} = -.14.$$

far enough to the right (as in the curve MD'), to the extent that high leverage tends to drive up the cost of senior capital. According to the conventional view, the yield curve as a function of leverage should be a horizontal straight line (like ML') through most of the relevant range; far enough to the right, the yield may tend to rise at an increasing rate. Here again, a straight-forward correlation—in this case between $\bar{\pi}^\tau/S$ and D/S—can provide a test of the two positions. If our view is correct, the correlation should be significantly positive; if the traditional view is correct, the correlation should be negligible.

Subject to the same qualifications noted above in connection with $\bar{X}^\tau$, we can approximate $\bar{\pi}^\tau$ by actual stockholder net income.[40] Letting z denote in each case the approximation to $\bar{\pi}^\tau/S$ (expressed as a percentage) and letting h denote the ratio D/S (also in percentage terms) the following results are obtained:

$$\text{Electric Utilities} \quad z = \underset{(\pm .004)}{6.6 + .017h} \qquad r = .53$$

$$\text{Oil Companies} \quad z = \underset{(\pm .012)}{8.9 + .051h} \qquad r = .53.$$

These results are shown in scatter diagram form in Figures 5 and 6.

Here again the implications of our analysis seem to be borne out by the data. Both correlation coefficients are positive and highly significant when account is taken of the substantial sample size. Furthermore, the estimates of the coefficients of the equations seem to accord reasonably well with our hypothesis. According to equation (12) the constant term should be the value of ρ_k^τ for the given class while the slope should be $(\rho_k^\tau - r)$. From the test of Proposition I we have seen that for the oil companies the mean value of ρ_k^τ could be estimated at around 8.7 Since the average yield of senior capital during the period covered was in the order of $3\frac{1}{2}$ per cent, we should expect a constant term of about 8.7 per cent and a slope of just over 5 per cent. These values closely approximate the regression estimates of 8.9 per cent and 5.1 per cent respectively. For the electric utilities, the yield of senior capital was also on the order of $3\frac{1}{2}$ per cent during the test years, but since the estimate of the mean value of ρ_k^τ from the test of Proposition I was 5.6 per cent,

[40] As indicated earlier, Smith's data were for the single year 1953. Since the use of a single year's profits as a measure of expected profits might be open to objection we collected profit data for 1952 for the same companies and based the computation of $\bar{\pi}^\tau/S$ on the average of the two years. The value of $\bar{\pi}^\tau/S$ was obtained from the formula:

$$\left(\text{net earnings in 1952}\cdot\frac{\text{assets in '53}}{\text{assets in '52}} + \text{net earnings in '1953}\right)\frac{1}{2}$$
$$\div \text{ (average market value of common stock in '53).}$$

The asset adjustment was introduced as rough allowance for the effects of possible growth in the size of the firm. It might be added that the correlation computed with $\bar{\pi}^\tau/S$ based on net profits in 1953 alone was found to be only slightly smaller, namely .50.

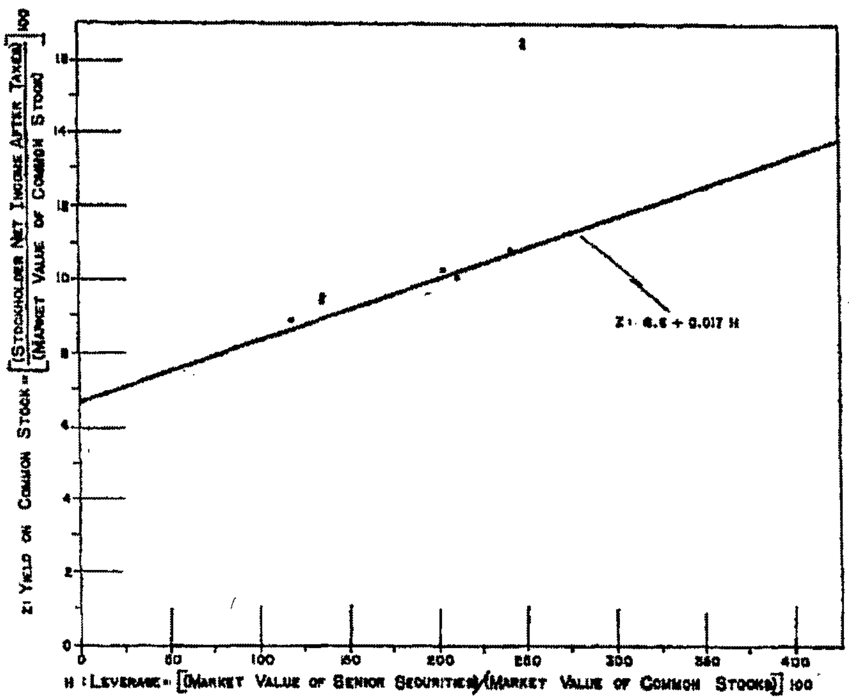

FIGURE 5. YIELD ON COMMON STOCK IN RELATION TO LEVERAGE FOR 43 ELECTRIC UTILITIES, 1947–48

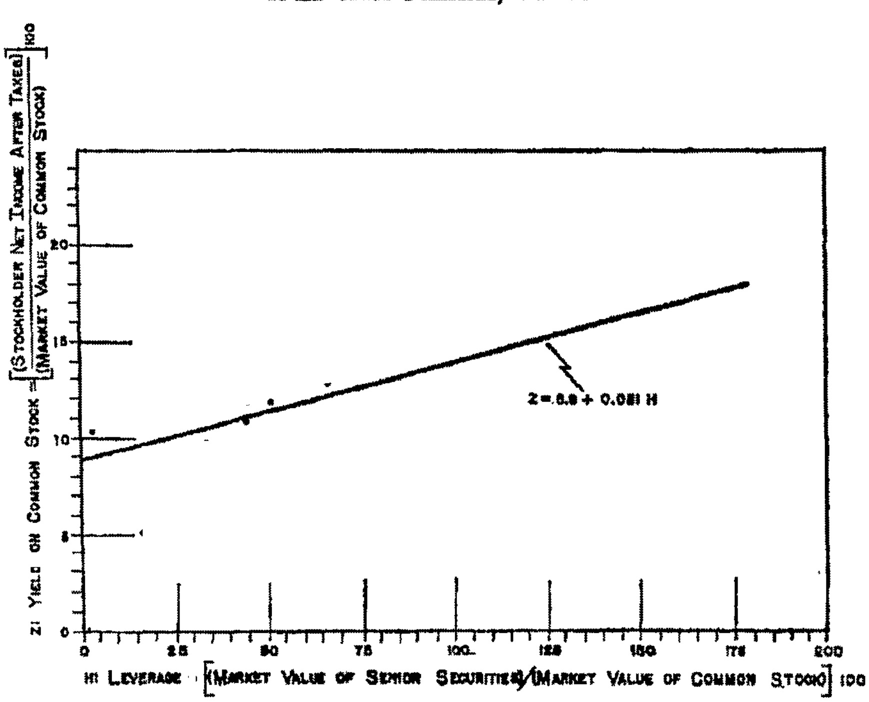

FIGURE 6. YIELD ON COMMON STOCK IN RELATION TO LEVERAGE FOR 42 OIL COMPANIES, 1952–53

the slope should be just above 2 per cent. The actual regression estimate for the slope of 1.7 per cent is thus somewhat low, but still within one standard error of its theoretical value. Because of this underestimate of the slope and because of the large mean value of leverage ($\bar{h}=160$ per cent) the regression estimate of the constant term, 6.6 per cent, is somewhat high, although not significantly different from the value of 5.6 per cent obtained in the test of Proposition I.

When we add a square term to the above equations to test for the presence and direction of curvature we obtain the following estimates:

$$\text{Electric Utilities} \quad z = 4.6 + .004h - .007h^2$$

$$\text{Oil Companies} \quad z = 8.5 + .072h - .016h^2.$$

For both cases the curvature is negative. In fact, for the electric utilities, where the observations cover a wider range of leverage ratios, the negative coefficient of the square term is actually significant at the 5 per cent level. Negative curvature, as we have seen, runs directly counter to the traditional hypothesis, whereas it can be readily accounted for by our model in terms of rising cost of borrowed funds.[41]

In summary, the empirical evidence we have reviewed seems to be broadly consistent with our model and largely inconsistent with traditional views. Needless to say much more extensive testing will be required before we can firmly conclude that our theory describes market behavior. Caution is indicated especially with regard to our test of Proposition II, partly because of possible statistical pitfalls[42] and partly because not all the factors that might have a systematic effect on stock yields have been considered. In particular, no attempt was made to test the possible influence of the dividend pay-out ratio whose role has tended to receive a great deal of attention in current research and thinking. There are two reasons for this omission. First, our main objective has been to assess the prima facie tenability of *our* model, and in this model, based as it is on rational behavior by investors, dividends per se play no role. Second, in a world in which the policy of dividend stabilization is widespread, there is no simple way of disentangling the true effect of dividend payments on stock prices from their apparent effect,

[41] That the yield of senior capital tended to rise for utilities as leverage increased is clearly shown in several of the scatter diagrams presented in the published version of Allen's study. This significant negative curvature between stock yields and leverage for utilities may be partly responsible for the fact, previously noted, that the constant in the linear regression is somewhat higher and the slope somewhat lower than implied by equation (12). Note also in connection with the estimate of ρ_k^τ that the introduction of the quadratic term reduces the constant considerably, pushing it in fact below the a priori expectation of 5.6, though the difference is again not statistically significant.

[42] In our test, *e.g.* the two variables z and h are both ratios with S appearing in the denominator, which may tend to impart a positive bias to the correlation (*cf.* note 38). Attempts were made to develop alternative tests, but although various possibilities were explored, we have so far been unable to find satisfactory alternatives.

the latter reflecting only the role of dividends as a proxy measure of long-term earning anticipations.[43] The difficulties just mentioned are further compounded by possible interrelations between dividend policy and leverage.[44]

II. *Implications of the Analysis for the Theory of Investment*

A. *Capital Structure and Investment Policy*

On the basis of our propositions with respect to cost of capital and financial structure (and for the moment neglecting taxes), we can derive the following simple rule for optimal investment policy by the firm:

Proposition III. If a firm in class k is acting in the best interest of the stockholders at the time of the decision, it will exploit an investment opportunity if and only if the rate of return on the investment, say ρ^*, is as large as or larger than ρ_k. That is, *the cut-off point for investment in the firm will in all cases be ρ_k and will be completely unaffected by the type of security used to finance the investment.* Equivalently, we may say that regardless of the financing used, the marginal cost of capital to a firm is equal to the average cost of capital, which is in turn equal to the capitalization rate for an unlevered stream in the class to which the firm belongs.[45]

To establish this result we will consider the three major financing alternatives open to the firm—bonds, retained earnings, and common stock issues—and show that in each case an investment is worth undertaking if, and only if, $\rho^* \geqq \rho_k$.[46]

Consider first the case of an investment financed by the sale of bonds. We know from Proposition I that the market value of the firm before the investment was undertaken was:[47]

$$V_0 = \overline{X}_0/\rho_k \qquad (20)$$

[43] We suggest that failure to appreciate this difficulty is responsible for many fallacious, or at least unwarranted, conclusions about the role of dividends.

[44] In the sample of electric utilities, there is a substantial negative correlation between yields and pay-out ratios, but also between pay-out ratios and leverage, suggesting that either the association of yields and leverage or of yields and pay-out ratios may be (at least partly) spurious. These difficulties however do not arise in the case of the oil industry sample. A preliminary analysis indicates that there is here no significant relation between leverage and pay-out ratios and also no significant correlation (either gross or partial) between yields and pay-out ratios.

[45] The analysis developed in this paper is essentially a comparative-statics, not a dynamic analysis. This note of caution applies with special force to Proposition III. Such problems as those posed by expected changes in r and in ρ_k over time will not be treated here. Although they are in principle amenable to analysis within the general framework we have laid out, such an undertaking is sufficiently complex to deserve separate treatment. *Cf.* note 17.

[46] The extension of the proof to other types of financing, such as the sale of preferred stock or the issuance of stock rights is straightforward.

[47] Since no confusion is likely to arise, we have again, for simplicity, eliminated the subscripts identifying the firm in the equations to follow. Except for ρ_k, the subscripts now refer to time periods.

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and that the value of the common stock was:

$$S_0 = V_0 - D_0. \tag{21}$$

If now the firm borrows I dollars to finance an investment yielding ρ^* its market value will become:

$$V_1 = \frac{\overline{X}_0 + \rho^* I}{\rho_k} = V_0 + \frac{\rho^* I}{\rho_k} \tag{22}$$

and the value of its common stock will be:

$$S_1 = V_1 - (D_0 + I) = V_0 + \frac{\rho^* I}{\rho_k} - D_0 - I \tag{23}$$

or using equation 21,

$$S_1 = S_0 + \frac{\rho^* I}{\rho_k} - I. \tag{24}$$

Hence $S_1 \gtreqless S_0$ as $\rho^* \gtreqless \rho_k$.[48]

To illustrate, suppose the capitalization rate for uncertain streams in the kth class is 10 per cent and the rate of interest is 4 per cent. Then if a given company had an expected income of 1,000 and if it were financed entirely by common stock we know from Proposition I that the market value of its stock would be 10,000. Assume now that the managers of the firm discover an investment opportunity which will require an outlay of 100 and which is expected to yield 8 per cent. At first sight this might appear to be a profitable opportunity since the expected return is double the interest cost. If, however, the management borrows the necessary 100 at 4 per cent, the total expected income of the company rises to 1,008 and the market value of the firm to 10,080. But the firm now will have 100 of bonds in its capital structure so that, paradoxically, the market value of the stock must actually be reduced from 10,000 to 9,980 as a consequence of this apparently profitable investment. Or, to put it another way, the gains from being able to tap cheap, borrowed funds are more than offset for the stockholders by the market's discounting of the stock for the added leverage assumed.

Consider next the case of retained earnings. Suppose that in the course of its operations the firm acquired I dollars of cash (without impairing

[48] In the case of bond-financing the rate of interest on bonds does not enter explicitly into the decision (assuming the firm borrows at the market rate of interest). This is true, moreover, given the conditions outlined in Section I.C, even though interest rates may be an increasing function of debt outstanding. To the extent that the firm borrowed at a rate other than the market rate the two I's in equation (24) would no longer be identical and an additional gain or loss, as the case might be, would accrue to the shareholders. It might also be noted in passing that permitting the two I's in (24) to take on different values provides a simple method for introducing underwriting expenses into the analysis.

the earning power of its assets). If the cash is distributed as a dividend to the stockholders their wealth W_0, after the distribution will be:

$$W_0 = S_0 + I = \frac{\overline{X}_0}{\rho_k} - D_0 + I \tag{25}$$

where $\overline{X}_0$ represents the expected return from the assets exclusive of the amount I in question. If however the funds are retained by the company and used to finance new assets whose expected rate of return is ρ^*, then the stockholders' wealth would become:

$$W_1 = S_1 = \frac{\overline{X}_0 + \rho^* I}{\rho_k} - D_0 = S_0 + \frac{\rho^* I}{\rho_k} \tag{26}$$

Clearly $W_1 \gtreqless W_0$ as $\rho^* \gtreqless \rho_k$ so that an investment financed by retained earnings raises the net worth of the owners if and only if $\rho^* > \rho_k$.[49]

Consider finally, the case of common-stock financing. Let P_0 denote the current market price per share of stock and assume, for simplicity, that this price reflects currently expected earnings only, that is, it does not reflect any future increase in earnings as a result of the investment under consideration.[50] Then if N is the original number of shares, the price per share is:

$$P_0 = S_0/N \tag{27}$$

and the number of new shares, M, needed to finance an investment of I dollars is given by:

$$M = \frac{I}{P_0} \tag{28}$$

As a result of the investment the market value of the stock becomes:

$$S_1 = \frac{\overline{X}_0 + \rho^* I}{\rho_k} - D_0 = S_0 + \frac{\rho^* I}{\rho_k} = NP_0 + \frac{\rho^* I}{\rho_k}$$

and the price per share:

$$P_1 = \frac{S_1}{N + M} = \frac{1}{N + M}\left[NP_0 + \frac{\rho^* I}{\rho_k}\right] \tag{29}$$

[49] The conclusion that ρ_k is the cut-off point for investments financed from internal funds applies not only to undistributed net profits, but to depreciation allowances (and even to the funds represented by the current sale value of any asset or collection of assets). Since the owners can earn ρ_k by investing funds elsewhere in the class, partial or total liquidating distributions should be made whenever the firm cannot achieve a marginal internal rate of return equal to ρ_k.

[50] If we assumed that the market price of the stock did reflect the expected higher future earnings (as would be the case if our original set of assumptions above were strictly followed) the analysis would differ slightly in detail, but not in essentials. The cut-off point for new investment would still be ρ_k, but where $\rho^* > \rho_k$ the gain to the original owners would be larger than if the stock price were based on the pre-investment expectations only.

Since by equation (28), $I = MP_0$, we can add MP_0 and subtract I from the quantity in bracket, obtaining:

$$
\begin{aligned}
P_1 &= \frac{1}{N+M}\left[(N+M)P_0 + \frac{\rho^* - \rho_k}{\rho_k} I\right] \\
&= P_0 + \frac{1}{N+M}\,\frac{\rho^* - \rho_k}{\rho_k} I > P_0 \text{ if,}
\end{aligned} \tag{30}
$$

and only if, $\rho^* > \rho_k$.

Thus an investment financed by common stock is advantageous to the current stockholders if and only if its yield exceeds the capitalization rate ρ_k.

Once again a numerical example may help to illustrate the result and make it clear why the relevant cut-off rate is ρ_k and not the current yield on common stock, i. Suppose that ρ_k is 10 per cent, r is 4 per cent, that the original expected income of our company is 1,000 and that management has the opportunity of investing 100 having an expected yield of 12 per cent. If the original capital structure is 50 per cent debt and 50 per cent equity, and 1,000 shares of stock are initially outstanding, then, by Proposition I, the market value of the common stock must be 5,000 or 5 per share. Furthermore, since the interest bill is $.04 \times 5{,}000 = 200$, the yield on common stock is $800/5{,}000 = 16$ per cent. It may then appear that financing the additional investment of 100 by issuing 20 shares to outsiders at 5 per share would dilute the equity of the original owners since the 100 promises to yield 12 per cent whereas the common stock is currently yielding 16 per cent. Actually, however, the income of the company would rise to 1,012; the value of the firm to 10,120; and the value of the common stock to 5,120. Since there are now 1,020 shares, each would be worth 5.02 and the wealth of the original stockholders would thus have been increased. What has happened is that the dilution in expected earnings per share (from .80 to .796) has been more than offset, in its effect upon the market price of the shares, by the decrease in leverage.

Our conclusion is, once again, at variance with conventional views,[51] so much so as to be easily misinterpreted. Read hastily, Proposition III seems to imply that the capital structure of a firm is a matter of indifference; and that, consequently, one of the core problems of corporate finance—the problem of the optimal capital structure for a firm—is no problem at all. It may be helpful, therefore, to clear up such possible misundertandings.

[51] In the matter of investment policy under uncertainty there is no single position which represents "accepted" doctrine. For a sample of current formulations, all very different from ours, see Joel Dean [2, esp. Ch. 3], M. Gordon and E. Shapiro [5], and Harry Roberts [17].

B. *Proposition III and Financial Planning by Firms*

Misinterpretation of the scope of Proposition III can be avoided by remembering that this Proposition tells us only that the type of instrument used to finance an investment is irrelevant to the question of whether or not the investment is worth while. This does not mean that the owners (or the managers) have no grounds whatever for preferring one financing plan to another; or that there are no other policy or technical issues in finance at the level of the firm.

That grounds for preferring one type of financial structure to another will still exist within the framework of our model can readily be seen for the case of common-stock financing. In general, except for something like a widely publicized oil-strike, we would expect the market to place very heavy weight on current and recent past earnings in forming expectations as to future returns. Hence, if the owners of a firm discovered a major investment opportunity which they felt would yield much more than ρ_k, they might well prefer not to finance it via common stock at the then ruling price, because this price may fail to capitalize the new venture. A better course would be a pre-emptive issue of stock (and in this connection it should be remembered that stockholders are free to borrow and buy). Another possibility would be to finance the project initially with debt. Once the project had reflected itself in increased actual earnings, the debt could be retired either with an equity issue at much better prices or through retained earnings. Still another possibility along the same lines might be to combine the two steps by means of a convertible debenture or preferred stock, perhaps with a progressively declining conversion rate. Even such a double-stage financing plan may possibly be regarded as yielding too large a share to outsiders since the new stockholders are, in effect, being given an interest in any similar opportunities the firm may discover in the future. If there is a reasonable prospect that even larger opportunities may arise in the near future and if there is some danger that borrowing now would preclude more borrowing later, the owners might find their interests best protected by splitting off the current opportunity into a separate subsidiary with independent financing. Clearly the problems involved in making the crucial estimates and in planning the optimal financial strategy are by no means trivial, even though they should have no bearing on the basic decision to invest (as long as $\rho^* \geqq \rho_k$).[52]

Another reason why the alternatives in financial plans may not be a matter of indifference arises from the fact that managers are concerned

[52] Nor can we rule out the possibility that the existing owners, if unable to use a financing plan which protects their interest, may actually prefer to pass up an otherwise profitable venture rather than give outsiders an "excessive" share of the business. It is presumably in situations of this kind that we could justifiably speak of a shortage of "equity capital," though this kind of market imperfection is likely to be of significance only for small or new firms.

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with more than simply furthering the interest of the owners. Such other objectives of the management—which need not be necessarily in conflict with those of the owners—are much more likely to be served by some types of financing arrangements than others. In many forms of borrowing agreements, for example, creditors are able to stipulate terms which the current management may regard as infringing on its prerogatives or restricting its freedom to maneuver. The creditors might even be able to insist on having a direct voice in the formation of policy.[53] To the extent, therefore, that financial policies have these implications for the management of the firm, something like the utility approach described in the introductory section becomes relevant to financial (as opposed to investment) decision-making. It is, however, the utility functions of the managers per se and not of the owners that are now involved.[54]

In summary, many of the specific considerations which bulk so large in traditional discussions of corporate finance can readily be superimposed on our simple framework without forcing any drastic (and certainly no systematic) alteration of the conclusion which is our principal concern, namely that for investment decisions, the marginal cost of capital is ρ_k.

C *The Effect of the Corporate Income Tax on Investment Decisions*

In Section I it was shown that when an unintegrated corporate income tax is introduced, the original version of our Proposition I,

$$\bar{X}/V = \rho_k = \text{a constant}$$

must be rewritten as:

$$\frac{(\bar{X} - rD)(1 - \tau) + rD}{V} \equiv \frac{\bar{X}^\tau}{V} = \rho_k{}^\tau = \text{a constant.} \tag{11}$$

Throughout Section I we found it convenient to refer to $\bar{X}^\tau/V$ as the cost of capital. The appropriate measure of the cost of capital relevant

[53] Similar considerations are involved in the matter of dividend policy. Even though the stockholders may be indifferent as to payout policy as long as investment policy is optimal, the management need not be so. Retained earnings involve far fewer threats to control than any of the alternative sources of funds and, of course, involve no underwriting expense or risk. But against these advantages management must balance the fact that sharp changes in dividend rates, which heavy reliance on retained earnings might imply, may give the impression that a firm's finances are being poorly managed, with consequent threats to the control and professional standing of the management.

[54] In principle, at least, this introduction of management's risk preferences with respect to financing methods would do much to reconcile the apparent conflict between Proposition III and such empirical findings as those of Modigliani and Zeman [14] on the close relation between interest rates and the ratio of new debt to new equity issues; or of John Lintner [12] on the considerable stability in target and actual dividend-payout ratios.

to investment decisions, however, is the ratio of the expected return *before* taxes to the market value, *i.e.*, $\bar{X}/V$ From (11) above we find:

$$\frac{\bar{X}}{V} = \frac{\rho_k^\tau - \tau r(D/V)}{1-\tau} = \frac{\rho_k^\tau}{1-\tau}\left[1 - \frac{\tau r D}{\rho_k^\tau V}\right] \tag{31}$$

which shows that the cost of capital now depends on the debt ratio, decreasing, as D/V rises, at the constant rate $\tau r/(1-\tau)$.[55] Thus, with a corporate income tax under which interest is a deductible expense, gains can accrue to stockholders from having debt in the capital structure, even when capital markets are perfect. The gains however are small, as can be seen from (31), and as will be shown more explicitly below.

From (31) we can develop the tax-adjusted counterpart of Proposition III by interpreting the term D/V in that equation as the proportion of debt used in any additional financing of V dollars. For example, in the case where the financing is entirely by new common stock, $D=0$ and the required rate of return ρ_k^S on a venture so financed becomes:

$$\rho_k^S = \frac{\rho_k^\tau}{1-\tau} \tag{32}$$

For the other extreme of pure debt financing $D=V$ and the required rate of return, ρ_k^D, becomes:

$$\rho_k^D = \frac{\rho_k^\tau}{1-\tau}\left[1 - \tau\frac{r}{\rho_k^\tau}\right] = \rho_k^S\left[1 - \tau\frac{r}{\rho_k^\tau}\right] = \rho_k^S - \frac{\tau}{1-\tau}r.\text{[56]} \tag{33}$$

For investments financed out of retained earnings, the problem of defining the required rate of return is more difficult since it involves a comparison of the tax consequences to the individual stockholder of receiving a dividend versus having a capital gain. Depending on the time of realization, a capital gain produced by retained earnings may be taxed either at ordinary income tax rates, 50 per cent of these rates, 25 per

[55] Equation (31) is amenable, in principle, to statistical tests similar to those described in Section I.E. However we have not made any systematic attempt to carry out such tests so far, because neither the Allen nor the Smith study provides the required information. Actually, Smith's data included a very crude estimate of tax liability, and, using this estimate, we did in fact obtain a negative relation between $\bar{X}/V$ and D/V. However, the correlation ($-.28$) turned out to be significant only at about the 10 per cent level. While this result is not conclusive, it should be remembered that, according to our theory, the slope of the regression equation should be in any event quite small. In fact, with a value of τ in the order of .5, and values of ρ_k^τ and r in the order of 8.5 and 3.5 per cent respectively (*cf.* Section I.E) an increase in D/V from 0 to 60 per cent (which is, approximately, the range of variation of this variable in the sample) should tend to reduce the average cost of capital only from about 17 to about 15 per cent.

[56] This conclusion does not extend to preferred stocks even though they have been classed with debt issues previously. Since preferred dividends except for a portion of those of public utilities are not in general deductible from the corporate tax, the cut-off point for new financing via preferred stock is exactly the same as that for common stock.

cent, or zero, if held till death. The rate on any dividends received in the event of a distribution will also be a variable depending on the amount of other income received by the stockholder, and with the added complications introduced by the current dividend-credit provisions. If we assume that the managers proceed on the basis of reasonable estimates as to the average values of the relevant tax rates for the owners, then the required return for retained earnings ρ_k^R can be shown to be:

$$\rho_k^R = \rho_k^\tau \frac{1}{1-\tau}\,\frac{1-\tau_d}{1-\tau_g} = \frac{1-\tau_d}{1-\tau_g}\,\rho_k^* \tag{34}$$

where τ_d is the assumed rate of personal income tax on dividends and τ_g is the assumed rate of tax on capital gains.

A numerical illustration may perhaps be helpful in clarifying the relationship between these required rates of return. If we take the following round numbers as representative order-of-magnitude values under present conditions: an after-tax capitalization rate ρ_k^τ of 10 per cent, a rate of interest on bonds of 4 per cent, a corporate tax rate of 50 per cent, a marginal personal income tax rate on dividends of 40 per cent (corresponding to an income of about $25,000 on a joint return), and a capital gains rate of 20 per cent (one-half the marginal rate on dividends), then the required rates of return would be: (1) 20 per cent for investments financed entirely by issuance of new common shares; (2) 16 per cent for investments financed entirely by new debt; and (3) 15 per cent for investments financed wholly from internal funds.

These results would seem to have considerable significance for current discussions of the effect of the corporate income tax on financial policy and on investment. Although we cannot explore the implications of the results in any detail here, we should at least like to call attention to the remarkably small difference between the "cost" of equity funds and debt funds. With the numerical values assumed, equity money turned out to be only 25 per cent more expensive than debt money, rather than something on the order of 5 times as expensive as is commonly supposed to be the case.[57] The reason for the wide difference is that the traditional

[57] See *e.g.* D. T. Smith [18]. It should also be pointed out that our tax system acts in other ways to reduce the gains from debt financing. Heavy reliance on debt in the capital structure, for example, commits a company to paying out a substantial proportion of its income in the form of interest payments taxable to the owners under the personal income tax. A debt-free company, by contrast, can reinvest in the business all of its (smaller) net income and to this extent subject the owners only to the low capital gains rate (or possibly no tax at all by virtue of the loophole at death). Thus, we should expect a high degree of leverage to be of value to the owners, even in the case of closely held corporations, primarily in cases where their firm was not expected to have much need for additional funds to expand assets and earnings in the future. To the extent that opportunities for growth were available, as they presumably would be for most successful corporations, the interest of the stockholders would tend to be better served by a structure which permitted maximum use of retained earnings.

view starts from the position that debt funds are several times cheaper than equity funds even in the absence of taxes, with taxes serving simply to magnify the cost ratio in proportion to the corporate rate. By contrast, in our model in which the repercussions of debt financing on the value of shares are taken into account, the *only* difference in cost is that due to the tax effect, and its magnitude is simply the tax on the "grossed up" interest payment. Not only is this magnitude likely to be small but our analysis yields the further paradoxical implication that the stockholders' gain from, and hence incentive to use, debt financing is actually smaller the lower the rate of interest. In the extreme case where the firm could borrow for practically nothing, the advantage of debt financing would also be practically nothing.

III. *Conclusion*

With the development of Proposition III the main objectives we outlined in our introductory discussion have been reached. We have in our Propositions I and II at least the foundations of a theory of the valuation of firms and shares in a world of uncertainty. We have shown, moreover, how this theory can lead to an operational definition of the cost of capital and how that concept can be used in turn as a basis for rational investment decision-making within the firm. Needless to say, however, much remains to be done before the cost of capital can be put away on the shelf among the solved problems. Our approach has been that of static, partial equilibrium analysis. It has assumed among other things a state of atomistic competition in the capital markets and an ease of access to those markets which only a relatively small (though important) group of firms even come close to possessing. These and other drastic simplifications have been necessary in order to come to grips with the problem at all. Having served their purpose they can now be relaxed in the direction of greater realism and relevance, a task in which we hope others interested in this area will wish to share.

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Turning now to the second and more intractable difficulty noted above, it would appear that firms in a given risk class would have utilized debt up to the limits of the institutional constraints facing them or up to the optimum amount, if such exists, to maximize V_L. Under both hypotheses, then, firms in a given class will tend to have the same debt-equity ratios. Consequently, a scatter diagram of either expected yields on shares or weighted averages of expected yields on bonds and shares plotted against debt-equity ratios should form a tight cluster (ideally a point).[16] The interpretation to be given the slope of a line fitted to such a scatter, such as the regression coefficients reported by MM [3, p. 281–87] for the oil and utility industries, is far from clear. Apart from measurement error, wide dispersion probably indicates the inclusion in the sample of firms from different risk classes. It may, therefore, be necessary to expand both hypotheses to include the effects of variation of institutional constraints and of optimal debt-equity ratios among risk classes to determine which of them describes the effects of leverage on market value in the real world. In the absence of such an undertaking it appears likely that tests quite different from those discussed here will be necessary to distinguish between the two hypotheses.

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The Cost of Capital, Corporation Finance, and the Theory of Investment: Reply

Although we can appreciate the ingenuity with which Messrs. Brewer and Michaelsen have developed parts of their argument, we fear that they have underestimated the limitations of their theoretical analysis and overestimated the significance of even their valid results for empirical applications.

[16] We abstract from the unsettled questions of how expected yields are to be measured or whether they exist in the sense used by MM. In much of the traditional literature expected and promised yields on bonds are not carefully distinguished. This might be the source of some of the current controversy, since the weighted average of expected yields on shares and promised yields on bonds will be a U-shaped curve under both hypotheses.

Taking up the various points in their paper in order, consider first their treatment of the much-mooted falling zone in the expected yield curve for shares. We referred to such a zone only very casually in our original paper and only because the possibility of its existence was a somewhat surprising implication of our Proposition I (namely, that with perfect capital markets, no taxes, and identical borrowing functions for firms and individuals, the value of any firm must be independent of its financial structure). We did not push the matter further at that time partly because we considered the point to be of no practical consequence and partly because there seemed to be no more that could validly be said about such a zone within the confines of our basic assumptions. Nothing in the Brewer-Michaelsen paper leads us to believe we were wrong in these judgments. To reason, as they do, that a ρ_k larger than the riskless rate of interest implies 'risk aversion," which in turn implies ρ_k greater than r everywhere, and hence a monotonically increasing yield curve is merely to play with words. No precise definition of "risk aversion' in this context is provided, let alone a proof that risk aversion (everywhere?) is implied by ρ_k greater than riskless r. Nor is this very surprising. The concept of risk aversion may perhaps have some heuristic value for rationalizing the gross behavior of the yield curves in commonsense terms; but we doubt that the term can ever be defined with sufficient precision and generality to derive conclusions of the kind Brewer and Michaelsen assert.[1]

Brewer and Michaelsen are on sounder ground in their derivation of the shape of the share-yield curve, *given* a bond-yield curve (or vice versa). That, as they show, is a straightforward matter of curve tracing, and we have no particular quarrel with it. We must admit, however, to being puzzled as to why they think their discussion of the curvature properties has any significant bearing on problems of empirical testing. As they themselves acknowledge, there would always be other and more direct implications by which to distinguish the two models (in particular, by reference to the behavior of total market value in response to differences in capital structure). Even in terms of the yield curves, there would be no very serious difficulties, in principle, in distinguishing between their curves *MA* and *ML'G* (particularly since the slope and curvature of *MA* can be directly predicted, as they show, from *ML'G* and an estimate of ρ_k). Whether, in practice, the two curves could be distinguished by simple regressions of yield on leverage, is, of course, another matter. But the uncertainties surrounding the usefulness of this particular type of test have nothing much to do with the sorts of questions raised by Brewer and Michaelsen.

Turning next to the issue of the proper measure of the value of the tax saving on debt, we fear that their proposed new expressions are based on a mis-

[1] The difficulties that arise with respect to defining risk aversion are merely one symptom of what is the real obstacle to specifying the relations between ρ_k and r, namely that these relations can be adequately treated only in the framework of a general equilibrium model of valuation under uncertainty. Hopefully, recent advances in this direction by Arrow (in "Le Rôle des Valeurs Boursières pour la Répartition la Meilleure des Risques," *International Colloquium on Econometrics*, 1952) and developed further by Hirshleifer ("Investment Decision Under Uncertainty," forthcoming), may open up some new lines of attack.

understanding (for which we must take some of the blame) of what we meant by the "certainty" of the tax deduction for interest payments. What we perhaps should have said more clearly is that our formulas would be valid when the tax deduction was exactly as certain or uncertain as the interest payment itself (or, equivalently, that the government's liability to the creditors is essentially the same as that of an ordinary stockholder).[2] Operationally, this means that the amount of the interest deduction for tax purposes is conditional on the amount of the interest actually paid to the bondholders either by the issuing corporation, or, in the event of the sale of the issuing firm, by the corporation acquiring the issuing firm and its accumulated tax losses. If so, the present value of the tax saving on interest should be computed by discounting the 'expected value of the tax saving"—the tax saving itself being in principle a random variable—at the very same rate the market applies to the stream of expected interest payments in arriving at the market value of the debt. And this, in turn, will lead to precisely our τD_L as the required present value. In practice, of course, the government's liability is not exactly the same as that of the stockholders. The complexity of our tax laws is such that cases can arise in which the government's liability to the creditors may be somewhat greater or may well be smaller. On the whole, however, we feel that our assumption represents a good first approximation; and certainly a far better one than that implied by Brewer and Michaelsen's equations (6), (7), and (12). These formulas, since they assume that the tax saving is certain in the literal sense, whether or not the interest is paid, amount to saying that the government assumes an absolutely unlimited liability to the bondholders and in perpetuity to boot!

Even if their formulas were acceptable descriptions of valuation under existing tax laws, we would find it hard to take seriously their claim to have disclosed new and "intractable" difficulties for empirical testing. For one thing, such discrepancies as would exist between their valuations and ours would be substantial only at levels of leverage far higher than any we normally observe. Nor would their higher estimate of the tax subsidy change the picture materially in the matter of choice of capital structure. We have noted

[2] In fact, under this "stockholder" interpretation for the government's share, it is possible to derive our tax formulas directly from the no-tax case. If we let the superscripts G, P, and T stand, respectively, for the government's "ownership" interest, the private sector's ownership interest, and the combined holdings of both groups; and if we assume that the government "owns" the fraction τ of the total common stock, then from Proposition I, we will have for an unlevered firm $V_U^T = S_U^P + S_U^G = \bar{X}/\rho_k$. The value of the purely private interest in that firm will then be

$$V_U^P = S_U^P = (1-\tau)V_U^T = \bar{X}(1-\tau)/\rho_k.$$

For a levered firm we will have

$$V_L^T = S_L^P + S_L^G + D_L^P = \bar{X}/\rho_k,$$

so that the private interest is

$$V_L^P = S_L^P + D_L^P = D_L^P + (1-\tau)[\bar{X}/\rho_k - D_L^P] = V_U^P + \tau D_L^P$$

exactly as in our equation (3).

many times that if one looks only at the tax subsidy to debt in our model (or at the "gains" from leverage under the simple traditional model), then one might expect every firm in the class to have the same debt ratio and that it would be as large as the tax laws or creditor restrictions permit. Similarly, under the more sophisticated traditional model, all firms would presumably always be at the unique 'optimum' debt ratio for the class. In the real world, however, such tight clustering does not seem to occur; and the differences in capital structure in most industries we have looked at are larger than can be convincingly accounted for by measurement errors or mixing of risk classes. We have always acknowledged that we have no completely specified model to account for these observed differences, though we think we can see some of the important elements out of which such a more general theory will someday be built.

In the meantime, however, empirical research need not grind to a halt. Differences in capital structure, for whatever reasons, do exist and they can be exploited to shed much light on the controversy over the effects of financial policy on market valuation. This is not to say, of course, that the empirical problems are easy or straightforward; on the contrary, they present a most severe challenge to the econometrician. Until this challenge has been accepted by finance specialists, may we propose a moratorium on all further speculations about what might or might not be true about valuation?

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Structural Unemployment: Comment

In a recent paper [1], Lowell Gallaway has entered the controversy over the reasons for the rising trend in the unemployment rate in the United States in the 'fifties and early 'sixties. He applies a novel test which purports to distinguish between two alternative explanations for the rising trend and concludes 'that the structural unemployment hypothesis is not a valid explanation of the increase in unemployment that has marked recent developments in the U.S. economy' [1, p. 712]. The purpose of this note is to show that Gallaway's test cannot distinguish between the alternative hypotheses and to suggest a test that can.

Briefly, the two alternative explanations are: (1) the level of aggregate demand has increasingly become inadequate, and (2) structural changes in the economy, due mainly to rapid technological change, have led to higher levels of frictional unemployment [2]. If the latter explanation is the correct one, Gallaway argues, the distribution of unemployment among the various sectors of the economy would be altered. "Therefore, if the structural argument is valid, the distribution of unemployment during the 1957-60 cycle should differ from that during the previous cycle" [1, pp. 710-12].

Gallaway refers to a straightforward method of measuring the degree of

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Public Meeting held January 11, 2007

Commissioners Present:

Wendell F. Holland, Chairman
James H. Cawley, Vice Chairman, Concurring & Dissenting Statement attached
Kim Pizzingrilli
Terrance J. Fitzpatrick

Pennsylvania Public Utility Commission,	R-00061366
Met-Ed Industrial Energy Users Group and	
Industrial Energy Consumers of Pennsylvania,	R-00061366C0001
William R. Lloyd, Jr. Small Business Advocate,	R-00061366C0002
Irwin A. Popowsky, Consumer Advocate,	R-00061366C0003
Met-Ed Industrial Energy Users Group and	
Industrial Energy Consumers of Pennsylvania,	R-00061366C0005
R.H. Sheppard Co. Inc.	R-00061366C0013
v.	
Metropolitan Edison Company	
Pennsylvania Public Utility Commission,	R-00061367
Penelec Industrial Customer Alliance and	
Industrial Energy Consumers of Pennsylvania,	R-00061367C0001
William R. Lloyd, Jr. Small Business Advocate,	R-00061367C0002
Irwin A. Popowsky, Consumer Advocate,	R-00061367C0003
Penelec Industrial Customer Alliance and	
Industrial Energy Consumers of Pennsylvania,	R-00061367C0005
Pierre Fortis,	R-00061367C0007
L.C. Rhodes	R-00061367C0008
v.	
Pennsylvania Electric Company	
Petition of Metropolitan Edison Company for	
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